Deep Learning and Al Yoshua Bengio

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Neural Networks & AI: Underlying Assumption



 There are principles giving rise to intelligence (machine, human or animal) via learning, simple enough that they can be described compactly, similarly to the laws of physics, i.e., our intelligence is not just the result of a huge bag of tricks and pieces of knowledge, but of general mechanisms to acquire knowledge.





Learning Multiple Levels of Abstraction (Bengio & LeCun 2007)

- The big payoff of deep learning is to facilitate learning higher levels of abstraction
- Higher-level abstractions can disentangle the factors of variation, which allows much easier generalization and transfer



Deep Learning AI Breakthroughs







A woman is throwing a <u>frisbee</u> in a park.

A dog is standing on a hardwood floor

Person

Dog

Chair

Computers have made huge strides in

perception,

manipulating languag games, reasoning, ...





Δ

2010-2012: breakthrough in speech recognition



Source: Microsoft

2012-2015: breakthrough in computer vision

- Graphics Processing Units (GPUs) + 10x more data
- 1,000 object categories,
- Facebook: millions of faces
- 2015: human-level performance





DEEP LEARNING REVOLUTIONIZING MEDICAL RESEARCH



Detecting Mitosis in Breast Cancer Cells



Understanding Gene Mutation to Prevent Disease

- IDSIA

of New Drugs

Predicting the Toxicity

- University of Toronto

Medical Image Classification Clinical Validation: Optical Colonoscopy

World's first real-time colon polyp malignancy determination from unmodified endoscope raw video with deep learning

	Accuracy
Imagia	> 90%, real time
GI Experts (Key Opinion Leaders)*	~ 90%
GI Doctors Trained by KOLs*	~ 75%

*(D. Rex, 2015)

Well received by expert clinicians and industry at many conferences, including Digestive Disease Week 2016



Separately Controlling Style & Content





Target style



[Luan et. al., 2017]





Computers become Creative with Deep Generative Models





 Progress in unsupervised generative neural nets allows them to synthesize a diversity images, sounds and text imitating unlabeled images, sounds or text

Predict a multi-modal future



Intelligence Needs Knowledge

• Learning:

powerful way to transfer knowledge to intelligent agents

- Failure of classical symbolic AI: a lot of knowledge is intuitive, difficult to put in rules & facts, not consciously accessible
- Solution: get knowledge from data & experience



Machine Learning, AI & No Free Lunch

- Five key ingredients for ML towards AI
 - 1. Lots & lots of data
 - 2. Very flexible models
 - 3. Enough computing power
 - 4. Computationally efficient inference
 - 5. Powerful priors that can defeat the curse of dimensionality

ML 101. What We Are Fighting Against: The Curse of Dimensionality

To generalize

locally, need representative examples for all relevant variations!

Classical solution: hope for a smooth enough target function, or make it smooth by handcrafting good features / kernel



Bypassing the curse of dimensionality

We need to build compositionality into our ML models

Just as human languages exploit compositionality to give representations and meanings to complex ideas

Exploiting compositionality can give an **exponential** gain in representational power

Distributed representations / embeddings: feature learning

Deep architecture: multiple levels of feature learning

Prior assumption: compositionality is useful to describe the world around us efficiently

Distributed Representations: The Power of Compositionality - Part 1

- Distributed (possibly sparse) representations, learned from data, can capture the meaning of the data and state
- Parallel composition of features: can be exponentially advantageous





Each feature can be discovered without the need for seeing the exponentially large number of configurations of the other features

Consider a network whose hidden units discover the following features:

Feature maps

- Person wears glasses
- Person is female
- Person is a child
- Etc.

If each of *n* feature requires *O(k)* parameters, need *O(nk)* examples

Non-parametric methods would require $O(n^d)$ examples

Hidden Units Discover Semantically Meaningful Concepts

- Zhou et al & Torralba, arXiv1412.6856 , ICLR 2015
- Network trained to recognize places, not objects



Deep Learning: Learning an Internal Representation

- Unlike other ML methods with either
 - no intermediate representation (linear)
 - or fixed (generally very high-dimensional) intermediate representations (SVMs, kernel machines)
- What is a good representation? Makes other tasks easier.



