## Deep Learning of Representations

#### **AAAI Tutorial**

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### Outline of the Tutorial

- 1. Motivations and Scope
- 2. Algorithms
- 3. Practical Considerations
- 4. Challenges

#### See (Bengio, Courville & Vincent 2013)

"Unsupervised Feature Learning and Deep Learning: A Review and New Perspectives" and <a href="http://www.iro.umontreal.ca/~bengioy/talks/deep-learning-tutorial-aaai2013.html">http://www.iro.umontreal.ca/~bengioy/talks/deep-learning-tutorial-aaai2013.html</a> for a pdf of the slides and a detailed list of references.

### Ultimate Goals

- Al
- Needs knowledge
- Needs learning (involves priors + optimization/search)
- Needs generalization
   (guessing where probability mass concentrates)
- Needs ways to fight the curse of dimensionality (exponentially many configurations of the variables to consider)
- Needs disentangling the underlying explanatory factors (making sense of the data)

## Representation Learning

Good features essential for successful ML



Handcrafting features vs learning them

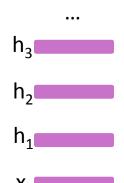
 Good representation: captures posterior belief about explanatory causes, disentangles these

factors of variation

Representation learning: guesses
 the features / factors / causes =
 good representation of observed data.

## Deep Representation Learning

Learn multiple levels of representation of increasing complexity/abstraction



- potentially exponential gain in expressive power
- brains are deep
- humans organize knowledge in a compositional way
- Better MCMC mixing in space of deeper representations (Bengio et al, ICML 2013)
- They work! SOTA on industrial-scale AI tasks (object recognition, speech recognition, language modeling, music modeling)

## Deep Learning

When the number of levels can be dataselected, this is a deep architecture



### A Good Old Deep Architecture: MLPs

### **Output layer**

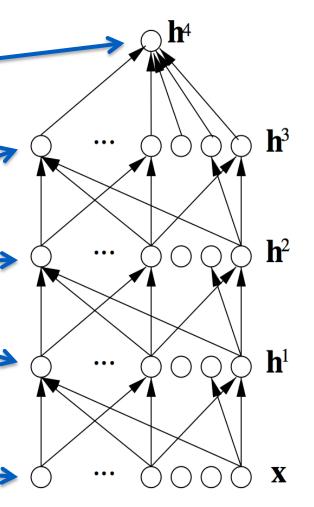
Here predicting a supervised target

### Hidden layers

These learn more abstract representations as you head up

#### Input layer

This has raw sensory inputs (roughly)



### A (Vanilla) Modern Deep Architecture

### **Optional** Output layer

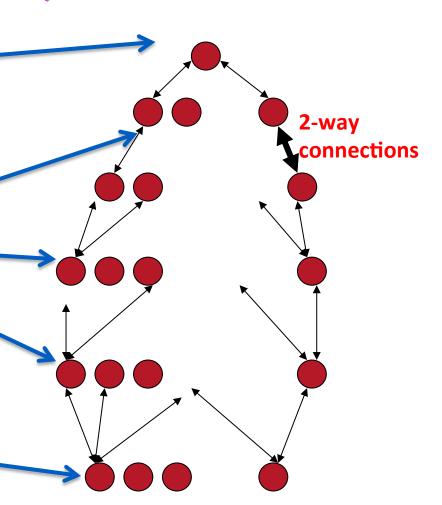
Here predicting or conditioning on a supervised target

### Hidden layers

These learn more abstract representations as you head up

#### Input layer

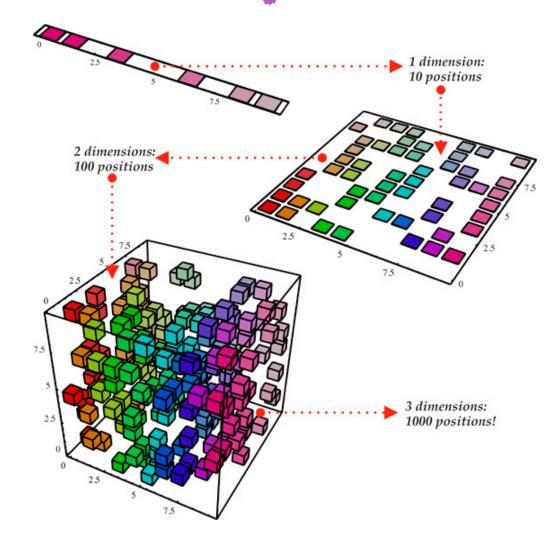
Inputs can be reconstructed, filled-in or sampled



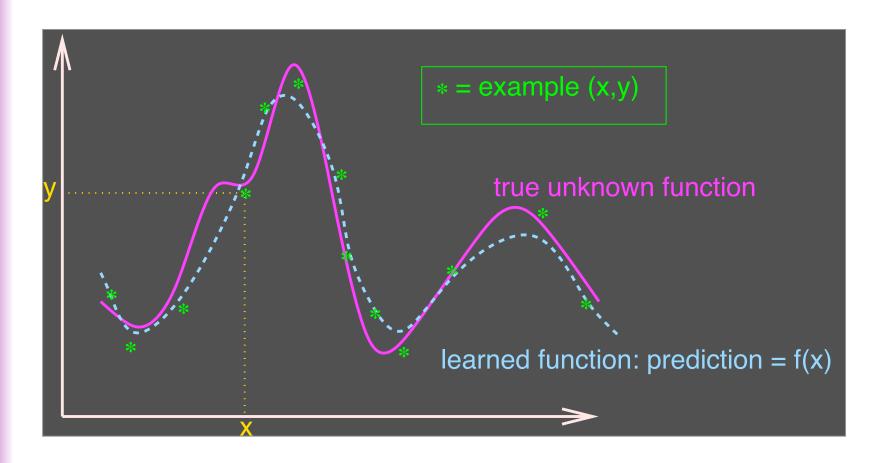
### ML 101. What We Are Fighting Against: The Curse of Dimensionality

To generalize locally, need representative examples for all relevant variations!

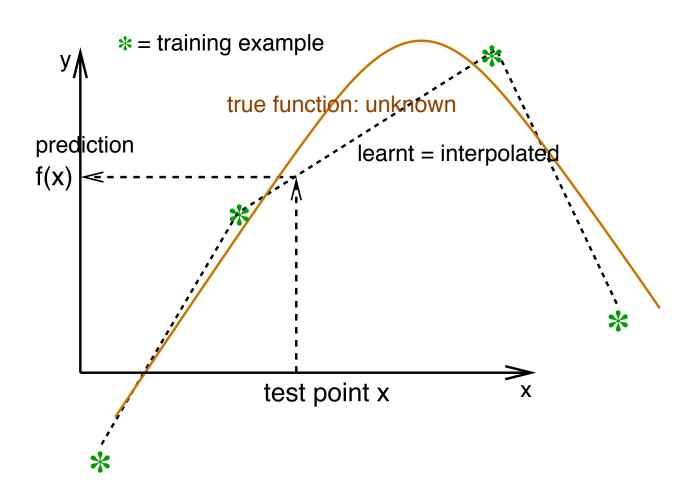
Classical solution: hope for a smooth enough target function, or make it smooth by handcrafting good features / kernel



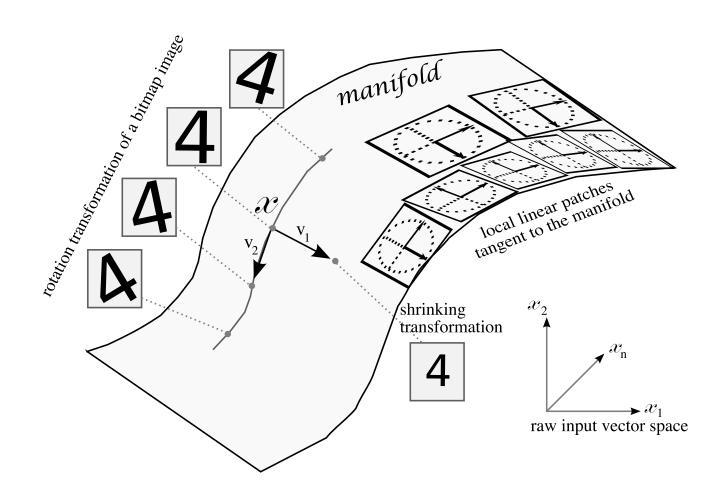
### Easy Learning



## Local Smoothness Prior: Locally Capture the Variations



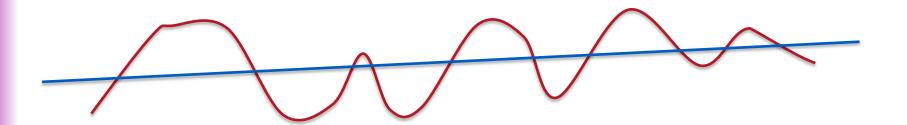
### However, Real Data Are near Highly Curved Sub-Manifolds



## Not Dimensionality so much as Number of Variations

(Bengio, Dellalleau & Le Roux 2007)

• Theorem: Gaussian kernel machines need at least *k* examples to learn a function that has *2k* zero-crossings along some line



 Theorem: For a Gaussian kernel machine to learn some maximally varying functions over d inputs requires O(2<sup>d</sup>) examples

### Putting Probability Mass where Structure is Plausible

- Empirical distribution: mass at training examples
- Smoothness: spread mass around
- Insufficient
- Guess some 'structure' and generalize accordingly

Is there any hope to generalize non-locally?

Yes! Need good priors!

#### Part 1

### Six Good Reasons to Explore Representation Learning

# #11 Learning features, not just handcrafting them

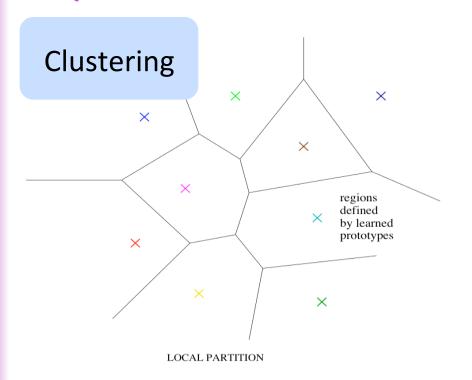
Most ML systems use very carefully hand-designed features and representations

Many practitioners are very experienced – and good – at such feature design (or kernel design)

"Machine learning" often reduces to linear models (including CRFs) and nearest-neighbor-like features/models (including n-grams, kernel SVMs, etc.)

Hand-crafting features is time-consuming, brittle, incomplete

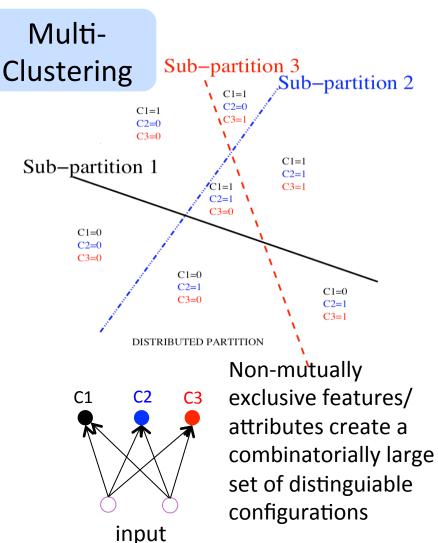
# #2 The need for distributed representations



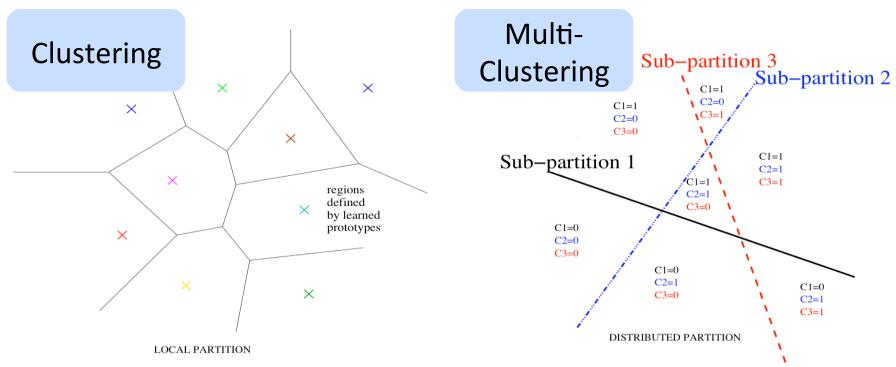
- Clustering, Nearest-Neighbors, RBF SVMs, local non-parametric density estimation & prediction, decision trees, etc.
- Parameters for each distinguishable region
- # of distinguishable regions is linear in # of parameters
- → No non-trivial generalization to regions without examples

## #2 The need for distributed representations

- Factor models, PCA, RBMs, Neural Nets, Sparse Coding, Deep Learning, etc.
- Each parameter influences many regions, not just local neighbors
- # of distinguishable regions grows almost exponentially with # of parameters
- GENERALIZE NON-LOCALLY TO NEVER-SEEN REGIONS



# #2 The need for distributed representations



Learning a set of features that are not mutually exclusive can be exponentially more statistically efficient than having nearest-neighbor-like or clustering-like models

## #3 Unsupervised feature learning

Today, most practical ML applications require (lots of) labeled training data

But almost all data is unlabeled

The brain needs to learn about 10<sup>14</sup> synaptic strengths

... in about 10<sup>9</sup> seconds

Labels cannot possibly provide enough information

Most information acquired in an unsupervised fashion

# #3 How do humans generalize from very few examples?

- They transfer knowledge from previous learning:
  - Representations
  - Explanatory factors

- Previous learning from: unlabeled data
  - + labels for other tasks
- Prior: shared underlying explanatory factors, in particular between P(x) and P(Y|x)

## #3 Sharing Statistical Strength by Semi-Supervised Learning

Hypothesis: P(x) shares structure with P(y|x)

semipurely supervised supervised

# #44 Learning multiple levels of representation

There is theoretical and empirical evidence in favor of multiple levels of representation

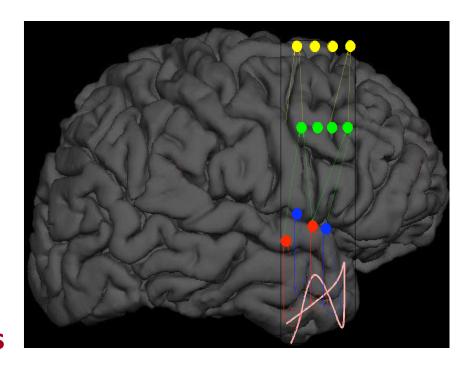
#### **Exponential gain for some families of functions**

Biologically inspired learning

Brain has a deep architecture

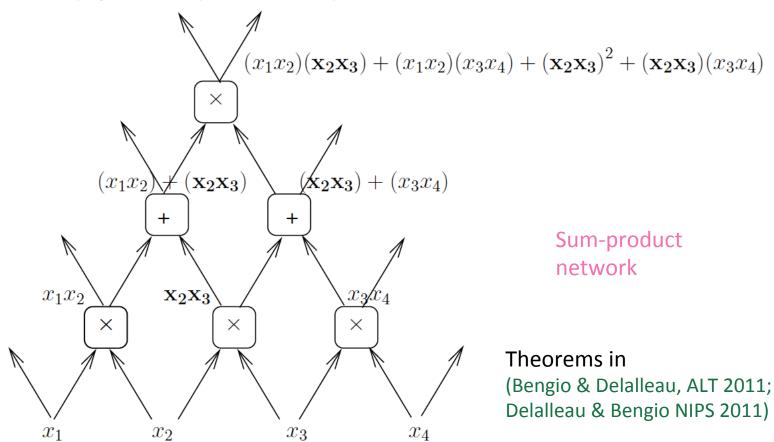
Cortex seems to have a generic learning algorithm

Humans first learn simpler concepts and then compose them into more complex ones



### #4 Sharing Components in a Deep Architecture

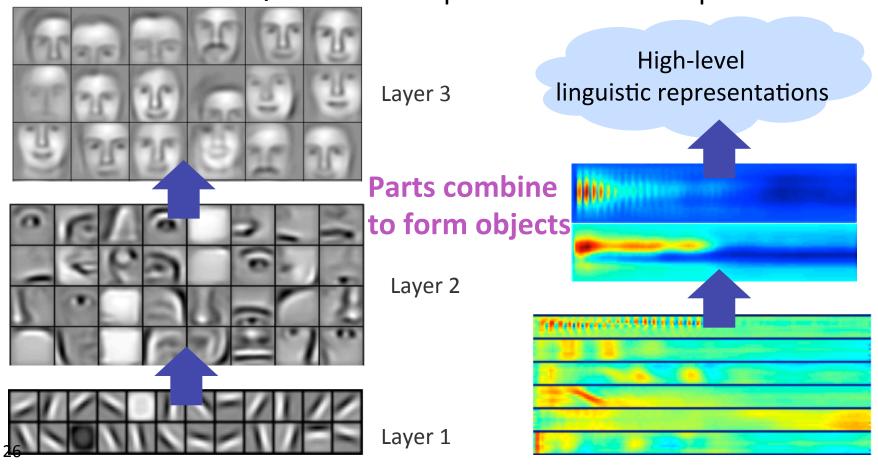
Polynomial expressed with shared components: advantage of depth may grow exponentially



# of representation (Lee, Pham, Largman & N

(Lee, Pham, Largman & Ng, NIPS 2009) (Lee, Grosse, Ranganath & Ng, ICML 2009)

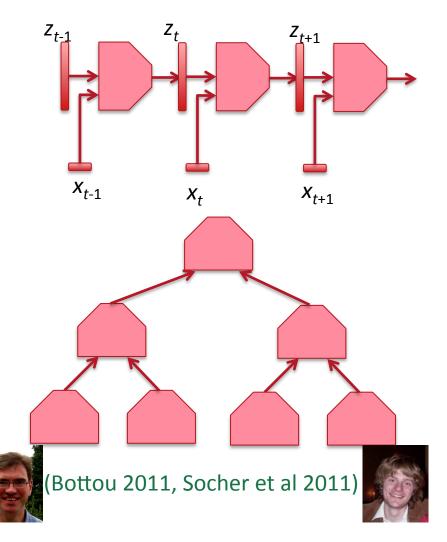
Successive model layers learn deeper intermediate representations



