

**ERRATA for the paper:** “Tables of Linear Congruential Generators of Different Sizes and Good Lattice Structure”, *Mathematics of Computation*, **68**, 225 (1999), 249–260.

Due to programming errors by the person who helped doing the computations, there are several errors in the tables of this paper. I sincerely apologize for this.

In Table 2 of the paper there are two cases with erroneous values. Table 2 below shows the corrected values for the two cases.

In Tables 4 and 5 of the paper, many values of the figure of merit, the ones that are not the best, are incorrect due to a programming error. However, all the best values (the ones with a \*) in the original tables are correct. In Table 5, the values of the  $a^*$  were not the inverse mod  $m$  of  $a$ , as advertized in the paper.

We reproduce below the corrected Tables 4 and 5 with the correct values.

Pierre L'Ecuyer, July 2005

TABLE 2. LCGs with Good Figures of Merit

| $m$                 | $a, a^*$   | $M_8(m, a)$ | $M_{16}(m, a)$ | $M_{32}(m, a)$ |
|---------------------|------------|-------------|----------------|----------------|
| $2^{10} - 3 = 1021$ | 65, 377    | 0.69069*    | 0.66317*       | 0.61872*       |
|                     | 644, 956   | 0.69069*    | 0.66317*       | 0.61872*       |
| $2^{12} - 3 = 4093$ | 209, 3858  | 0.67296*    | 0.60649        | 0.60649        |
|                     | 235, 3884  | 0.67296*    | 0.60649        | 0.60649        |
|                     | 352, 500   | 0.64259     | 0.64259*       | 0.64259*       |
|                     | 3593, 3741 | 0.64259     | 0.64259*       | 0.64259*       |

TABLE 4. LCGs with Good Figures of Merit, for  $m = 2^e$  and  $c$  odd

| $m$       | $a$                                    | $M_8(m, a)$ | $M_{16}(m, a)$ | $M_{32}(m, a)$ |
|-----------|--|-------------|----------------|----------------|
| $2^{30}$  | 438293613                              | 0.75107*    | 0.58300        | 0.58300        |
|           | 523592853                              | 0.70068     | 0.67686*       | 0.64694        |
|           | 116646453                              | 0.67718     | 0.67420        | 0.67107*       |
| $2^{31}$  | 37769685                               | 0.75896*    | 0.59146        | 0.59146        |
|           | 26757677                               | 0.68312     | 0.68289*       | 0.60858        |
|           | 20501397                               | 0.67787     | 0.67787        | 0.66548*       |
| $2^{32}$  | 2891336453                             | 0.75466*    | 0.56806        | 0.56806        |
|           | 29943829                               | 0.67429     | 0.67105*       | 0.58062        |
|           | 32310901                               | 0.65630     | 0.65336        | 0.65336*       |
| $2^{33}$  | 3766383685                             | 0.75029*    | 0.56952        | 0.56952        |
|           | 32684613                               | 0.68055     | 0.67255*       | 0.62595        |
|           | 5080384621                             | 0.66619     | 0.66604        | 0.66604*       |
| $2^{34}$  | 52765661                               | 0.74421*    | 0.54539        | 0.54539        |
|           | 50004141                               | 0.68442     | 0.67057*       | 0.65570        |
|           | 67037349                               | 0.69761     | 0.66579        | 0.66579*       |
| $2^{35}$  | 22475205                               | 0.74676*    | 0.51736        | 0.51736        |
|           | 15319397                               | 0.67472     | 0.66933*       | 0.60508        |
|           | 15550228621                            | 0.65734     | 0.65552        | 0.65552*       |
| $2^{36}$  | 12132445                               | 0.75179*    | 0.52329        | 0.51602        |
|           | 8572309                                | 0.66450     | 0.66389*       | 0.64445        |
|           | 33690453                               | 0.68461     | 0.65808        | 0.65760*       |
| $2^{40}$  | 330169576829                           | 0.75723*    | 0.46879        | 0.46879        |
|           | 42595477                               | 0.67959     | 0.66436*       | 0.63832        |
|           | 33261733                               | 0.65941     | 0.65477        | 0.65477*       |
| $2^{48}$  | 181465474592829                        | 0.75812*    | 0.54668        | 0.54668        |
|           | 77596615844045                         | 0.67653     | 0.66906*       | 0.61130        |
|           | 10430376854301                         | 0.66530     | 0.64759        | 0.64759*       |
| $2^{60}$  | 454339144066433781                     | 0.75956*    | 0.57465        | 0.57465        |
|           | 21828622668691829                      | 0.65844     | 0.65566*       | 0.63458        |
|           | 395904651965728677                     | 0.63944     | 0.63944        | 0.63944*       |
| $2^{63}$  | 9219741426499971445                    | 0.73715*    | 0.54235        | 0.54235        |
|           | 2806196910506780709                    | 0.69668     | 0.66519*       | 0.60754        |
|           | 3249286849523012805                    | 0.64507     | 0.63523        | 0.63523*       |
| $2^{64}$  | 2862933555777941757                    | 0.75673*    | 0.55283        | 0.54445        |
|           | 3202034522624059733                    | 0.66164     | 0.66041*       | 0.60256        |
|           | 3935559000370003845                    | 0.67938     | 0.63763        | 0.63763*       |
| $2^{96}$  | 75564983892026345434470042133          | 0.74760*    | 0.61011        | 0.61011        |
|           | 41898663544932533964435923957          | 0.64460     | 0.64460*       | 0.54346        |
|           | 22104684854187731770179339485          | 0.65329     | 0.63558        | 0.63287*       |
| $2^{128}$ | 47026247687942121848144207491837418733 | 0.74763*    | 0.58508        | 0.57619        |
|           | 52583122484843402430317208685168068605 | 0.70223     | 0.65994*       | 0.56182        |
|           | 47026247687942121848144207491837523525 | 0.64332     | 0.63077        | 0.62853*       |