Learning multiple levels



(Lee, Grosse, Ranganath & Ng, ICML 2009) Successive model layers learn deeper intermediate representations



Prior: underlying factors & concepts compactly expressed w/ multiple levels of abstraction

Why Multiple Layers? The World is Compositional

Hierarchy of representations with increasing level of abstraction

- Each stage is a kind of trainable feature transform
- Image recognition: Pixel \rightarrow edge \rightarrow texton \rightarrow motif \rightarrow part \rightarrow object
- **Text**: Character \rightarrow word \rightarrow word group \rightarrow clause \rightarrow sentence \rightarrow story
- Speech: Sample \rightarrow spectral band \rightarrow sound $\rightarrow ... \rightarrow$ phone \rightarrow phoneme \rightarrow word



Exponential advantage of depth

- Expressiveness of deep networks with piecewise linear activation functions: exponential advantage for depth
- (Montufar et al & Bengio, NIPS 2014)
- Number of pieces distinguished for a network with depth L and *n_i* units per layer is at least

$$\left(\prod_{i=1}^{L-1} \left\lfloor \frac{n_i}{n_0} \right\rfloor^{n_0}\right) \sum_{j=0}^{n_0} \binom{n_L}{j}$$

or, if hidden layers have width n and input has size n₀

$$\Omega\left(\left(n_{n_0}^{\prime} \right)^{(L-1)n_0} n^{n_0} \right)$$

Not so terrible local minima: convexity is not needed

Myth busted:

- Local minima dominate in low-D, but_ saddle points dominate in high-D
- Most local minima are relatively close to the bottom (global minimum error)
 (Dauphin et al NIPS'2014,

Choromanska et al AISTATS'2015)







Recap: Machine Learning 101

- Family of functions $f_{ heta}$
- Tunable parameters θ
- Examples (x,y) sampled from unknown data generating distribution P(x,y)
- Loss fn ${\it L}$ compares target y and output $~~f_{\theta}(x)$, returns a number
- Regularizer R (typically depends on θ but possibly also on x & y)
- Training criterion for supervised learning: $C(\theta) = \operatorname{average}_{(x,y)\sim \operatorname{dataset}} L(f_{\theta}(x), y) + R(\theta, x, y)$
- Approximate minimization algorithm to search for good $\, heta$

Logistic Regression

- Predict the probability of a category y, given input x
 - *P*(*Y*=*y* / *X*=*x*)
- Simple extension of linear regression (binary case):
 - P(Y=1 | X=x) = sigmoid(b + w. x)
- Train by tuning (b,w) to maximize average log-likelihood

Average(log P(Y=y|X=x))

over training pairs (*x*, *y*), by gradientbased optimization

 This is a very shallow neural network (no hidden layer)





Hidden units

(from Hugo Larochelle)

$$a(\mathbf{x}) = b + \sum_{i} w_i x_i = b + \mathbf{w}^\top \mathbf{x}$$

- Neuron (output) activation
 - $h(\mathbf{x}) = g(a(\mathbf{x})) = g(b + \sum_{i} w_i x_i)$

 w_d

 x_d

 w_1

 x_1

- $\cdot \mathbf{w}$ are the connection weights
- b is the neuron bias
- $g(\cdot)$ is called the activation function

A neural network = running several logistic regressions at the same time

If we feed a vector of inputs through a bunch of logistic regression functions, then we get a vector of outputs



But we don't have to decide ahead of time what variables these logistic regressions are trying to predict!

A neural network = running several logistic regressions at the same time

... which we can feed into another logistic regression function



and it is the training criterion that will decide what those intermediate binary target variables should be, so as to make a good job of predicting the targets for the next layer, etc.

A neural network = running several logistic regressions at the same time

• Before we know it, we have a multilayer neural network....