Prior: underlying factors & concepts compactly expressed w/ multiple levels of abstraction

# ## Handling the compositionality of human language and thought

- Human languages, ideas, and artifacts are composed from simpler components
- Recursion: the same operator (same parameters) is applied repeatedly on different states/components of the computation
- Result after unfolding = deep computation / representation

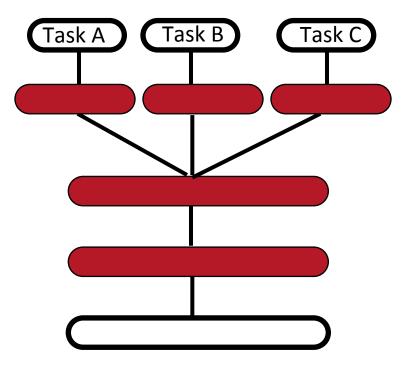


## #5 Multi-Task Learning

- Generalizing better to new tasks (tens of thousands!) is crucial to approach AI
- Deep architectures learn good intermediate representations that can be shared across tasks

(Collobert & Weston ICML 2008, Bengio et al AISTATS 2011)

 Good representations that disentangle underlying factors of variation make sense for many tasks because each task concerns a subset of the factors



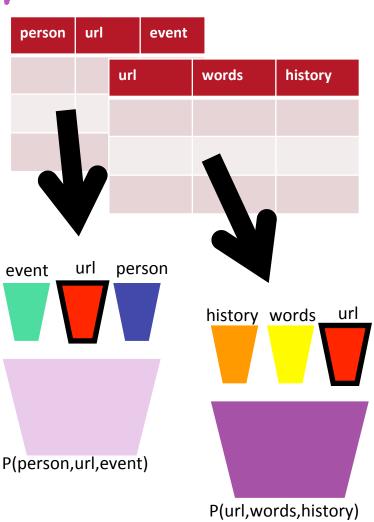
E.g. dictionary, with intermediate concepts re-used across many definitions

Prior: shared underlying explanatory factors between tasks

## #5 Combining Multiple Sources of Evidence with Shared Representations

- Traditional ML: data = matrix
- Relational learning: multiple sources, different tuples of variables
- Share representations of same types across data sources
- Shared learned representations help propagate information among data sources: e.g., WordNet, XWN, Wikipedia, FreeBase, ImageNet... (Bordes et al AISTATS 2012, ML J. 2013)
- FACTS = DATA
- Deduction = Generalization





## #5 Different object types represented in same space

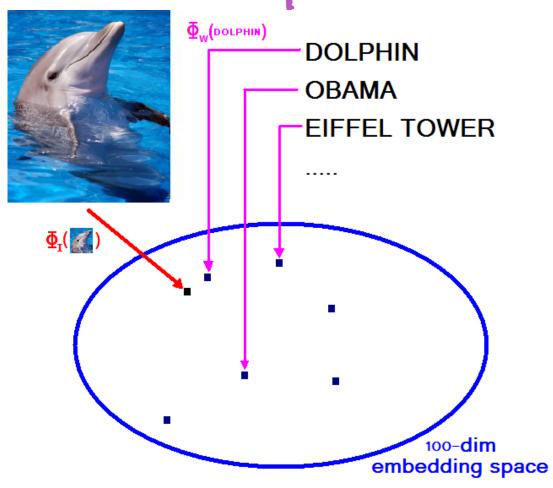


Google: S. Bengio, J. Weston & N.



(IJCAI 2011, NIPS'2010, JMLR 2010, ML J. 2010)





Learn  $\Phi_{\tau}(\cdot)$  and  $\Phi_{\omega}(\cdot)$  to optimize precision@k.

### #6 Invariance and Disentangling

Invariant features

• Which invariances?



Alternative: learning to disentangle factors

### #6 Emergence of Disentangling

- (Goodfellow et al. 2009): sparse auto-encoders trained on images
  - some higher-level features more invariant to geometric factors of variation
- (Glorot et al. 2011): sparse rectified denoising autoencoders trained on bags of words for sentiment analysis
  - different features specialize on different aspects (domain, sentiment)







## #6 Sparse Representations

- Just add a sparsifying penalty on learned representation (prefer 0s in the representation)
- Information disentangling (compare to dense compression)
- More likely to be linearly separable (high-dimensional space)
- Locally low-dimensional representation = local chart
- Hi-dim. sparse = efficient variable size representation

= data structure

Few bits of information



Many bits of information



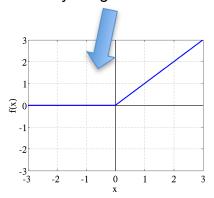
Prior: only few concepts and attributes relevant per example

### Deep Sparse Rectifier Neural Networks

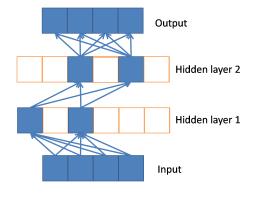
(Glorot, Bordes and Bengio AISTATS 2011), following up on (Nair & Hinton 2010) softplus RBMs

#### **Neuroscience motivations**

Leaky integrate-and-fire model



Rectifier f(x)=max(0,x)









#### **Machine learning motivations**

- Sparse representations
- Sparse gradients
  - Trains deep nets even w/o pretraining



Outstanding results by Krizhevsky et al 2012 killing the state-of-the-art on ImageNet 1000:

	1 <sup>st</sup> choice	Top-5
2 <sup>nd</sup> best		27% err
Previous SOTA	45% err	26% err
Krizhevsky et al	37% err	15% err

### Temporal Coherence and Scales

- Hints from nature about different explanatory factors:
  - Rapidly changing factors (often noise)
  - Slowly changing (generally more abstract)
  - Different factors at different time scales
- Exploit those hints to disentangle better!
- (Becker & Hinton 1993, Wiskott & Sejnowski 2002, Hurri & Hyvarinen 2003, Berkes & Wiskott 2005, Mobahi et al 2009, Bergstra & Bengio 2009)

## Bypassing the curse

We need to build compositionality into our ML models

Just as human languages exploit compositionality to give representations and meanings to complex ideas

Exploiting compositionality gives an exponential gain in representational power

Distributed representations / embeddings: feature learning

Deep architecture: multiple levels of feature learning

Prior: compositionality is useful to describe the world around us efficiently

# Bypassing the curse by sharing statistical strength

- Besides very fast GPU-enabled predictors, the main advantage of representation learning is statistical: potential to learn from less labeled examples because of sharing of statistical strength:
  - Unsupervised pre-training and semi-supervised training
  - Multi-task learning
  - Multi-data sharing, learning about symbolic objects and their relations

Unsupervised and Transfer Learning Challenge + Transfer Learning Challenge: Deep Learning 1st Place NIPS'2011 Transfer Raw data Learning 1 layer 2 layers Challenge Paper: ICML'2012 SYLVESTER VALID: ALC=0.8511 ICML'2011 SYLVESTER VALID: ALC=0.9316 workshop on 0.9770 0.95 Unsup. & 0.9 3 layers Transfer Learning \* 0.75 Area under the ROC cunve (AUC) 4 layers Log\_(Number of training examples) Log<sub>a</sub>(Number of training examples)



Despite prior investigation and understanding of many of the algorithmic techniques ...

Before 2006 training deep architectures was unsuccessful (except for convolutional neural nets when used by people who speak French)

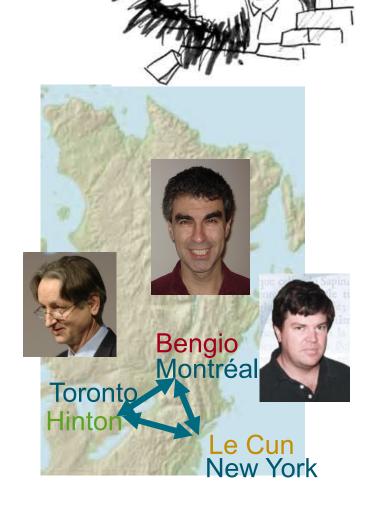
#### What has changed?

- New methods for unsupervised pre-training have been developed (variants of Restricted Boltzmann Machines = RBMs, regularized auto-encoders, sparse coding, etc.)
- New methods to successfully train deep supervised nets even without unsupervised pre-training
- Successful real-world applications, winning challenges and beating SOTAs in various areas, large-scale industrial apps

Major Breakthrough in 2006

 Ability to train deep architectures by using layer-wise unsupervised learning, whereas previous purely supervised attempts had failed

- Unsupervised feature learners:
  - RBMs
  - Auto-encoder variants
  - Sparse coding variants



# 2012: Industrial-scale success in speech recognition

- Google uses DL in their android speech recognizer (both serverside and on some phones with enough memory)
- Microsoft uses DL in their speech recognizer
- Error reductions on the order of 30%, a major progress



# Deep Networks for Speech Recognition: results from Google, IBM, Microsoft

task	Hours of training data	Deep net+HMM	GMM+HMM same data	GMM+HMM more data
Switchboard	309	16.1	23.6	17.1 (2k hours)
English Broadcast news	50	17.5	18.8	
Bing voice search	24	30.4	36.2	
Google voice input	5870	12.3		16.0 (lots more)
Youtube	1400	47.6	52.3	

(numbers taken from Geoff Hinton's June 22, 2012 Google talk)

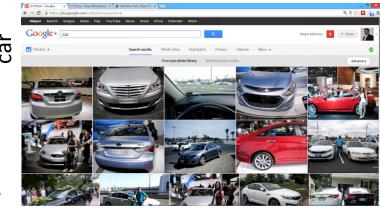
Industrial-scale success in object

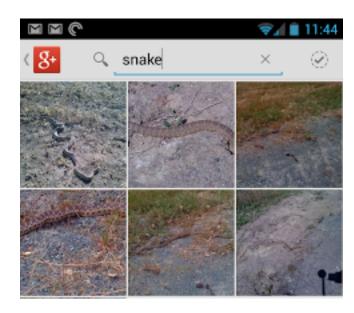
recognition

Krizhevsky, Sutskever & Hinton NIPS 2012

	1 <sup>st</sup> choice	Top-5
2 <sup>nd</sup> best		27% err
Previous SOTA	45% err	26% err
Krizhevsky et al	37% err	15% err

- Google incorporates DL in Google+ photo search, "A step across the semantic gap" (Google Research blog, June 12, 2013)
- Baidu now offers with similar services





baby



### More Successful Applications

- Microsoft uses DL for speech rec. service (audio video indexing), based on Hinton/Toronto's DBNs (Mohamed et al 2012)
- Google uses DL in its Google Goggles service, using Ng/Stanford DL systems, and in its Google+ photo search service, using deep convolutional nets
- NYT talks about these: http://www.nytimes.com/2012/06/26/technology/in-a-big-network-of-computers-evidence-of-machine-learning.html?\_r=1
- Substantially beating SOTA in language modeling (perplexity from 140 to 102 on Broadcast News) for speech recognition (WSJ WER from 16.9% to 14.4%)
   (Mikolov et al 2011) and translation (+1.8 BLEU) (Schwenk 2012)
- SENNA: Unsup. pre-training + multi-task DL reaches SOTA on POS, NER, SRL, chunking, parsing, with >10x better speed & memory (Collobert et al 2011)
- Recursive nets surpass SOTA in paraphrasing (Socher et al 2011)
- Denoising AEs substantially beat SOTA in sentiment analysis (Glorot et al 2011)
- Contractive AEs SOTA in knowledge-free MNIST (.8% err) (Rifai et al NIPS 2011)
- Le Cun/NYU's stacked PSDs most accurate & fastest in pedestrian detection and DL in top 2 winning entries of German road sign recognition competition

### Already Many NLP Applications of DL

- Language Modeling (Speech Recognition, Machine Translation)
- Acoustic Modeling
- Part-Of-Speech Tagging
- Chunking
- Named Entity Recognition
- Semantic Role Labeling
- Parsing
- Sentiment Analysis
- Paraphrasing
- Question-Answering
- Word-Sense Disambiguation

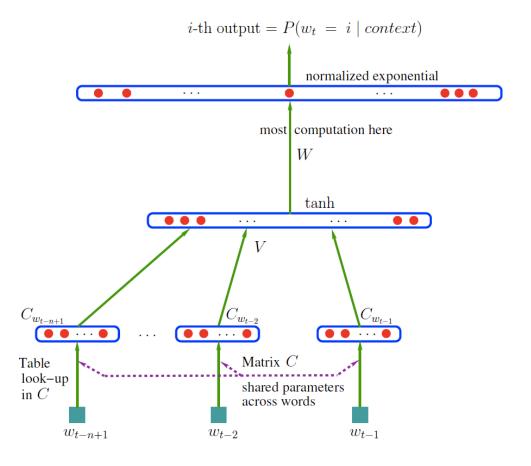
#### Neural Language Model

 Bengio et al NIPS'2000 and JMLR 2003 "A Neural Probabilistic

Language Model"

 Each word represented by a distributed continuousvalued code vector = embedding

 Generalizes to sequences of words that are semantically similar to training sequences





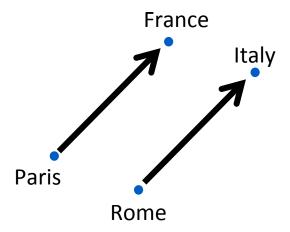


### Neural word embeddings - visualization



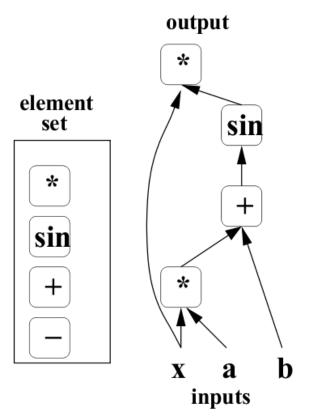
# Analogical Representations for Free (Mikolov et al, ICLR 2013)

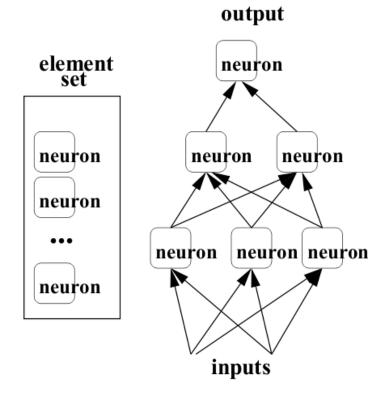
- Semantic relations appear as linear relationships in the space of learned representations
- King Queen ≈ Man Woman
- Paris France + Italy ≈ Rome



### More about depth

### Architecture Depth





# Deep Architectures are More Expressive

Theoretical arguments:

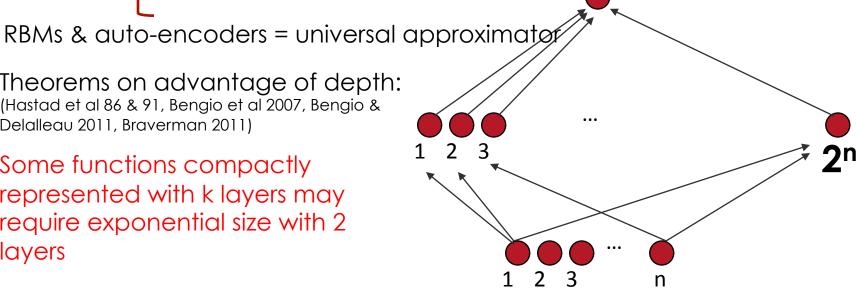
Logic gates 2 layers of Formal neurons RBF units

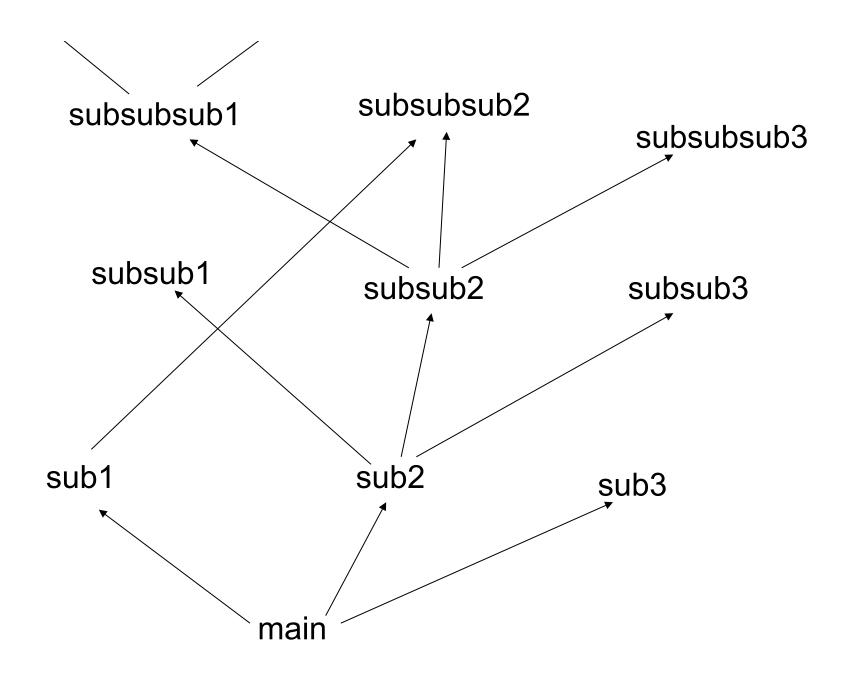
= universal approximator

Theorems on advantage of depth:

(Hastad et al 86 & 91, Bengio et al 2007, Bengio & Delalleau 2011, Braverman 2011)

Some functions compactly represented with k layers may require exponential size with 2 layers

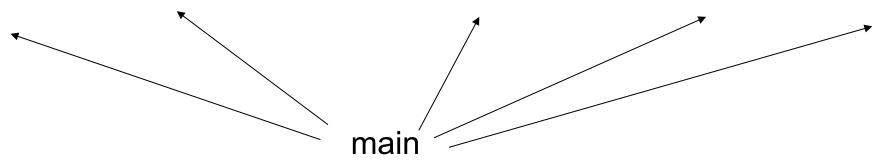




"Deep" computer program

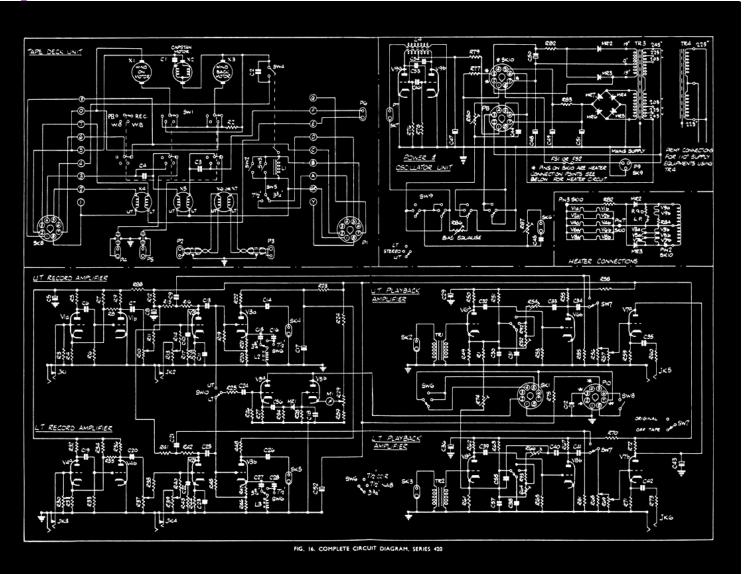
subroutine1 includes subsub1 code and subsub2 code and subsubsub1 code

subroutine2 includes subsub2 code and subsub3 code and subsubsub3 code and ...