TABLE 5. LCGs with Good Figures of Merit, for  $m = 2^e$  and  $c = 0$ 

| $m$       | $a, a^*$   | $M_8(m, a)$ | $M_{16}(m, a)$ | $M_{32}(m, a)$ |
|-----------|--|-------------|----------------|----------------|
| $2^{30}$  | 177911525, 285808365   | 0.74878*    | 0.61693        | 0.61693        |
|           | 156051869, 857580725   | 0.69501     | 0.67940*       | 0.64413        |
|           | 143133861, 770767661   | 0.69305     | 0.66791        | 0.66791*       |
| $2^{31}$  | 594156893, 989142773   | 0.75913*    | 0.50735        | 0.50735        |
|           | 558177141, 1487707357  | 0.68978     | 0.68749*       | 0.59450        |
|           | 602169653, 448899357   | 0.67295     | 0.67116        | 0.67116*       |
| $2^{32}$  | 741103597, 4109213157  | 0.75652*    | 0.60751        | 0.60751        |
|           | 1597334677, 851723965  | 0.70068     | 0.67686*       | 0.64694        |
|           | 747796405, 3425435293  | 0.66893     | 0.66001        | 0.66001*       |
| $2^{33}$  | 2185253333, 173170557  | 0.75896*    | 0.59146        | 0.59146        |
|           | 2174241325, 3554448805   | 0.68312     | 0.68289*       | 0.60858        |
|           | 2167985045, 8162762685   | 0.67787     | 0.67787        | 0.66548*       |
| $2^{34}$  | 11481271045, 16579283405   | 0.75466*    | 0.56806        | 0.56806        |
|           | 4324911125, 14504929085  | 0.67429     | 0.67105*       | 0.58062        |
|           | 4327278197, 7881103837   | 0.65630     | 0.65336        | 0.65336*       |
| $2^{35}$  | 8670442045, 10790122773  | 0.75818*    | 0.52727        | 0.52727        |
|           | 8622619205, 31842912397  | 0.68055     | 0.67255*       | 0.62595        |
|           | 22260253805, 7113024869  | 0.66619     | 0.66604        | 0.66604*       |
| $2^{36}$  | 4092856269, 31404866821  | 0.75662*    | 0.50169        | 0.50169        |
|           | 17229873325, 35216319269   | 0.68442     | 0.67057*       | 0.65570        |
|           | 17246906533, 12512050989   | 0.69761     | 0.66579        | 0.66579*       |
| $2^{48}$  | 49402601338917, 75935939978157   | 0.75801*    | 0.55089        | 0.55089        |
|           | 70189847242853, 209773542181229  | 0.67618     | 0.66857*       | 0.63609        |
|           | 21749276838573, 136842555189541  | 0.65702     | 0.64692        | 0.64692*       |
| $2^{60}$  | 276137484736346373, 672857982035536845   | 0.75277*    | 0.48916        | 0.48916        |
|           | 150878991426218621, 1108456478704721621  | 0.65527     | 0.65510*       | 0.59498        |
|           | 271413322654087621, 111008605039107341   | 0.64851     | 0.64851        | 0.64435*       |
| $2^{63}$  | 3512401965023503517, 3753721746144068021   | 0.74926*    | 0.50092        | 0.50092        |
|           | 2444805353187672469, 2079243811257762237   | 0.70937     | 0.66091*       | 0.61403        |
|           | 1987591058829310733, 4007969225820588997   | 0.64490     | 0.64060        | 0.63994*       |
| $2^{64}$  | 1181783497276652981, 13515856136758413469  | 0.76039*    | 0.42672        | 0.42672        |
|           | 7664345821815920749, 1865811235122147685   | 0.67778     | 0.66115*       | 0.54884        |
|           | 2685821657736338717, 6415128727920758069   | 0.65961     | 0.63932        | 0.63932*       |
| $2^{128}$ | 25096281518912105342191851917838718629,<br>310852368452748150078297415926143836461 | 0.76598*    | 0.55122        | 0.54891        |
|           | 23766634975743270097972271989927654085,<br>67836365537811707609274168323887561741  | 0.65708     | 0.65708*       | 0.55662        |
|           | 92563704562804186071655587898373606109,<br>297407245016942170064352095129111993717 | 0.63462     | 0.63462        | 0.63405*       |