Multilayer network as universal approximator

A series of non-linear transformations of the same type but different parameters A single but large enough hidden layer yields a **universal approximator**

More layers allow representing more complex functions with less parameters



- Universal approximator property does not guarantee
- easy optimization (low training error is found)
- 2. good generalization

Non-linearity = activation function

- Stacking linear layers: like one (factorized) linear layer
- Universal approximator : stack linear+nonlinear transformations
- Many types of non-linearities are possible: activation function
 - E.g. linear, sigmoid, tanh, rectifier (ReLU), softmax
- Breakthrough in 2011: it is much easier to train a deep multilayer network with rectifiers (ReLU) than with sigmoid or tanh, making it possible to train deep nets in a purely supervised way for the first first time (Glorot & Bengio AISTATS 2011)

$$g(a) = \operatorname{sigm}(a) = \frac{1}{1 + \exp(-a)}$$

Topics: softmax activation function

- For multi-class classification:
 - we need multiple outputs (I output per class)
 - $m{\cdot}$ we would like to estimate the conditional probability $p(y=c|\mathbf{x})$
- We use the softmax activation function at the output:

$$\mathbf{o}(\mathbf{a}) = \operatorname{softmax}(\mathbf{a}) = \left[\frac{\exp(a_1)}{\sum_c \exp(a_c)} \dots \frac{\exp(a_C)}{\sum_c \exp(a_c)}\right]^{-1}$$

- strictly positive
- sums to one
- Predicted class is the one with highest estimated probability

 $g(a) = \tanh(a) = \frac{\exp(a) - \exp(-a)}{\exp(a) + \exp(-a)} = \frac{\exp(2a) - 1}{\exp(2a) + 1}$

Topics: rectified linear activation function

- Bounded below by 0 (always non-negative)
- Not upper bounded
- Strictly increasing
- Tends to give neurons with sparse activities



 $g(a) = \operatorname{reclin}(a) = \max(0, a)$

Supervised training of an MLP by backpropagation



Requires(X,Y)=(input,target) pairs as training data

Iterative training by SGD

Topics: stochastic gradient descent (SGD)

(from Hugo Larochelle)

• Algorithm that performs updates after each example

initialize
$$\boldsymbol{\theta}$$
 ($\boldsymbol{\theta} \equiv \{\mathbf{W}^{(1)}, \mathbf{b}^{(1)}, \dots, \mathbf{W}^{(L+1)}, \mathbf{b}^{(L+1)}\}$)

- for N iterations
- To apply this algorithm to neural network training, we need
 - the loss function $l(\mathbf{f}(\mathbf{x}^{(t)}; \boldsymbol{\theta}), y^{(t)})$
 - a procedure to compute the parameter gradients $\nabla_{\boldsymbol{\theta}} l(\mathbf{f}(\mathbf{x}^{(t)}; \boldsymbol{\theta}), y^{(t)})$
 - the regularizer $\Omega({m heta})$ (and the gradient $abla_{{m heta}}\Omega({m heta})$)
 - initialization method

Motivation for backpropagation: gradient-based optimization

- Knowing how a small change of parameters influences loss L tells us how to change the parameters $\,\theta\,$

• The gradient $\frac{\partial L}{\partial \theta}$ measures the ratio of error change due to a small parameter change.

• Indicates the best local descent direction!

Why backprop is powerful

- With *n* parameters need O(*n*) computations to obtain *L*
- Also need only O(n) computations to obtain gradient by backprop
- Dumb alternative, by finite differences:

$$\frac{\partial L(\theta_i, \theta_{-i})}{\partial \theta_i} \approx \frac{L(\theta_i + \epsilon, \theta_{-i}) - L(\theta_i, \theta_{-i})}{\epsilon}$$

• But that would cost O(n²) instead of O(n) by backprop!