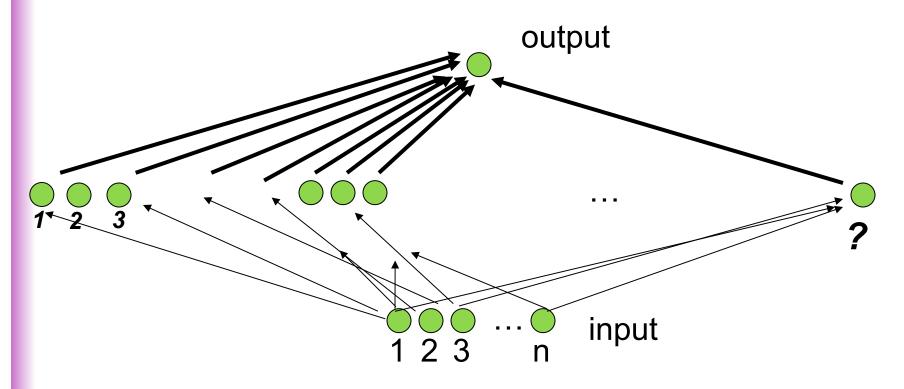


"Shallow" computer program

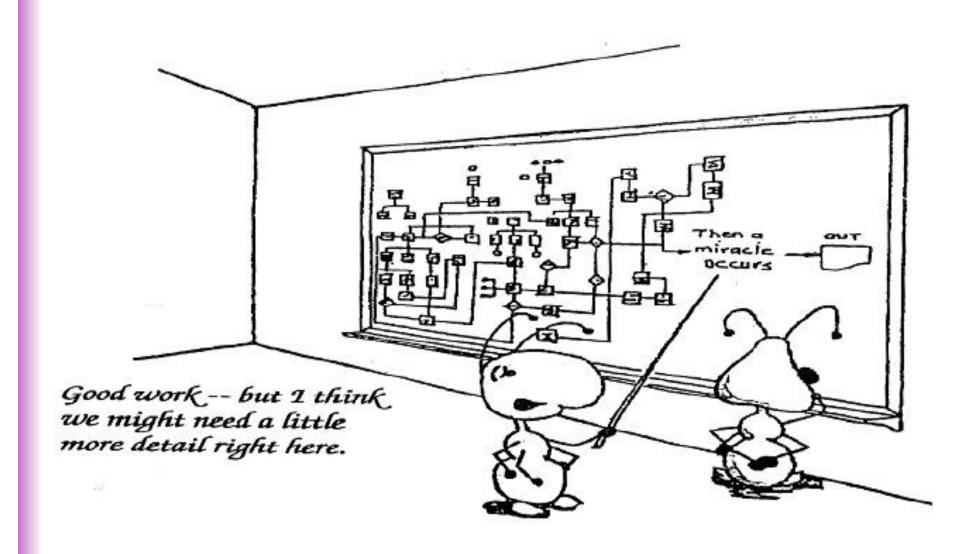
#### "Deep" circuit



#### "Shallow" circuit



Falsely reassuring theorems: one can approximate any reasonable (smooth, boolean, etc.) function with a 2-layer architecture

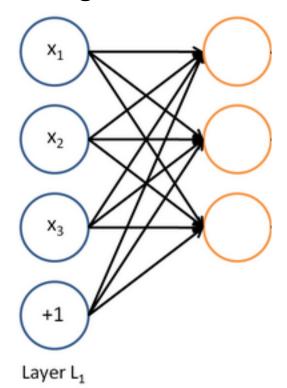


#### Part 2

### Representation Learning Algorithms

# A neural network = running several logistic regressions at the same time

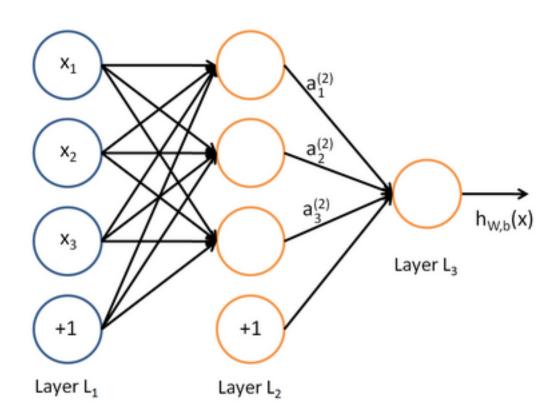
If we feed a vector of inputs through a bunch of logistic regression functions, then we get a vector of outputs



But we don't have to decide ahead of time what variables these logistic regressions are trying to predict!

# A neural network = running several logistic regressions at the same time

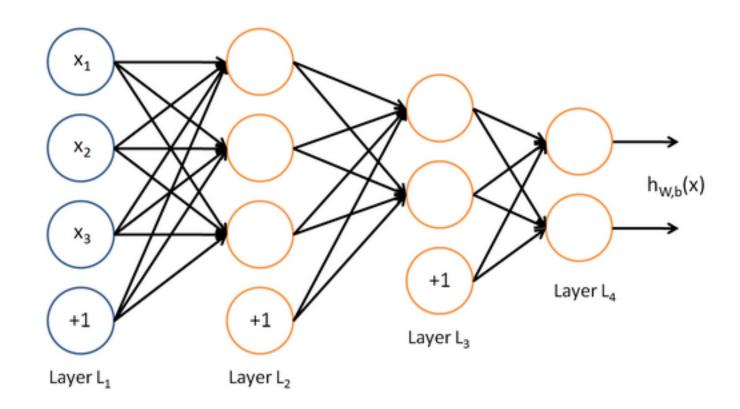
... which we can feed into another logistic regression function



and it is the training criterion that will decide what those intermediate binary target variables should be, so as to make a good job of predicting the targets for the next layer, etc.

## A neural network = running several logistic regressions at the same time

Before we know it, we have a multilayer neural network....



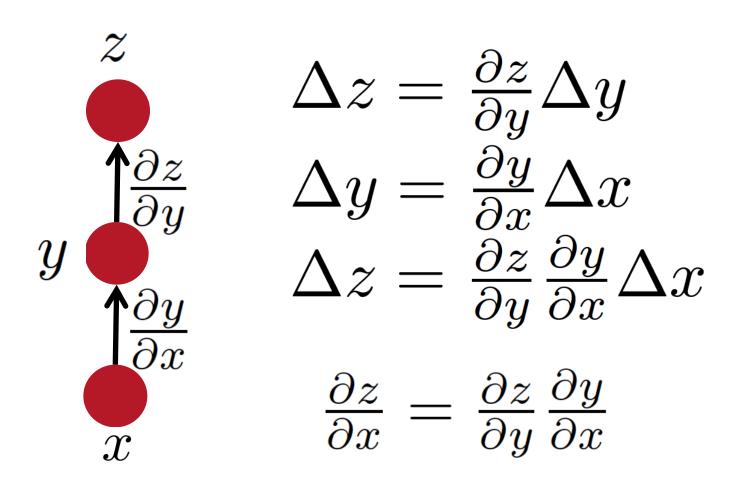
### Back-Prop

- Compute gradient of example-wise loss wrt parameters
- Simply applying the derivative chain rule wisely

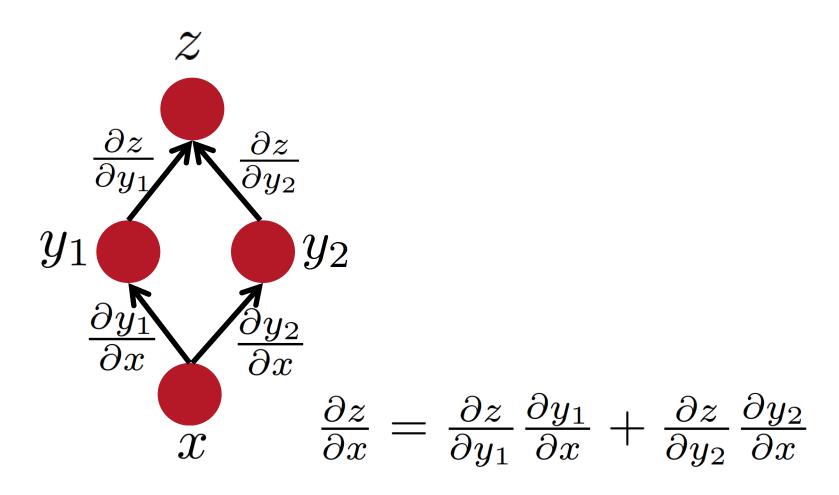
$$z = f(y)$$
  $y = g(x)$   $\frac{\partial z}{\partial x} = \frac{\partial z}{\partial y} \frac{\partial y}{\partial x}$ 

 If computing the loss(example, parameters) is O(n) computation, then so is computing the gradient

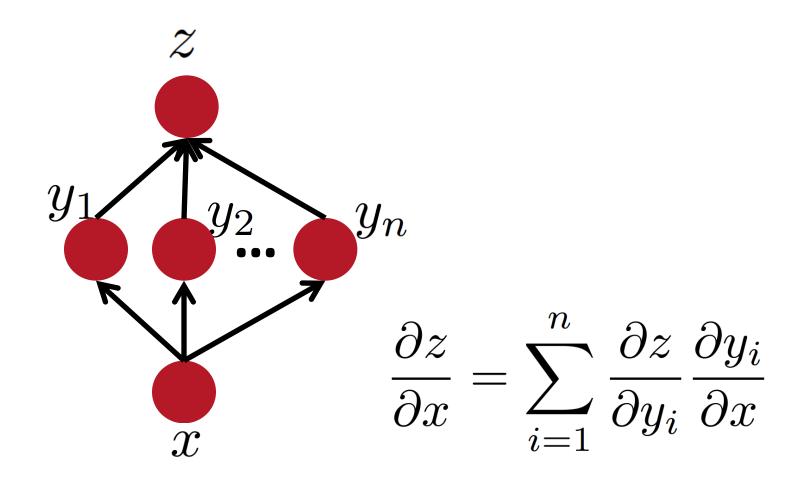
### Simple Chain Rule



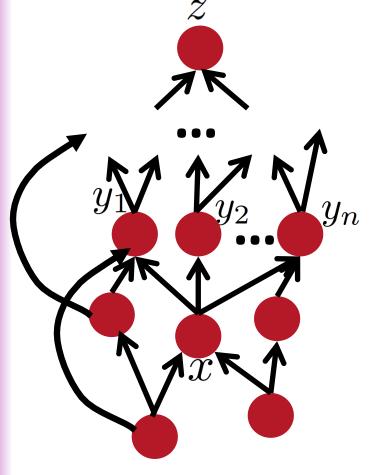
#### Multiple Paths Chain Rule



#### Multiple Paths Chain Rule - General



### Chain Rule in Flow Graph

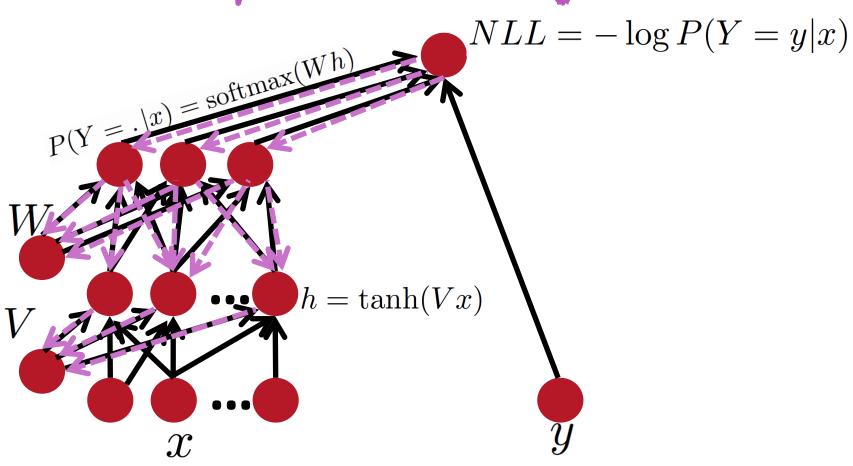


Flow graph: any directed acyclic graph node = computation result arc = computation dependency

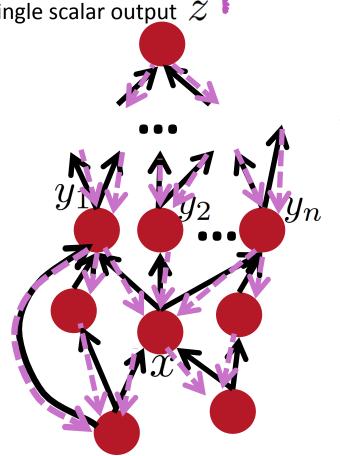
$$\{y_1,\,y_2,\;\ldots\;y_n\}$$
 = successors of  $\,x$ 

$$\frac{\partial z}{\partial x} = \sum_{i=1}^{n} \frac{\partial z}{\partial y_i} \frac{\partial y_i}{\partial x}$$

### Back-Prop in Multi-Layer Net



### Back-Prop in General Flow Graph Single scalar output $\boldsymbol{z}$



- 1. Fprop: visit nodes in topo-sort order
  - Compute value of node given predecessors
- 2. Bprop:
  - initialize output gradient = 1
  - visit nodes in reverse order:

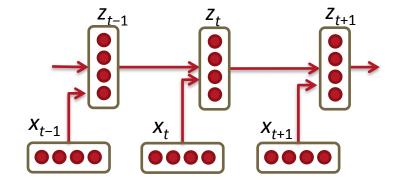
Compute gradient wrt each node using gradient wrt successors

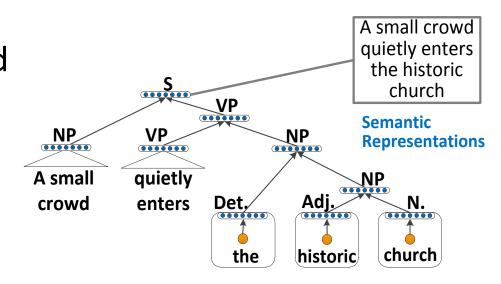
$$\{y_1,\,y_2,\,\ldots\,y_n\}$$
 = successors of  ${\mathcal X}$ 

$$\frac{\partial z}{\partial x} = \sum_{i=1}^{n} \frac{\partial z}{\partial y_i} \frac{\partial y_i}{\partial x}$$

#### Back-Prop in Recurrent & Recursive Nets

- Replicate a
   parameterized function
   over different time
   steps or nodes of a DAG
- Output state at one time-step / node is used as input for another time-step / node

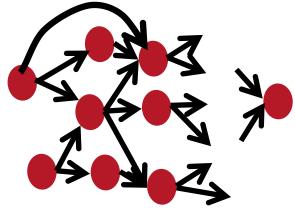


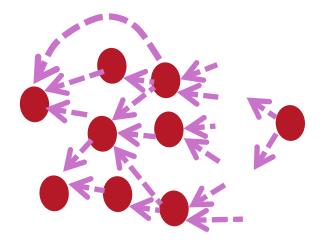


### Backpropagation Through Structure

- Inference → discrete choices
  - (e.g., shortest path in HMM, best output configuration in CRF)
- E.g. Max over configurations or sum weighted by posterior
- The loss to be optimized depends on these choices
- The inference operations are flow graph nodes
- If continuous, can perform stochastic gradient descent
  - Max(a,b) is continuous.

### Automatic Differentiation

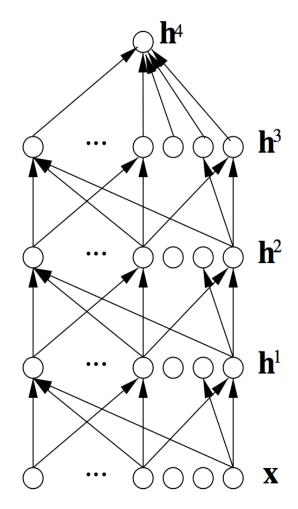




- The gradient computation can be automatically inferred from the symbolic expression of the fprop.
- Each node type needs to know how to compute its output and how to compute the gradient wrt its inputs given the gradient wrt its output.
- Easy and fast prototyping

### Deep Supervised Neural Nets

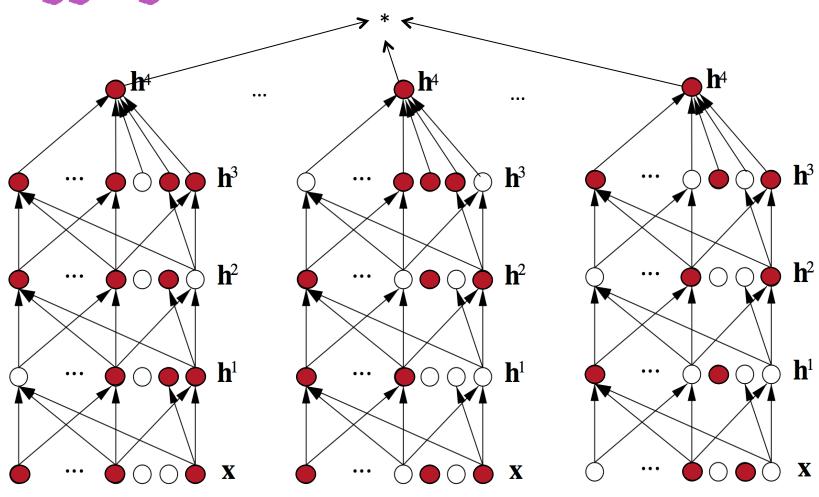
- We can now train them even without unsupervised pretraining, thanks to better initialization and non-linearities (rectifiers, maxout) and they can generalize well with large labeled sets and dropout.
- Unsupervised pre-training still useful for rare classes, transfer, smaller labeled sets, or as an extra regularizer.



#### Stochastic Neurons as Regularizer: Improving neural networks by preventing co-adaptation of feature detectors (Hinton et al 2012, arXiv)

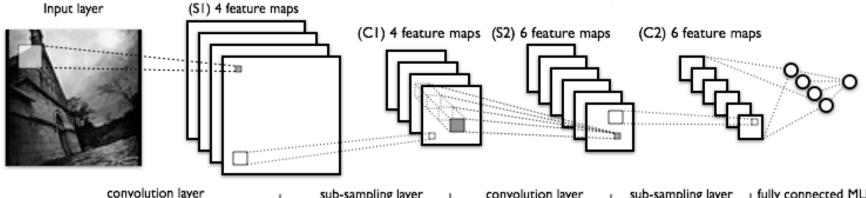
- Dropouts trick: during training multiply neuron output by random bit (p=0.5), during test by 0.5
- Used in deep supervised networks
- Similar to denoising auto-encoder, but corrupting every layer
- Works better with some non-linearities (rectifiers, maxout) (Goodfellow et al. ICML 2013)
- Equivalent to averaging over exponentially many architectures
  - Used by Krizhevsky et al to break through ImageNet SOTA
  - Also improves SOTA on CIFAR-10 (18→16% err)
  - Knowledge-free MNIST with DBMs (.95→.79% err)
  - TIMIT phoneme classification (22.7→19.7% err)

#### Dropout Regularizer: Super-Efficient Bagging



## Temporal & Spatial Inputs: Convolutional & Recurrent Nets

- Local connectivity across time/space
- Sharing weights across time/space (translation equivariance)
- Pooling (translation invariance, cross-channel pooling for learned invariances)

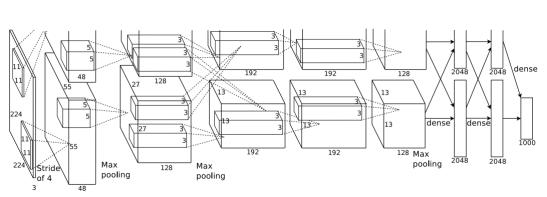


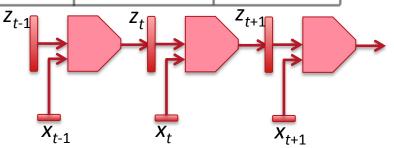
sub-sampling layer

convolution layer

sub-sampling layer

fully connected MLP





Recurrent nets (RNNs) can summarize information from the past

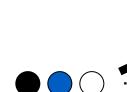
Bidirectional RNNs also summarize information from the future

Distributed Representations & Neural Nets:

How to do unsupervised training?

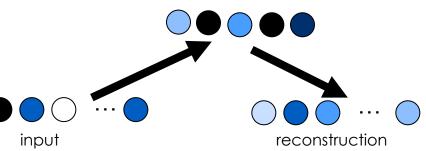
#### PCA

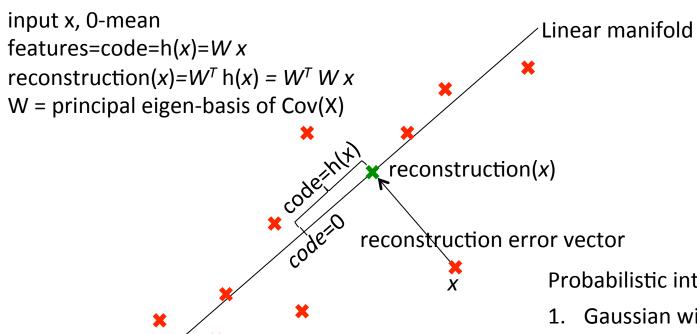
code= latent features h





= Linear Gaussian Factors



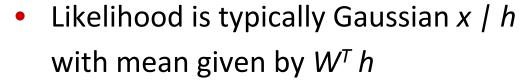


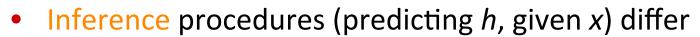
Probabilistic interpretations:

- 1. Gaussian with full covariance  $W^T W + \lambda I$
- 2. Latent marginally iid Gaussian factors h with  $x = W^T h + noise$

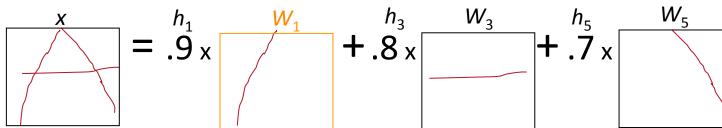
## Directed Factor Models: P(x,h)=P(h)P(x|h) factors prior likelihood

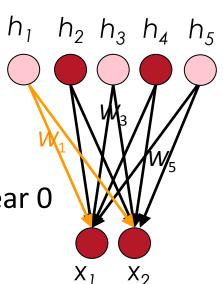
- P(h) factorizes into  $P(h_1)$   $P(h_2)$ ...
- Different priors:
  - PCA:  $P(h_i)$  is Gaussian
  - ICA:  $P(h_i)$  is non-parametric
  - Sparse coding:  $P(h_i)$  is concentrated near 0



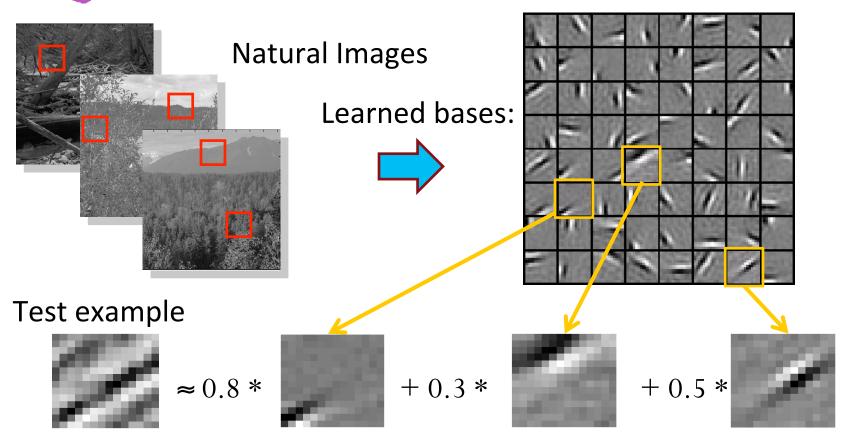








## Sparse autoencoder illustration for images

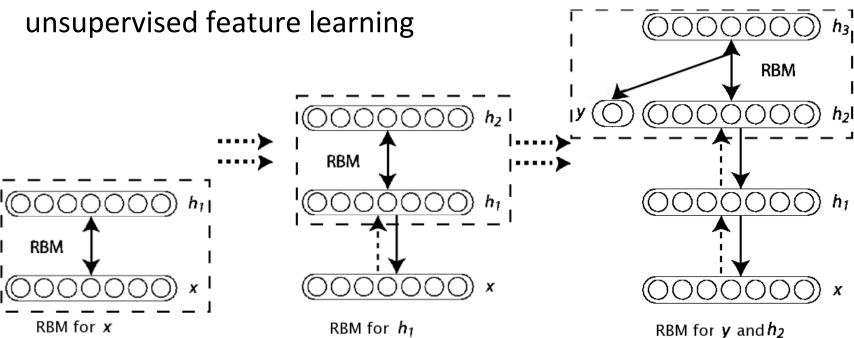


$$[h_1, ..., h_{64}] = [0, 0, ..., 0, 0.8, 0, ..., 0, 0.3, 0, ..., 0, 0.5, 0] (feature representation)$$

#### Stacking Single-Layer Learners

 PCA is great but can't be stacked into deeper more abstract representations (linear x linear = linear)

One of the big ideas from Hinton et al. 2006: layer-wise

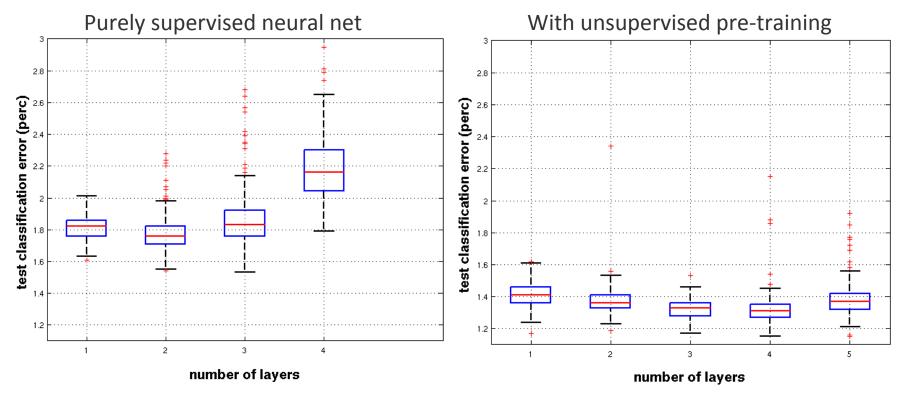


Stacking Restricted Boltzmann Machines (RBM) → Deep Belief Network (DBN)

Effective deep learning first became possible with unsupervised pre-training

[Erhan et al., JMLR 2010]

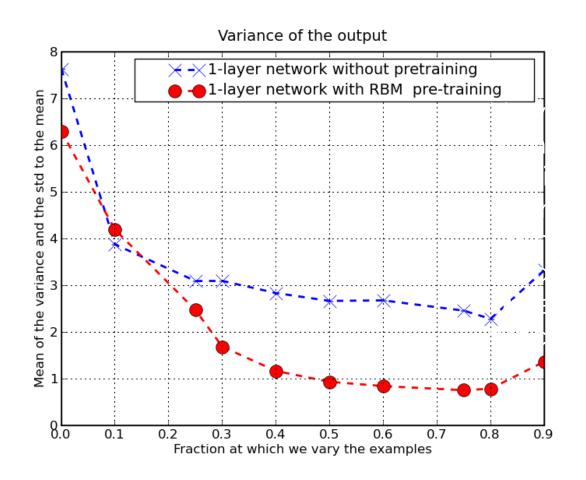
(with RBMs and Denoising Auto-Encoders)



#### Optimizing Deep Non-Linear Composition of Functions Seems Hard

- Failure of training deep supervised nets before 2006
- Regularization effect vs optimization effect of unsupervised pre-training
- Is optimization difficulty due to
  - ill-conditioning?
  - local minima?
  - both?
- The jury is still out, but we now have success stories of training deep supervised nets without unsupervised pre-training

# Initial Examples Matter More (critical period?)



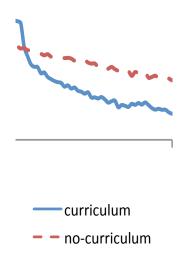
Order & Selection of Examples Matters

(Bengio, Louradour, Collobert & Weston, ICML'2009)



- (Bengio et al 2009, Krueger & Dayan 2009)
- Start with easier examples

Faster convergence to a better local minimum in deep architectures



# Understanding the difficulty of training deep feedforward neural networks

(Glorot & Bengio, AISTATS 2010)

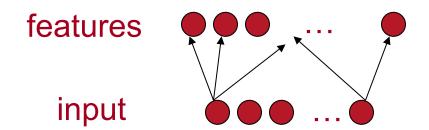


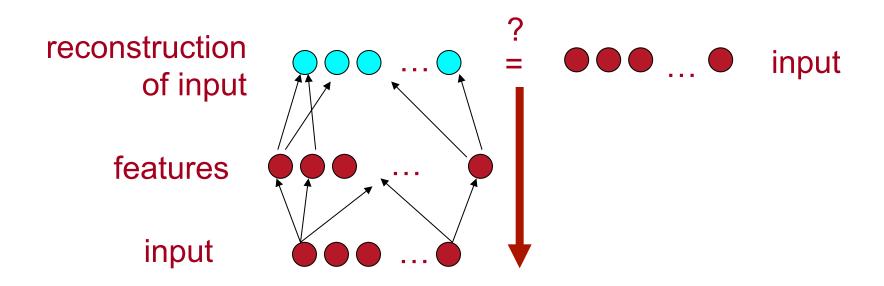
- wrt depth
- as training progresses
- for different initializations → big difference
- for different non-linearities → big difference

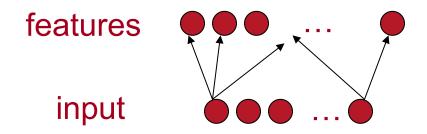
First demonstration that deep supervised nets can be successfully trained almost as well as with unsupervised pretraining, by setting up the optimization problem appropriately...

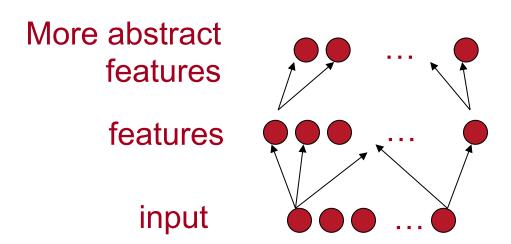
#### Layer-wise Unsupervised Learning

input ••• ...•

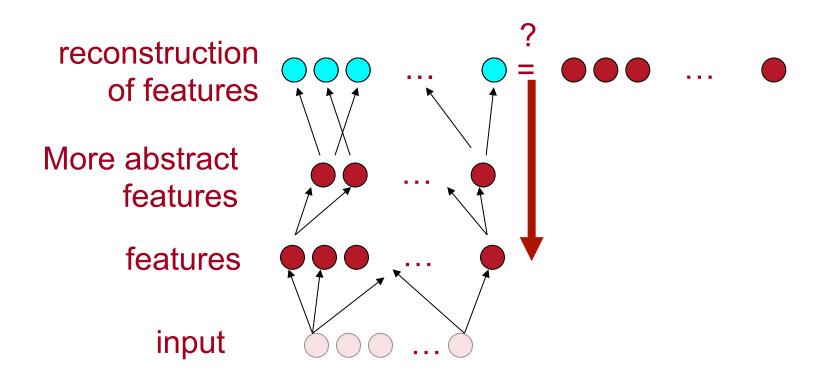


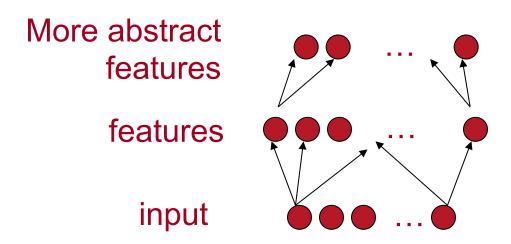




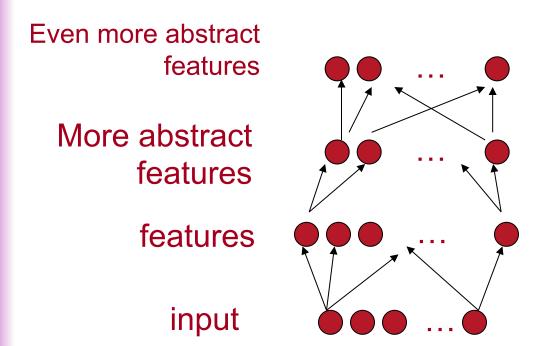


#### Layer-wise Unsupervised Learning

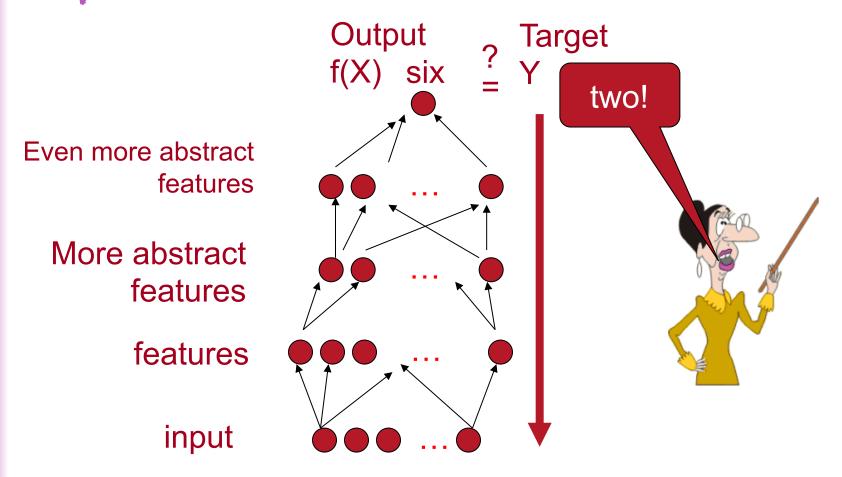




#### Layer-wise Unsupervised Learning



#### Supervised Fine-Tuning



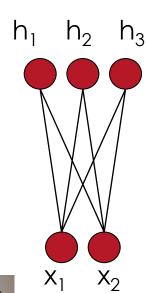
Additional hypothesis: features good for P(x) good for P(y|x)

#### Restricted Boltzmann Machines

#### Undirected Models: the Restricted Boltzmann Machine

[Hinton et al 2006]

- Probabilistic model of the joint distribution of the observed variables (inputs alone or inputs and targets) x
- Latent (hidden) variables h model high-order dependencies
- Inference is easy, P(h|x) factorizes into product of  $P(h_i|x)$
- See Bengio (2009) detailed monograph/review: "Learning Deep Architectures for AI".
- See Hinton (2010)
   "A practical guide to training Restricted Boltzmann Machines"





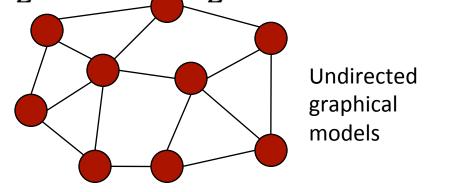
#### Boltzmann Machines & MRFs

Boltzmann machines:

(Hinton 84) 
$$P(x) = \frac{1}{Z}e^{-\text{Energy}(x)} = \frac{1}{Z}e^{c^Tx + x^TWx} = \frac{1}{Z}e^{\sum_i c_i x_i + \sum_{i,j} x_i W_{ij} x_j}$$

Markov Random Fields:

$$P(x) = \frac{1}{Z} e^{\sum_{i} w_{i} f_{i}(x)}$$



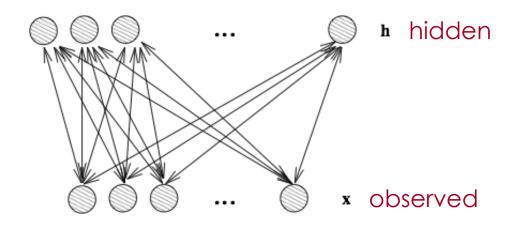
Soft constraint / probabilistic statement

More interesting with latent variables!