Confusion on the word BACKPROP

- **Backprop**: the backward accumulation procedure to compute gradients efficiently wrt a scalar (the loss)
- NOT THE SAME THING AS gradient descent, nor the MLP architecture.
- Backprop is not just used for supervised learning: also for unsupervised learning and RL, with different losses

Back-Prop & Chain Rule

- Compute gradient of example-wise loss wrt parameters, by considering intermediate values such as the outputs of neurons
- Simply applying the derivative chain rule wisely

$$z = f(y)$$
 $y = g(x)$ $\frac{\partial z}{\partial x} = \frac{\partial z}{\partial y}\frac{\partial y}{\partial x}$

Chain Rule

Also works if all these quantities are tensors, using the appropriate tensor products



 $\frac{\partial z}{\partial y} \Delta y$ $\frac{\partial y}{\partial y} \Delta x$ ΛT $\frac{\partial z}{\partial y} \frac{\partial y}{\partial x}$ X $rac{\partial z}{\partial x}$ $\frac{\partial z}{\partial y} \frac{\partial y}{\partial x}$

Multiple Paths Chain Rule



Multiple Paths Chain Rule - General



Chain Rule in Flow Graph z



Flow graph: any directed acyclic graph node = computation result arc = computation dependency

$$\{y_1, y_2, \ldots, y_n\}$$
 = successors of $\mathcal X$

$$\frac{\partial z}{\partial x} = \sum_{i=1}^{n} \frac{\partial z}{\partial y_i} \frac{\partial y_i}{\partial x}$$



How outputs could change to make error smaller



How he could change to make error smaller



How h1 could change to make error smaller



How W1 could change to make error smaller

Back-Prop in General Flow Graph



- 1. Fprop: visit nodes in topo-sort order
 - Compute value of node given predecessors
- 2. Bprop:
 - initialize output gradient = 1
 - visit nodes in reverse order:
 - Compute gradient wrt each node using gradient wrt successors

$$\{y_1, y_2, \ldots, y_n\}$$
 = successors of x

$$\frac{\partial z}{\partial x} = \sum_{i=1}^{n} \frac{\partial z}{\partial y_i} \frac{\partial y_i}{\partial x}$$

 $\bullet \bullet \bullet$

Back-Prop in Recurrent & Recursive Nets

- Replicate a parameterized function over different time steps or nodes of a DAG
- Output state at one time-step / node is used as input for another time-step / node



Automatic Differentiation



- The gradient computation can be automatically inferred from the symbolic expression of the fprop.
- Each node type needs to know how to compute its output and how to compute the gradient wrt its inputs given the gradient wrt its output

Easy and fast prototyping



Log-likelihood as loss function

(from Hugo Larochelle) **Topics:** loss function for classification

- Neural network estimates $f(\mathbf{x})_c = p(y = c | \mathbf{x})$
 - igwedge we could maximize the probabilities of $y^{(t)}$ given $\mathbf{x}^{(t)}$ in the training set
- To frame as minimization, we minimize the negative log-likelihood natural log (In)

$$l(\mathbf{f}(\mathbf{x}), y) = -\sum_{c} \mathbb{1}_{(y=c)} \log f(\mathbf{x})_{c} = -\log f(\mathbf{x})_{y}$$

- we take the log to simplify for numerical stability and math simplicity
- sometimes referred to as cross-entropy

Log-Likelihood for Neural Nets

- Estimating a conditional probability $\,P(Y|X)\,$
- Parametrize it by $P(Y|X) = P(Y|\omega = f_{\theta}(X))$
- Loss = $-\log P(Y|X)$
- E.g. Gaussian Y, $\omega = (\mu, \sigma)$ typically only μ is the network output, depends on X Equivalent to MSE criterion:

Loss = $-\log P(Y|X) = \log \sigma + ||f_{\theta}(X) - Y||^2 / \sigma^2$

• E.g. Multinoulli Y for classification,

$$\omega_i = P(Y = i | x) = f_{\theta,i}(X) = \operatorname{softmax}_i(a(X))$$

Loss = $-\log \omega_Y = -\log f_{\theta,Y}(X)$

Multiple Output Variables

• If they are conditionally independent (given X), the individual prediction losses add up:

 $-\log P(Y|X) = -\log P(Y_1, \dots, Y_k|X) = -\log \prod_i P(Y_i|X) = -\sum_i \log P(Y_i|X)$

- Likelihood if some Y'_i 's are missing: just ignore those losses
- If not conditionally independent, need to capture the conditional joint distribution $P(Y_1,\ldots Y_k|X)$
 - Example: output = image, sentence, tree, etc.
 - Similar to unsupervised learning problem of capturing joint
 - Exact likelihood may similarly be intractable, depending on model

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