## Restricted Boltzmann Machine (RBM)

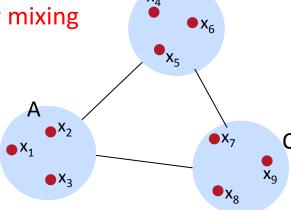
$$P(x,h) = \frac{1}{Z} e^{b^T h + c^T x + h^T W x} = \frac{1}{Z} e^{\sum_i b_i h_i + \sum_j c_j x_j + \sum_{i,j} h_i W_{ij} x_j}$$

- A popular building block for deep architectures
- Bipartite undirected graphical model



#### Gibbs Sampling & Block Gibbs Sampling

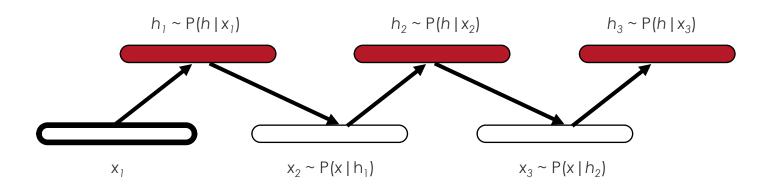
- Want to sample from P(X<sub>1</sub>,X<sub>2</sub>,...X<sub>n</sub>)
- Gibbs sampling
  - Iterate or randomly choose i in {1...n}
  - Sample  $X_i$  from  $P(X_i \mid X_1, X_2, ... X_{i-1}, X_{i+1}, ... X_n)$  can only make small changes at a time!  $\rightarrow$  slow mixing Note how fixed point samples from the joint. Special case of Metropolis-Hastings.



B

- Block Gibbs sampling (not always possible)
  - X's organized in blocks, e.g.  $A=(X_1,X_2,X_3)$ ,  $B=(X_4,X_5,X_6)$ , C=...
  - Do Gibbs on P(A,B,C,...), i.e.
    - Sample A from P(A|B,C)
    - Sample B from P(B|A,C)
    - Sample C from P(C|A,B), and iterate...
  - Larger changes → faster mixing

#### Block Gibbs Sampling in RBMs



P(h|x) and P(x|h) factorize

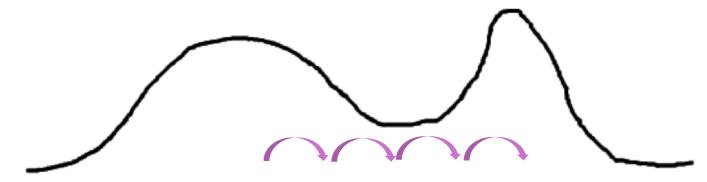
$$P(h|x) = \prod_{i} P(h_i|x)$$

Easy inferenceEfficient block Gibbs sampling  $x \rightarrow h \rightarrow x \rightarrow h...$ 

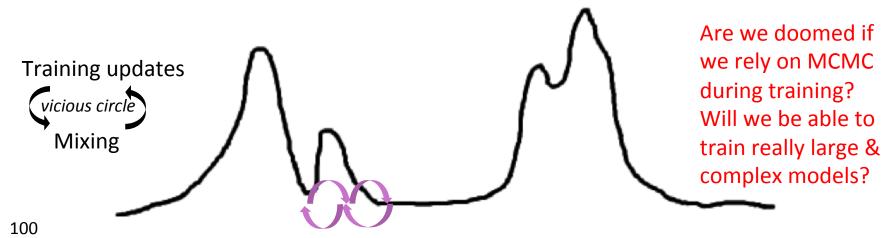
$$P(x,h) = \frac{1}{Z}e^{b^T h + c^T x + h^T W x}$$

#### Obstacle: Vicious Circle Between Learning and MCMC Sampling

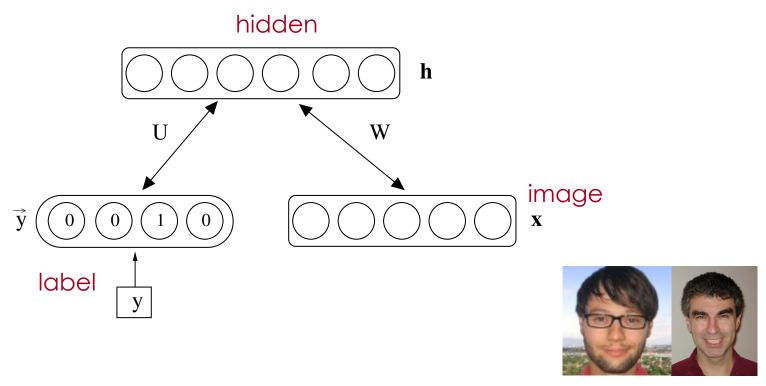
Early during training, density smeared out, mode bumps overlap



Later on, hard to cross empty voids between modes



#### RBM with (image, label) visible units



(Larochelle & Bengio 2008)

#### RBMs are Universal Approximators

(Le Roux & Bengio 2008)

- Adding one hidden unit (with proper choice of parameters) guarantees increasing likelihood
- With enough hidden units, can perfectly model any discrete distribution
- RBMs with variable # of hidden units = non-parametric

#### RBM Conditionals Factorize

$$P(\mathbf{h}|\mathbf{x}) = \frac{\exp(\mathbf{b}'\mathbf{x} + \mathbf{c}'\mathbf{h} + \mathbf{h}'W\mathbf{x})}{\sum_{\tilde{\mathbf{h}}} \exp(\mathbf{b}'\mathbf{x} + \mathbf{c}'\tilde{\mathbf{h}} + \tilde{\mathbf{h}}'W\mathbf{x})}$$

$$= \frac{\prod_{i} \exp(\mathbf{c}_{i}\mathbf{h}_{i} + \mathbf{h}_{i}W_{i}\mathbf{x})}{\prod_{i} \sum_{\tilde{\mathbf{h}}_{i}} \exp(\mathbf{c}_{i}\tilde{\mathbf{h}}_{i} + \tilde{\mathbf{h}}_{i}W_{i}\mathbf{x})}$$

$$= \prod_{i} \frac{\exp(\mathbf{h}_{i}(\mathbf{c}_{i} + W_{i}\mathbf{x}))}{\sum_{\tilde{\mathbf{h}}_{i}} \exp(\tilde{\mathbf{h}}_{i}(\mathbf{c}_{i} + W_{i}\mathbf{x}))}$$

$$= \prod_{i} P(\mathbf{h}_{i}|\mathbf{x}).$$

#### RBM Energy Gives Binomial Neurons

With 
$$\mathbf{h}_i \in \{0, 1\}$$
, recall Energy $(\mathbf{x}, \mathbf{h}) = -\mathbf{b}'\mathbf{x} - \mathbf{c}'\mathbf{h} - \mathbf{h}'W\mathbf{x}$ 

$$P(\mathbf{h}_{i} = 1|\mathbf{x}) = \frac{e^{1\mathbf{c}_{i}+1W_{i}\mathbf{x}+other\ terms}}{e^{1\mathbf{c}_{i}+1W_{i}\mathbf{x}+other\ terms} + e^{0\mathbf{c}_{i}+0W_{i}\mathbf{x}+other\ terms}}$$

$$= \frac{e^{\mathbf{c}_{i}+W_{i}\mathbf{x}}}{e^{\mathbf{c}_{i}+W_{i}\mathbf{x}}+1}$$

$$= \frac{1}{1+e^{-\mathbf{c}_{i}-W_{i}\mathbf{x}}}$$

$$= \operatorname{sigm}(\mathbf{c}_{i}+W_{i}\mathbf{x}).$$

since  $sigm(a) = \frac{1}{1+e^{-a}}$ .

## RBM Free Energy $P(\mathbf{x}, \mathbf{h}) = \frac{e^{-\mathrm{Energy}(\mathbf{x}, \mathbf{h})}}{Z}$

$$P(\mathbf{x}, \mathbf{h}) = \frac{e^{-\text{Energy}(\mathbf{x}, \mathbf{h})}}{Z}$$

Free Energy = equivalent energy when marginalizing

$$P(\mathbf{x}) = \sum_{\mathbf{h}} \frac{e^{-\text{Energy}(\mathbf{x}, \mathbf{h})}}{Z} = \frac{e^{-\text{FreeEnergy}(\mathbf{x})}}{Z}$$

Can be computed exactly and efficiently in RBMs

FreeEnergy(
$$\mathbf{x}$$
) =  $-\mathbf{b}'\mathbf{x} - \sum_{i} \log \sum_{\mathbf{h}_{i}} e^{\mathbf{h}_{i}(\mathbf{c}_{i} + W_{i}\mathbf{x})}$ 

Marginal likelihood P(x) tractable up to partition function Z

#### Energy-Based Models Gradient

$$P(\mathbf{x}) = \frac{e^{-\text{Energy}(\mathbf{x})}}{Z} \qquad Z = \sum_{\mathbf{x}} e^{-\text{Energy}(\mathbf{x})}$$
$$\frac{\partial \log P(\mathbf{x})}{\partial \theta} = -\frac{\partial \text{Energy}(\mathbf{x})}{\partial \theta} - \frac{\partial \log Z}{\partial \theta}$$

$$\frac{\partial \log Z}{\partial \theta} = \frac{\partial \log \sum_{\mathbf{x}} e^{-\text{Energy}(\mathbf{x})}}{\partial \theta}$$

$$= \frac{1}{Z} \frac{\partial \sum_{\mathbf{x}} e^{-\text{Energy}(\mathbf{x})}}{\partial \theta}$$

$$= -\frac{1}{Z} \sum_{\mathbf{x}} e^{-\text{Energy}(\mathbf{x})} \frac{\partial \text{Energy}(\mathbf{x})}{\partial \theta}$$

$$= -\sum_{\mathbf{x}} P(\mathbf{x}) \frac{\partial \text{Energy}(\mathbf{x})}{\partial \theta}$$

#### Boltzmann Machine Gradient

$$P(x) = \frac{1}{Z} \sum_{h} e^{-\text{Energy}(x,h)} = \frac{1}{Z} e^{-\text{FreeEnergy}(x)}$$

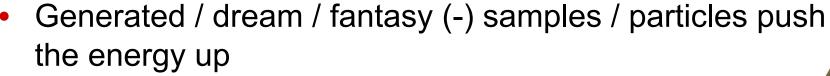
Gradient has two components:

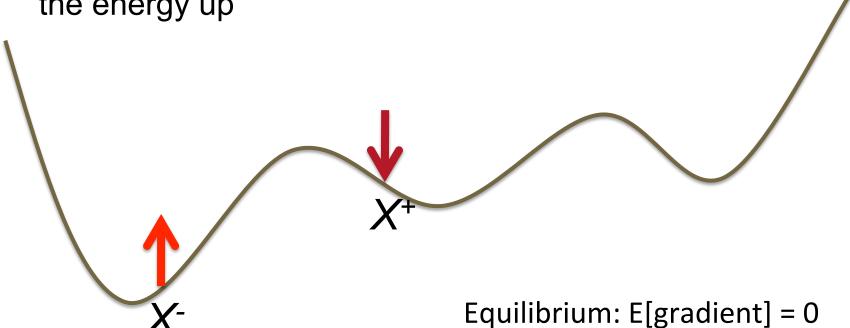
$$\frac{\partial \log P(x)}{\partial \theta} = \underbrace{ -\frac{\partial \operatorname{FreeEnergy}(x)}{\partial \theta}} + \underbrace{ \sum_{\tilde{x}} P(\tilde{x}) \frac{\partial \operatorname{FreeEnergy}(\tilde{x})}{\partial \theta}} \\ = \underbrace{ -\sum_{h} P(h|x) \frac{\partial \operatorname{Energy}(x,h)}{\partial \theta}} + \underbrace{ \sum_{\tilde{x},\tilde{h}} P(\tilde{x},\tilde{h}) \frac{\partial \operatorname{Energy}(\tilde{x},\tilde{h})}{\partial \theta}}$$

- In RBMs, easy to sample or sum over  $h \mid x$
- Difficult part: sampling from P(x), typically with a Markov chain

#### Positive & Negative Samples

Observed (+) examples push the energy down





## Training RBMs

Contrastive Divergence: start negative Gibbs chain at observed x, run k (CD-k) Gibbs steps

SML/Persistent CD: run negative Gibbs chain in background while (PCD) weights slowly change

Fast PCD: two sets of weights, one with a large learning rate only used for negative phase, quickly exploring modes

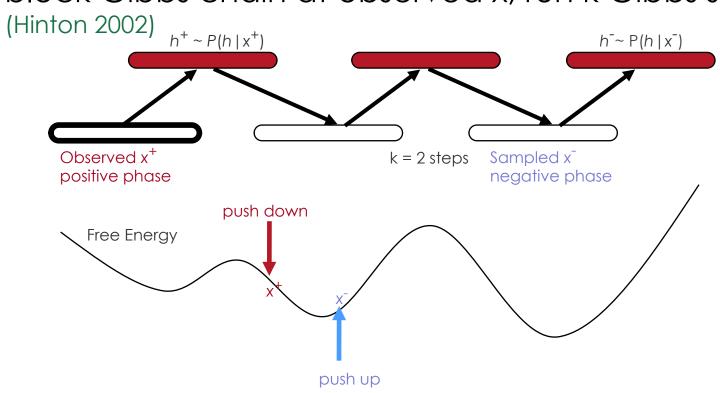
Herding: Deterministic near-chaos dynamical system defines both learning and sampling

Tempered MCMC: use higher temperature to escape modes

## Contrastive Divergence



Contrastive Divergence (CD-k): start negative phase block Gibbs chain at observed x, run k Gibbs steps



## Persistent CD (PCD) / Stochastic Max. Likelihood (SML)

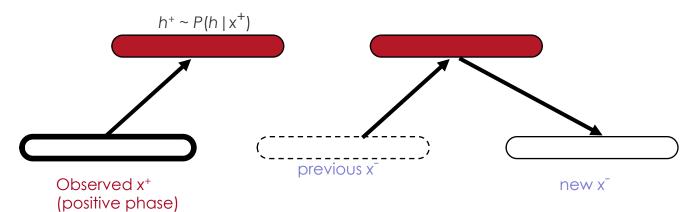
Run negative Gibbs chain in background while weights slov change (Younes 1999, Tieleman 2008):



- Guarantees (Younes 1999; Yuille 2005)
- If learning rate decreases in 1/t,
   chain mixes before parameters change too much,
   chain stays converged when parameters change





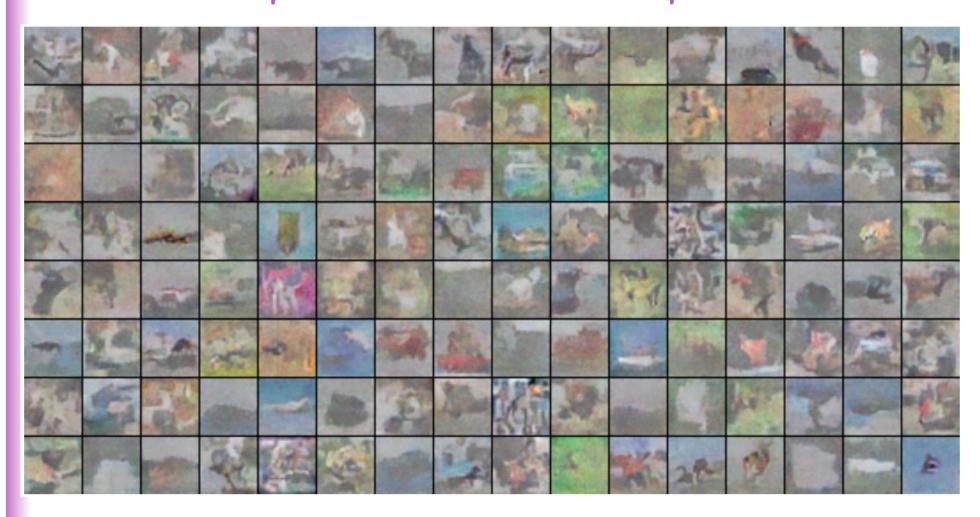


## Some RBM Variants

- Different energy functions and allowed values for the hidden and visible units:
  - Hinton et al 2006: binary-binary RBMs
  - Welling NIPS'2004: exponential family units
  - Ranzato & Hinton CVPR'2010: Gaussian RBM weaknesses (no conditional covariance), propose mcRBM
  - Ranzato et al NIPS'2010: mPoT, similar energy function
  - Courville et al ICML'2011: spike-and-slab RBM



## Convolutionally Trained Spike & Slab RBMs Samples



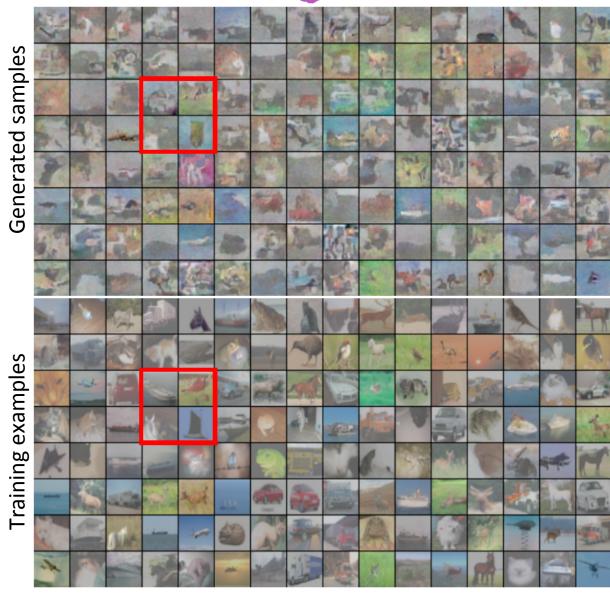
## ssRBM is not Cheating

Samples from  $\mu$ -ssRBM:



Nearest examples in CIFAR: (least square dist.)





Time for a break

## Auto-Encoders & Variants: Learning a computational graph

# Computational Graphs

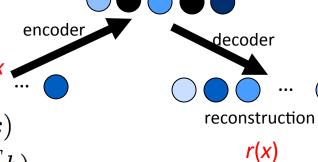
h<sup>4</sup>
... h<sup>3</sup>
... h<sup>2</sup>
... x

- Operations for particular task
- Neural nets' structure = computational graph for P(y|x)
- Graphical model's structure ≠ computational graph for inference
- Recurrent nets & graphical models
  - → family of computational graphs sharing parameters

 Could we have a parametrized family of computational graphs defining "the model"?

## Simple Auto-Encoders

- MLP whose target output = input
- Reconstruction=decoder(encoder(input)),
   e.g.



code= latent features h

$$h = \tanh(b + Wx)$$
  
 $\operatorname{reconstruction} = \tanh(c + W^T h)$   
 $\operatorname{Loss} L(x, \operatorname{reconstruction}) = ||\operatorname{reconstruction} - x||^2$ 

- With bottleneck, code = new coordinate system
- Encoder and decoder can have 1 or more layers
- Training deep auto-encoders notoriously difficult

### Link Between Contrastive Divergence and Auto-Encoder Reconstruction Error Gradient

#### (Bengio & Delalleau 2009):



- CD-2k estimates the log-likelihood gradient from 2k diminishing terms of an expansion that mimics the Gibbs steps
- reconstruction error gradient looks only at the first step, i.e., is a kind of mean-field approximation of CD-0.5

$$\frac{\partial \log P(x_1)}{\partial \theta} = \sum_{s=1}^{t-1} \left( E\left[ \frac{\partial \log P(x_s|h_s)}{\partial \theta} \middle| x_1 \right] + E\left[ \frac{\partial \log P(h_s|x_{s+1})}{\partial \theta} \middle| x_1 \right] \right) + E\left[ \frac{\partial \log P(x_t)}{\partial \theta} \middle| x_1 \right]$$

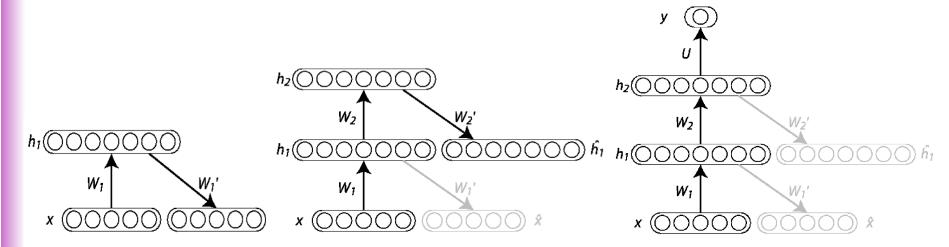
# I finally understand what auto-encoders do!

• Try to carve holes in  $||r(x)-x||^2$  or  $-\log P(x \mid h(x))$  at examples



- Vector r(x)-x points in direction of increasing prob., i.e. estimate score = d log p(x) / dx: learn score vector field = local mean
- Generalize (*valleys*) in between above holes to form *manifolds* 
  - dr(x)/dx estimates the **local covariance** and is linked to the Hessian  $d^2 \log p(x)/dx^2$
- A Markov Chain associated with AEs estimates the datagenerating distribution (Bengio et al, arxiv 1305.663, 2013)

## Stacking Auto-Encoders



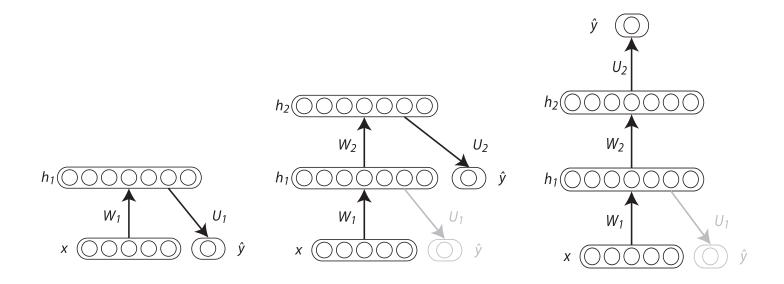
Auto-encoders can be stacked successfully (Bengio et al NIPS'2006) to form highly non-linear representations, which with fine-tuning overperformed purely supervised MLPs







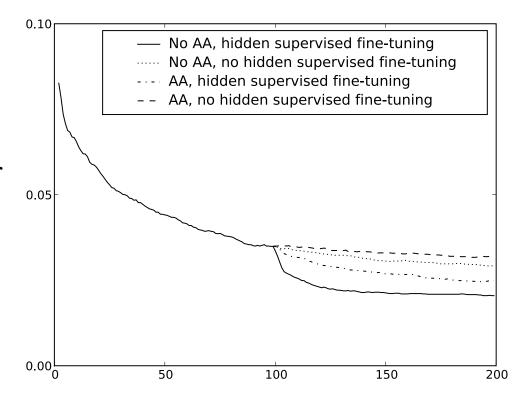
## Greedy Layerwise Supervised Training



Generally worse than unsupervised pre-training but better than ordinary training of a deep neural network (Bengio et al. NIPS'2006). Has been used successfully on large labeled datasets, where unsupervised pre-training did not make as much of an impact.

## Supervised Fine-Tuning is Important

- Greedy layer-wise unsupervised pretraining phase with RBMs or auto-encoders on MNIST
- Supervised phase with or without unsupervised updates, with or without fine-tuning of hidden layers
- Can train all RBMs at the same time, same results

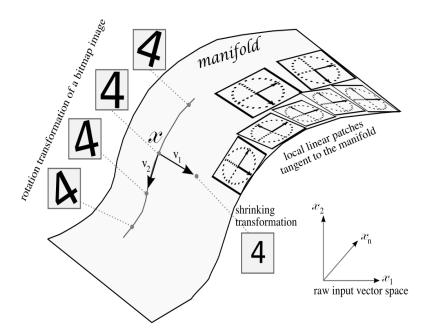


## (Auto-Encoder) Reconstruction Loss

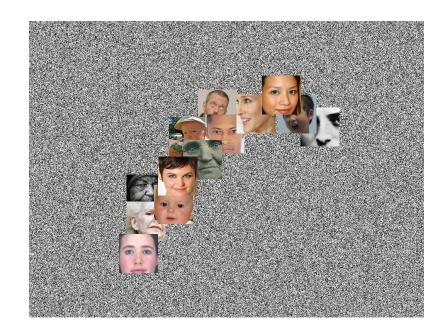
- Discrete inputs: cross-entropy for binary inputs
  - -  $\Sigma_i x_i \log r_i(x) + (1-x_i) \log(1-r_i(x))$  (with  $0 < r_i(x) < 1$ ) or log-likelihood reconstruction criterion, e.g., for a multinomial (one-hot) input
  - -  $\Sigma_i x_i \log r_i(x)$  (where  $\Sigma_i r_i(x) = 1$ , summing over subset of inputs associated with this multinomial variable)
- In general: consider what are appropriate loss functions to predict each of the input variables,
  - typically, reconstruction neg. log-likelihood –log P(x | h(x))

## Manifold Learning

 Additional prior: examples Concentrate near a lower dimensional "manifold" (region of high density with only few operations allowed which allow small changes while staying on the manifold)



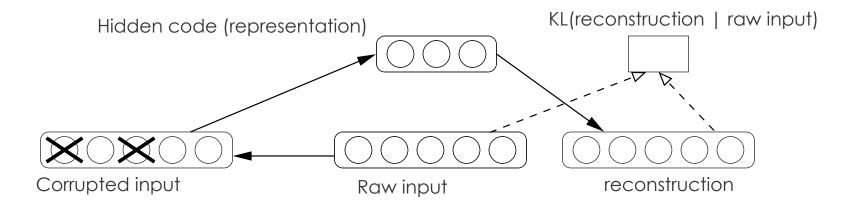
- variable dimension locally?
- Soft # of dimensions?



# Denoising Auto-Encoder (Vincent et al 2008)



- Corrupt the input during training only
- Train to reconstruct the uncorrupted input



- Encoder & decoder: any parametrization
- As good or better than RBMs for unsupervised pre-training

## Denoising Auto-Encoder

Learns a vector field pointing towards
 higher probability direction (Alain & Bengio 2013)

 $r(x)-x \propto dlogp(x)/dx$ 

 Some DAEs correspond to a kind of Gaussian RBM with regularized Score Matching (Vincent 2011)

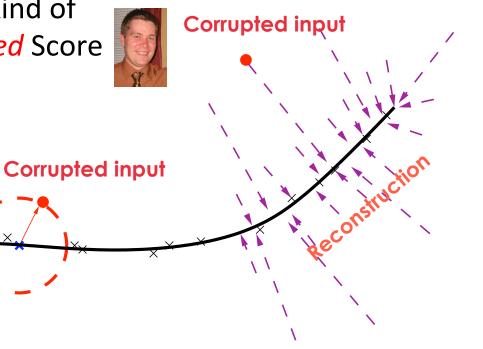
[equivalent when noise  $\rightarrow$  0]

Compared to RBM:
 No partition function issue,

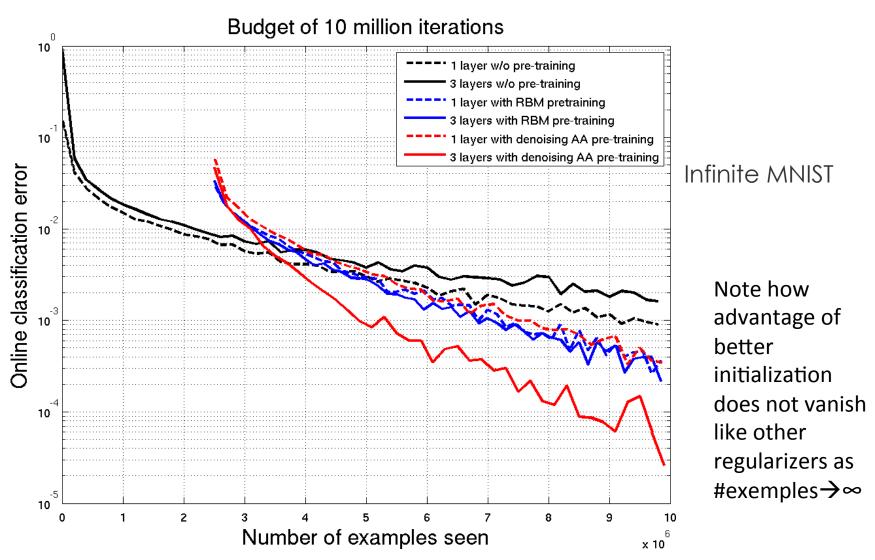
+ can measure training

criterion

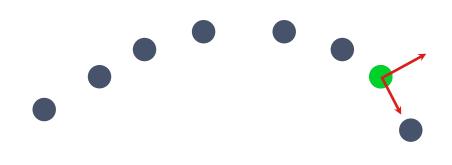
prior: examples concentrate near a lower dimensional "manifold"



## Stacked Denoising Auto-Encoders



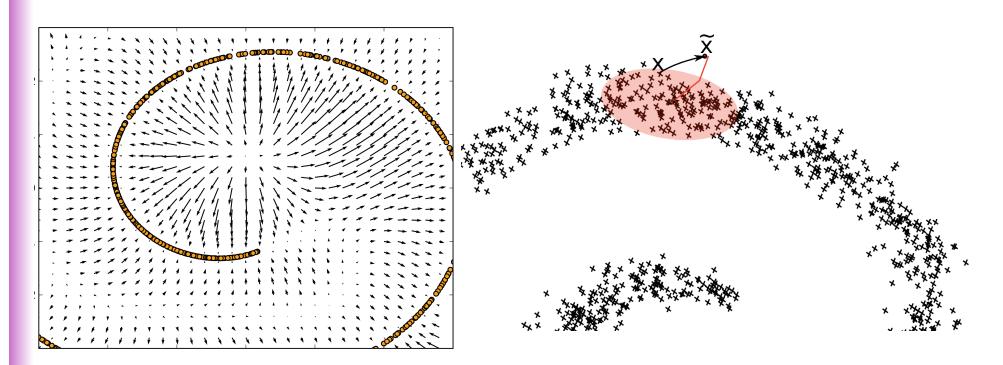
### Auto-Encoders Learn Salient Variations, like a non-linear PCA



- Minimizing reconstruction error forces to keep variations along manifold.
- Regularizer wants to throw away all variations.
- With both: keep ONLY sensitivity to variations ON the manifold.

### Regularized Auto-Encoders Learn a Vector Field or a Markov Chain Transition Distribution

- (Bengio, Vincent & Courville, TPAMI 2013) review paper
- (Alain & Bengio ICLR 2013; Bengio et al, arxiv 2013)



## Contractive Auto-Encoders



(Rifai, Vincent, Muller, Glorot, Bengio ICML 2011; Rifai, Mesnil, Vincent, Bengio, Dauphin, Glorot ECML 2011; Rifai, Dauphin, Vincent, Bengio, Muller NIPS 2011)

$$\operatorname{reconstruction}(x) = g(h(x)) = \operatorname{decoder}(\operatorname{encoder}(x))$$

Training criterion:

$$\mathcal{J}_{CAE}(\theta) = \sum_{x \in D_n} \lambda \sum_{ij} \left( \frac{\partial h_j(x)}{\partial x_i} \right)^2 + L(x, \text{reconstruction}(x))$$

wants contraction in all directions

cannot afford contraction in manifold directions

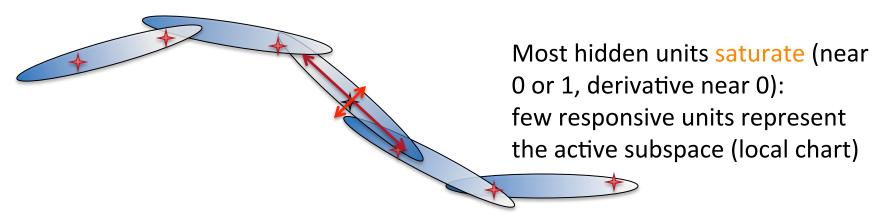
If 
$$h_i = sigmoid(b_i + W_i x)$$

$$(dh_j(x)/dx_i)^2 = h_j^2(1-h_j)^2W_{ji}^2$$

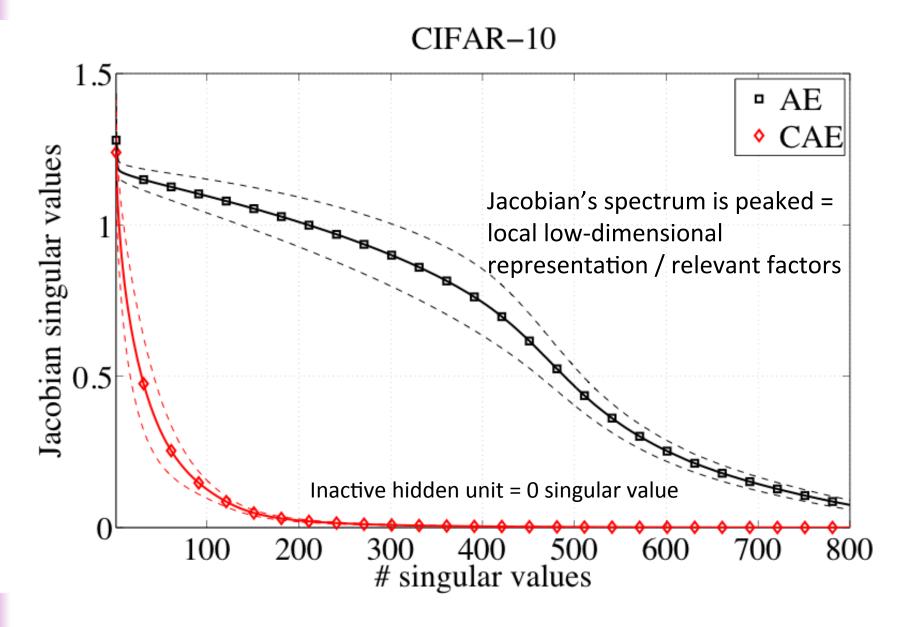
## Contractive Auto-Encoders



(Rifai, Vincent, Muller, Glorot, Bengio ICML 2011; Rifai, Mesnil, Vincent, Bengio, Dauphin, Glorot ECML 2011; Rifai, Dauphin, Vincent, Bengio, Muller NIPS 2011)



Each region/chart = subset of active hidden units
Neighboring region: one of the units becomes active/inactive
SHARED SET OF FILTERS ACROSS REGIONS, EACH USING A SUBSET



## Contractive Auto-Encoders

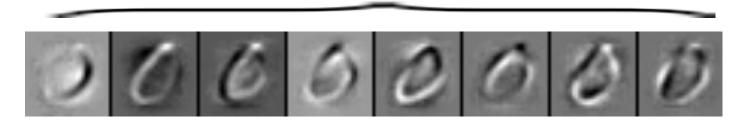
Benchmark of medium-size datasets on which several deep learning algorithms had been evaluated (Larochelle et al ICML 2007)

Data Set	$\mathrm{SVM}_{rbf}$	SAE-3	RBM-3	DAE-b-3	CAE-1	CAE-2
basic	3.03±0.15	$3.46_{\pm 0.16}$	3.11±0.15	$2.84_{\pm 0.15}$	2.83±0.15	2.48 <sub>±0.14</sub>
rot	11.11±0.28	$10.30_{\pm 0.27}$	$10.30_{\pm 0.27}$	$9.53_{\pm 0.26}$	$11.59_{\pm 0.28}$	9.66 <sub>±0.26</sub>
bg-rand	$14.58_{\pm 0.31}$	$11.28_{\pm 0.28}$	6.73 <sub>±0.22</sub>	$10.30_{\pm 0.27}$	$13.57_{\pm 0.30}$	$10.90{\scriptstyle~\pm 0.27}$
bg-img	22.61±0.379	23.00 <sub>±0.37</sub>	16.31±0.32	16.68±0.33	16.70 <sub>±0.33</sub>	15.50±0.32
bg-img-rot	55.18±0.44	51.93±0.44	$47.39_{\pm0.44}$	43.76 <sub>±0.43</sub>	$48.10_{\pm 0.44}$	45.23±0.44
rect	2.15±0.13	2.41±0.13	2.60 <sub>±0.14</sub>	$1.99_{\pm 0.12}$	1.48±0.10	1.21±0.10
rect-img	24.04±0.37	$24.05{\scriptstyle\pm0.37}$	22.50 <sub>±0.37</sub>	21.59 <sub>±0.36</sub>	21.86±0.36	21.54±0.36

#### **Input Point**

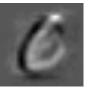
#### **Tangents**







 $O + 0.5 \times O = O$ 





**MNIST** 

# Input Point Tangents Tangents

MNIST Tangents

# Distributed vs Local (CIFAR-10 unsupervised)

Input Point Tangents





Local PCA (no sharing across regions)





Contractive Auto-Encoder

# Denoising auto-encoders are also contractive!

Taylor-expand Gaussian corruption noise in reconstruction error:

$$E\left[\ell(x, r(x+\epsilon))\right] \approx E\left[\left(x - \left(r(x) + \frac{\partial r(x)}{\partial x}\epsilon\right)\right)^{T} \left(x - \left(r(x) + \frac{\partial r(x)}{\partial x}\epsilon\right)\right)\right]$$

$$= E\left[\|x - r(x)\|^{2}\right] + \sigma^{2}E\left[\left\|\frac{\partial r(x)}{\partial x}\right\|_{F}^{2}\right]$$

 Yields a contractive penalty in the reconstruction function (instead of encoder) proportional to amount of corruption noise

## Learned Tangent Prop: the Manifold Tangent Classifier

(Rifai et al NIPS 2011)

3 hypotheses:

- 1. Semi-supervised hypothesis (P(x) related to P(y|x))
- 2. Unsupervised manifold hypothesis (data concentrates near low-dim. manifolds)
- 3. Manifold hypothesis for classification (low density between class manifolds)

## Learned Tangent Prop: the Manifold Tangent Classifier

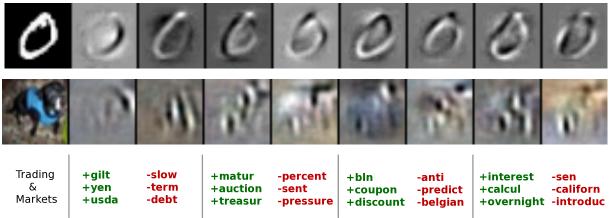
#### Algorithm:

- Estimate local principal directions of variation U(x) by CAE (principal singular vectors of dh(x)/dx)
- 2. Penalize f(x)=P(y|x) predictor by || df/dx U(x) ||

Makes f(x) insensitive to variations on manifold at x, tangent plane characterized by U(x).

## Manifold Tangent Classifier Results

Leading singular vectors on MNIST, CIFAR-10, RCV1:



Knowledge-free MNIST: 0.81% error

K-NN	NN	SVM	DBN	CAE	DBM	CNN	MTC
3.09%	1.60%	1.40%	1.17%	1.04%	0.95%	0.95%	0.81%

Semi-sup.

	NN	SVM	CNN	<b>TSVM</b>	DBN-rNCA	EmbedNN	CAE	MTC
100	25.81	23.44	22.98	16.81	-	16.86	13.47	12.03
600	11.44	8.85	7.68	6.16	8.7	5.97	6.3	5.13
1000	10.7	7.77	6.45	5.38	-	5.73	4.77	3.64
3000	6.04	4.21	3.35	3.45	3.3	3.59	3.22	2.57

• Forest (500k examples)

SVM	Distributed SVM	MTC
4.11%	3.46%	3.13%

## Inference and Explaining Away

- Easy inference in RBMs and regularized Auto-Encoders
- But no explaining away (competition between causes)
- (Coates et al 2011): even when training filters as RBMs it helps to perform additional explaining away (e.g. plug them into a Sparse Coding inference), to obtain better-classifying features



- RBMs would need lateral connections to achieve similar effect
- Auto-Encoders would need to have lateral recurrent connections or deep recurrent structure

# Sparse Coding (Olshausen et al 97)



Directed graphical model:

$$P(h) \propto e^{-\lambda |h|_1} \quad x|h \sim N(W^T h, \sigma^2 I)$$

 One of the first unsupervised feature learning algorithms with non-linear feature extraction (but linear decoder)

$$\min_{h} \frac{||x - W^T h||^2}{\sigma^2} + \lambda |h|_1$$

MAP inference recovers sparse h although P(h|x) not concentrated at 0

- Linear decoder, non-parametric encoder
- Sparse Coding inference: convex but expensive optimization

## Predictive Sparse Decomposition

 Approximate the inference of sparse coding by a parametric encoder:

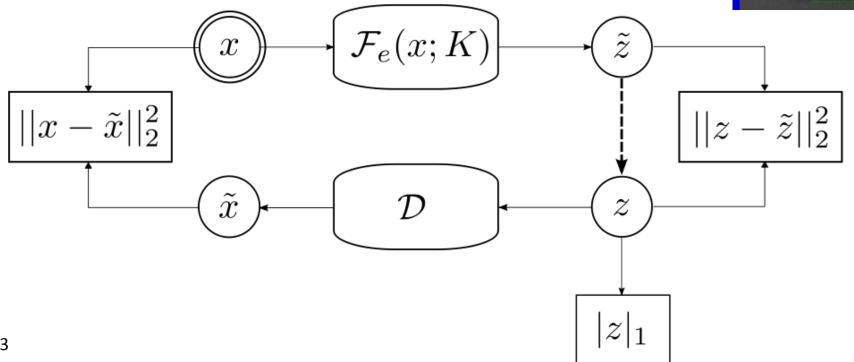


**Predictive Sparse Decomposition** 

(Kavukcuoglu et al 2008)

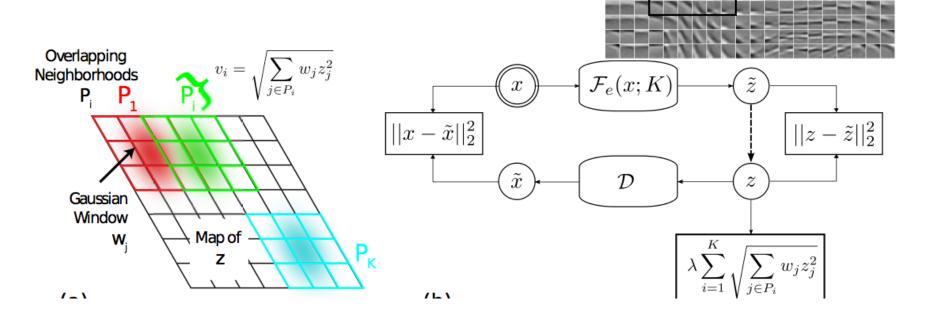
Very successful applications in machine vision with convolutional architectures





## Predictive Sparse Decomposition

- Stacked to form deep architectures
- Alternating convolution, rectification, pooling
- Tiling: no sharing across overlapping filters
- Group sparsity penalty yields topographic maps



### Deep Variants

### Level-Local Learning is Important

- Initializing each layer of an unsupervised deep Boltzmann machine helps a lot
- Initializing each layer of a supervised neural network as an RBM, auto-encoder, denoising auto-encoder, etc can help a lot
- Helps most the layers further away from the target
- Not just an effect of the unsupervised prior
- Jointly training all the levels of a deep architecture is difficult because of the increased non-linearity / non-smoothness
- Initializing using a level-local learning algorithm is a useful trick
- Providing intermediate-level targets can help tremendously (Gulcehre & Bengio ICLR 2013)

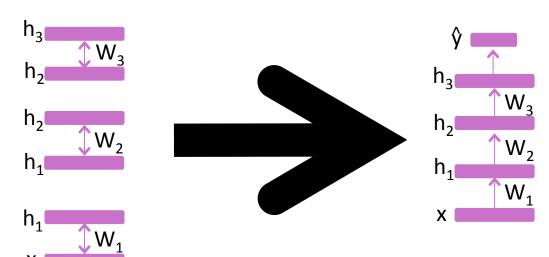
# Stack of RBMs / AES -> Deep MLP

• Encoder or P(h|v) becomes MLP layer









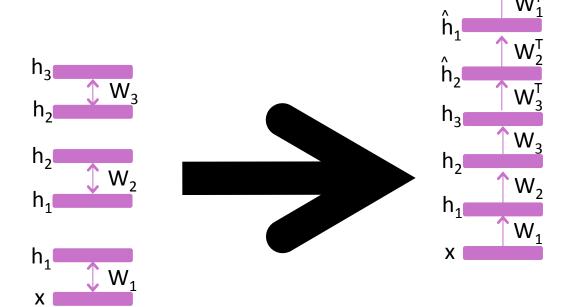
## Stack of RBMs / AEs -> Deep Auto-Encoder



χ̂

(Hinton & Salakhutdinov 2006)

- Stack encoders / P(h|x) into deep encoder
- Stack decoders / P(x|h) into deep decoder



### Stack of RBMs / AEs > Deep Recurrent Auto-Encoder

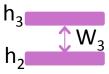
(Savard 2011) 3



(Bengio & Laufer, arxiv 2013)

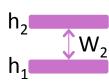


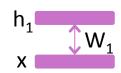


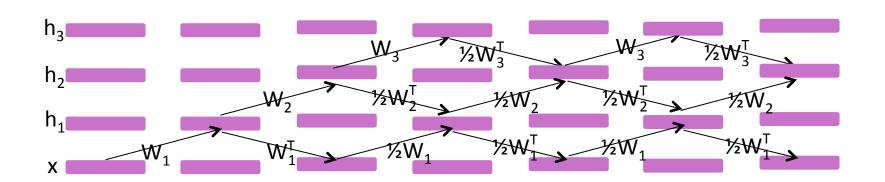


- Each hidden layer receives input from below and above
- Deterministic (mean-field) recurrent computation (Savard 2011)
- Stochastic (injecting noise) recurrent computation: Deep Generative Stochastic Networks (GSNs)

(Bengio & Laufer arxiv 2013)



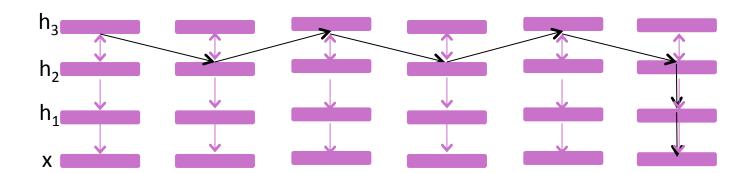




# 



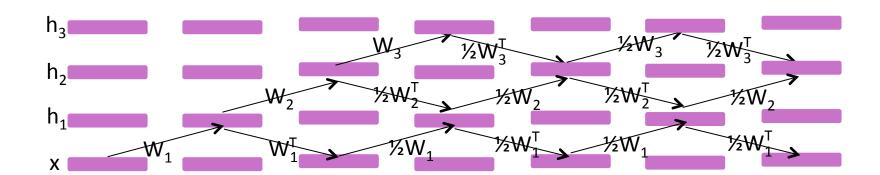
- Stack lower levels RBMs' P(x|h) along with top-level RBM
- $P(x, h_1, h_2, h_3) = P(h_2, h_3) P(h_1|h_2) P(x | h_1)$
- Sample: Gibbs on top RBM, propagate down



## Stack of RBMs Teep Boltzmann Machine

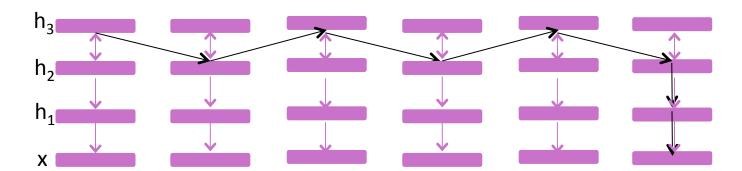
(Salakhutdinov & Hinton AISTATS 2009)

- Halve the RBM weights because each layer now has inputs from below and from above
- Positive phase: (mean-field) variational inference = recurrent AE
- Negative phase: Gibbs sampling (stochastic units)
- train by SML/PCD



# Stack of Auto-Encoders Deep Generative Auto-Encoder (Rifai et al ICML 2012)

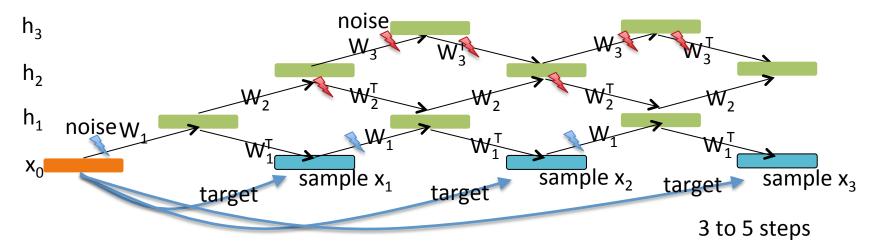
- MCMC on top-level auto-encoder
  - $h_{t+1}$  = encode(decode( $h_t$ ))+ $\sigma$  noise where noise is Normal(0, d/dh encode(decode( $h_t$ )))
- Then deterministically propagate down with decoders



#### Generative Stochastic Networks (GSN)

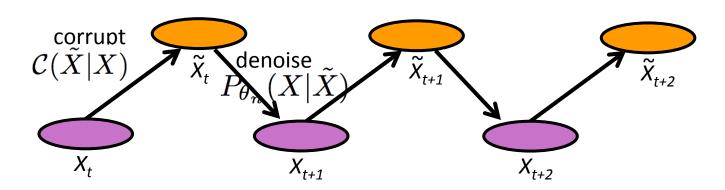
(Bengio, Yao, Alain & Vincent, arxiv 2013; Bengio & Laufer, arxiv 2013)

- Recurrent parametrized stochastic computational graph that defines a transition operator for a Markov chain whose asymptotic distribution is implicitly estimated by the model
- Noise injected in input and hidden layers
- Trained to max. reconstruction prob. of example at each step
- Example structure inspired from the DBM Gibbs chain:



### Denoising Auto-Encoder Markov Chain

- $\mathcal{P}(X)$ : true data-generating distribution
- ullet  $\mathcal{C}(X|X)$  : corruption process
- $P_{\theta_n}(X|\tilde{X})$ : denoising auto-encoder trained with n examples  $X, \tilde{X}$  from  $\mathcal{C}(\tilde{X}|X)\mathcal{P}(X)$ , probabilistically "inverts" corruption
- ullet  $T_n$ : Markov chain over X alternating  $ilde{X} \sim \mathcal{C}( ilde{X}|X)$  ,  $\ X \sim P_{ heta_n}(X| ilde{X})$



#### Previous Theoretical Results on Probabilistic Interpretation of Auto-Encoders (Vincent 2011, Alain & Bengio 2013)

- Continuous X
- Gaussian corruption
- Noise  $\sigma \rightarrow 0$
- Squared reconstruction error  $||r(X+\text{noise})-X||^2$

 $(r(X)-X)/\sigma^2$  estimates the score d log p(X) / dX

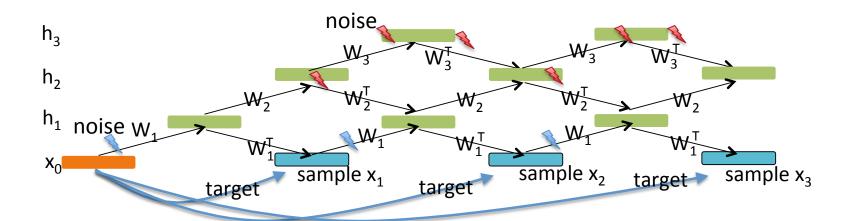
#### New Theoretical Results

 Denoising AE are consistent estimators of the data-generating distribution through their Markov chain, so long as they consistently estimate the conditional denoising distribution and the Markov chain converges.

Making 
$$P_{\theta_n}(X|\tilde{X})$$
 match  $\mathcal{P}(X|\tilde{X})$  makes  $\pi_n(X)$  match  $\mathcal{P}(X)$  denoising distr. truth

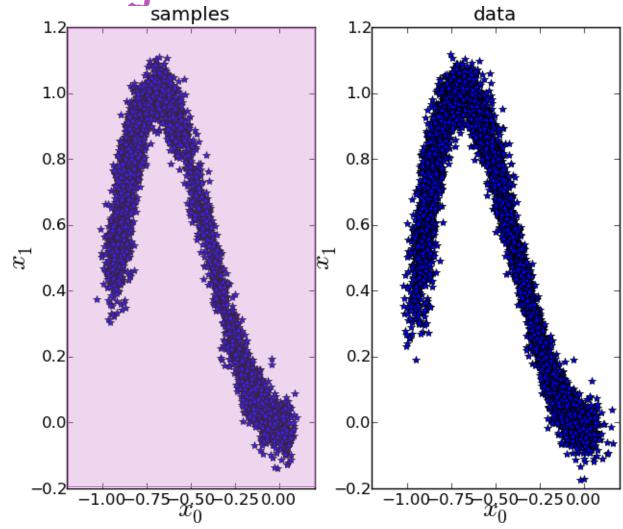
#### Generative Stochastic Networks (GSN)

• If we decompose the reconstruction probability into a parametrized noise-dependent part  $\tilde{X} = f_{\theta_1}(X,Z)$  and a noise-independent part  $P_{\theta_2}(X|\tilde{X})$ , we also get a consistent estimator of the data generating distribution, if the chain converges.

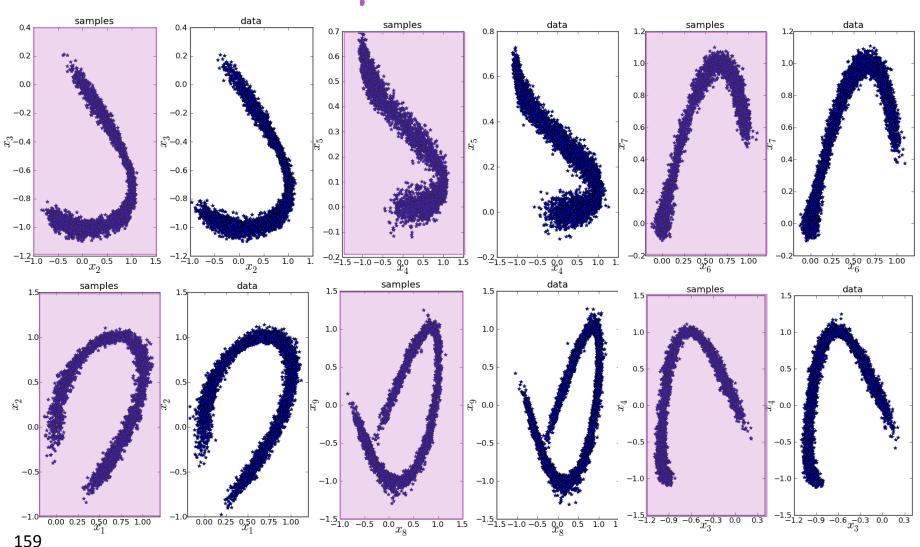


# GSN Experiments: validating the theorem in a continuous non-parametric setting

- Continuous data,
   X in R<sup>10</sup>, Gaussian corruption
- Reconstruction
   distribution =
   Parzen (mixture of
   Gaussians)
   estimator
- 5000 training examples, 5000 samples
- Visualize a pair of dimensions

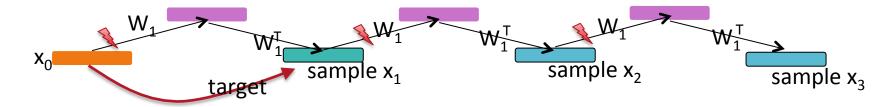


### GSN Experiments: validating the theorem in a continuous non-parametric setting



### Shallow Model: Generalizing the Denoising Auto-Encoder Probabilistic Interpretation

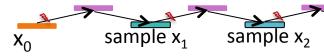
- Classical denoising auto-encoder architecture, single hidden layer with noise only injected in input
- Factored Bernouilli reconstruction prob. distr.
- $\tilde{X} = f_{\theta_1}(X, Z)$  = parameter-less, salt-and-pepper noise on top of X



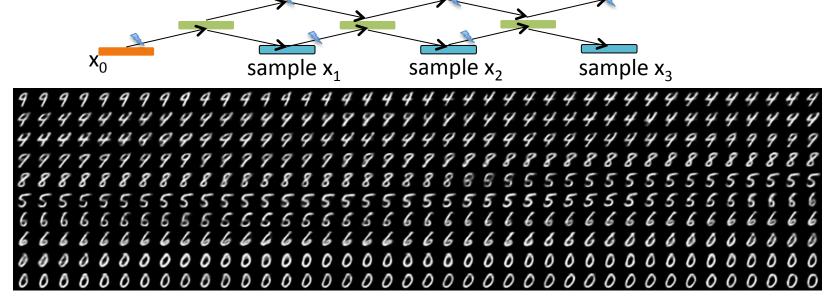
• Generalizes (Alain & Bengio ICLR 2013): not just continuous r.v., any training criterion (as log-likelihood), not just Gaussian but any corruption (no need to be tiny to correctly estimate distribution).

### Experiments: Shallow vs Deep

 Shallow (DAE), no recurrent path at higher levels, state=X only



Deep GSN:



### Quantitative Evaluation of Samples

- Previous procedure for evaluating samples (Breuleux et al 2011, Rifai et al 2012, Bengio et al 2013):
  - Generate 10000 samples from model
  - Use them as training examples for Parzen density estimator
  - Evaluate its log-likelihood on MNIST test data

**Training** 

examples

	GSN-2	DAE	RBM	DBM-3	DBN-2	MNIST
Log-likelihood	214	-152	-244	32	138	24
STANDARD ERROR	1.1	2.2	54	1.9	2.0	1.6

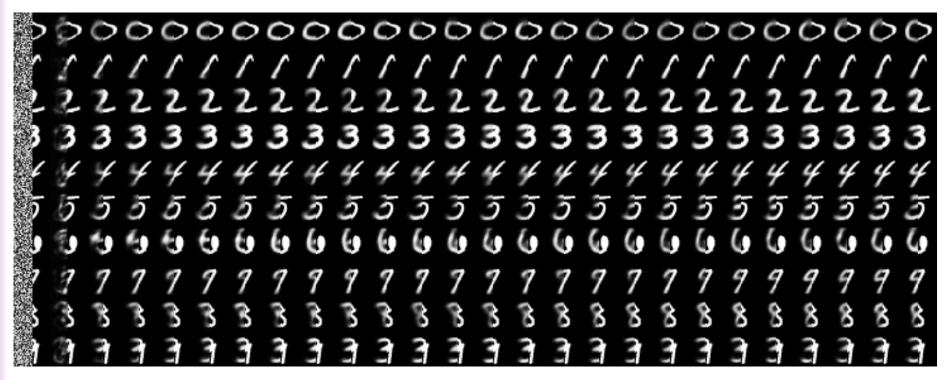
### Question Answering, Missing Inputs and Structured Output

 Once trained, a GSN can provably sample from any conditional over subsets of its inputs, so long as we use the conditional associated with the reconstruction distribution and clamp the right-hand side variables.

(Bengio & Laufer arXiv 2013)

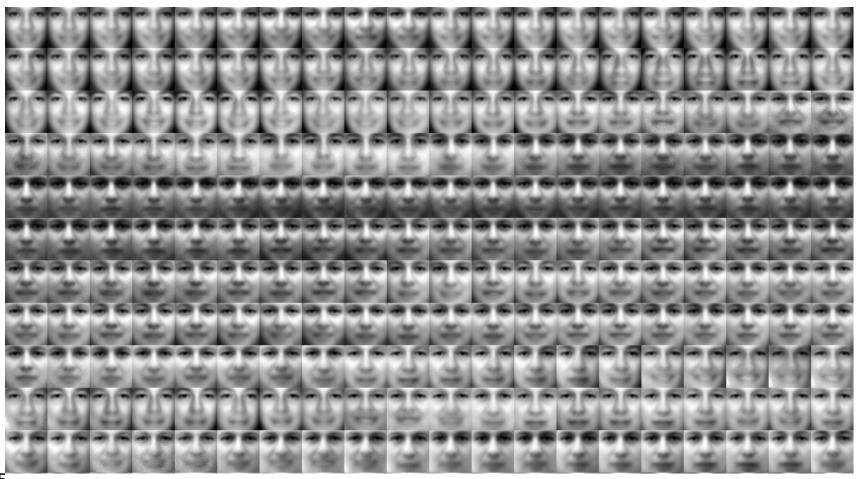
### Experiments: Structured Conditionals

 Stochastically fill-in missing inputs, sampling from the chain that generates the conditional distribution of the missing inputs given the observed ones (notice the fast burn-in!)



### Not Just MNIST: experiments on TFD

• 3 hidden layer model, consecutive samples:



Part 3

### Practical Considerations

### Deep Learning Tricks of the Trade

- Y. Bengio (2013), "Practical Recommendations for Gradient-Based Training of Deep Architectures"
  - Unsupervised pre-training
  - Stochastic gradient descent and setting learning rates
  - Main hyper-parameters
    - Learning rate schedule
    - Early stopping
    - Minibatches
    - Parameter initialization
    - Number of hidden units
    - L1 and L2 weight decay
    - Sparsity regularization
  - Debugging
  - How to efficiently search for hyper-parameter configurations

### Stochastic Gradient Descent (SGD)

 Gradient descent uses total gradient over all examples per update, SGD updates after only 1 or few examples:

$$\theta^{(t)} \leftarrow \theta^{(t-1)} - \epsilon_t \frac{\partial L(z_t, \theta)}{\partial \theta}$$

- L = loss function,  $z_t$  = current example,  $\theta$  = parameter vector, and  $\varepsilon_t$  = learning rate.
- Ordinary gradient descent is a batch method, very slow, should never be used. 2<sup>nd</sup> order batch method are being explored as an alternative but SGD with selected learning schedule remains the method to beat.

### Learning Rates

- Simplest recipe: keep it fixed and use the same for all parameters.
- Collobert scales them by the inverse of square root of the fan-in of each neuron
- Better results can generally be obtained by allowing learning rates to decrease, typically in O(1/t) because of theoretical convergence guarantees, e.g.,

$$\epsilon_t = \frac{\epsilon_0 \tau}{\max(t, \tau)}$$

with hyper-parameters  $\varepsilon_0$  and  $\tau$ .

 New papers on adaptive learning rates procedures (Schaul 2012, 2013), Adagrad (Duchi et al 2011), ADADELTA (Zeiler 2012)

### Early Stopping

- Beautiful FREE LUNCH (no need to launch many different training runs for each value of hyper-parameter for #iterations)
- Monitor validation error during training (after visiting # of training examples = a multiple of validation set size)
- Keep track of parameters with best validation error and report them at the end
- If error does not improve enough (with some patience), stop.





• In very deep networks such as **recurrent networks** (or possibly recursive ones), the gradient is a product of Jacobian matrices, each associated with a step in the forward computation. This can become very small or very large quickly [Bengio et al 1994], and the locality assumption of gradient descent breaks down.

$$L = L(s_T(s_{T-1}(\dots s_{t+1}(s_t, \dots))))$$

$$\frac{\partial L}{\partial s_t} = \frac{\partial L}{\partial s_T} \frac{\partial s_T}{\partial s_{T-1}} \dots \frac{\partial s_{t+1}}{\partial s_t}$$

- Two kinds of problems:
  - sing. values of Jacobians > 1 → gradients explode
  - or sing. values < 1 → gradients shrink & vanish</li>

### The Optimization Challenge in Deep / Recurrent Nets

- Higher-level abstractions require highly non-linear transformations to be learned
- Sharp non-linearities are difficult to learn by gradient

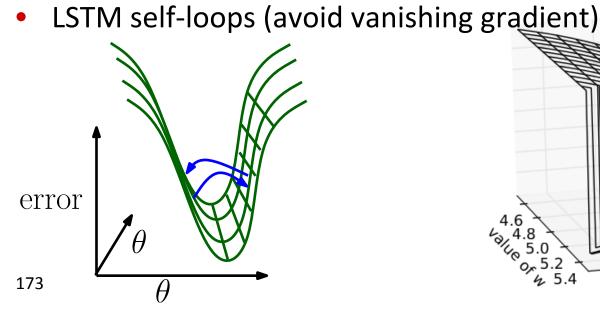
Composition of many non-linearities = sharp non-linearity

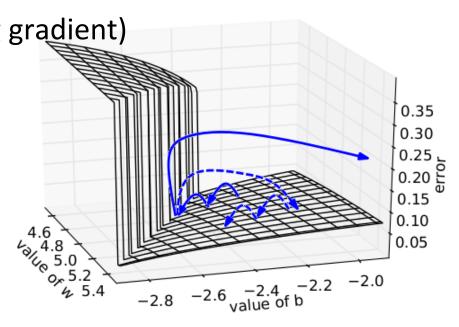
**Exploding or vanishing gradients**  $\mathcal{E}_{t+1}$  $\mathbf{X}_{t-1}$  $\mathbf{X}_{t}$  $\mathbf{X}_{t+1}$  $\partial \mathbf{x}_t$  $\partial \mathbf{x}_{t+1}$  $\partial \mathbf{x}_{t-1}$  $\overline{\partial \mathbf{x}_{t-1}}$  $\partial \mathbf{x}_t$ 172  $u_{t-1}$  $u_t$  $u_{t+1}$ 

#### RNN Tricks

(Pascanu, Mikolov, Bengio, ICML 2013; Bengio, Boulanger & Pascanu, ICASSP 2013)

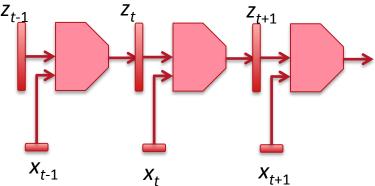
- Clipping gradients (avoid exploding gradients)
- Leaky integration (propagate long-term dependencies)
- Momentum (cheap 2<sup>nd</sup> order)
- Initialization (start in right ballpark avoids exploding/vanishing)
- Sparse Gradients (symmetry breaking)
- Gradient propagation regularizer (avoid vanishing gradient)





Long-Term Dependencies and Clipping Trick





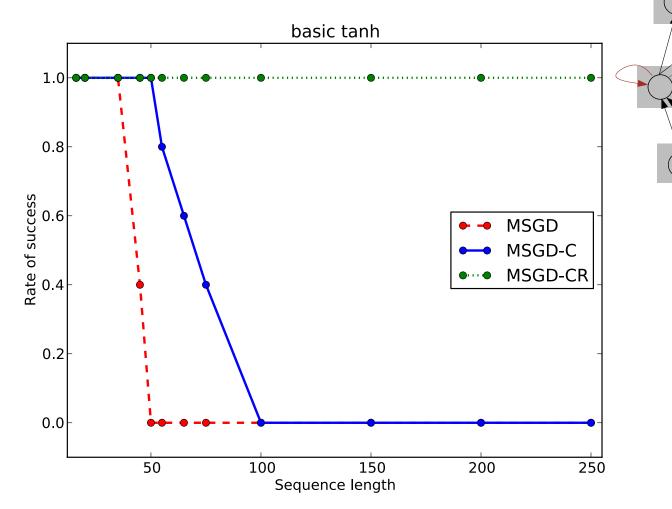
Trick first introduced by Mikolov is to clip gradients to a maximum NORM value.

Makes a big difference in Recurrent Nets (Pascanu et al ICML 2013) Allows SGD to compete with HF optimization on difficult long-term dependencies tasks. Helped to beat SOTA in text compression, language modeling, speech recognition.

# Combining clipping to avoid gradient explosion and Jacobian regularizer to avoid gradient vanishing

(Pascanu, Mikolov & Bengio, ICML 2013)

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### Normalized Initialization to Achieve Unity-Like Jacobian

Assuming f'(act=0)=1

To keep information flowing in both direction we would like to have the following properties.

• Forward-propagation:

$$\forall (i, i'), Var[z^i] = Var[z^{i'}] \Leftrightarrow \forall i, n_i Var[W^i] = 1$$

• Back-propagation:

$$\forall (i, i'), Var\left[\frac{\partial Cost}{\partial s^i}\right] = Var\left[\frac{\partial Cost}{\partial s^{i'}}\right] \Leftrightarrow \forall i, n_{i+1}Var[W^i] = 1$$

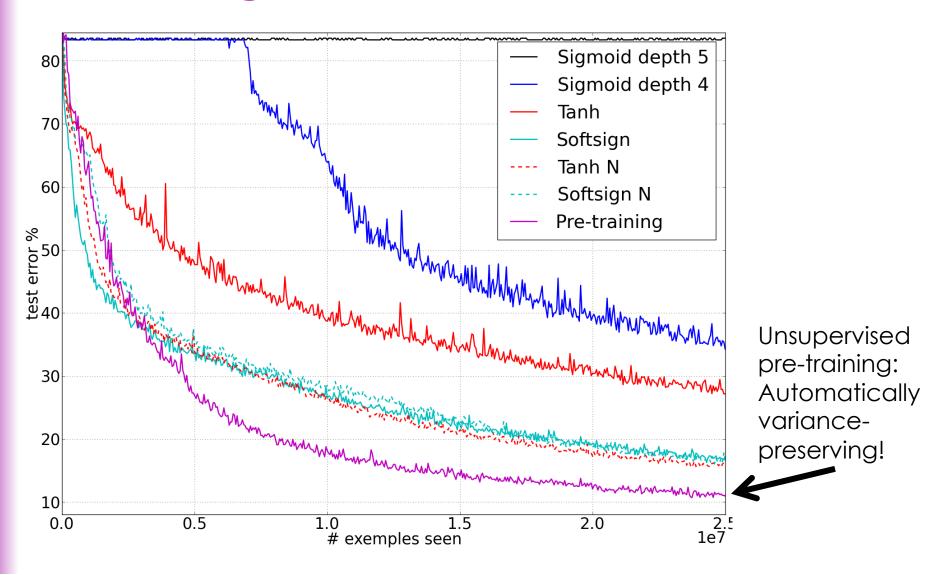
Possible compromise:

$$\forall i, Var[W^i] = \frac{2}{n_i + n_{i+1}} \tag{4}$$

This gives rise to proposed normalized initialization procedure:

$$W^{i} \sim U \left[ -\frac{\sqrt{6}}{\sqrt{n_{i} + n_{i+1}}}, \frac{\sqrt{6}}{\sqrt{n_{i} + n_{i+1}}} \right]$$
 (5)

### Normalized Initialization with Variance-Preserving Jacobians



#### Parameter Initialization

- Initialize hidden layer biases to 0 and output (or reconstruction) biases to optimal value if weights were 0 (e.g. mean target or inverse sigmoid of mean target).
- Initialize weights ~ Uniform(-r,r), r inversely proportional to fanin (previous layer size) and fan-out (next layer size):

$$\sqrt{6/(\text{fan-in} + \text{fan-out})}$$

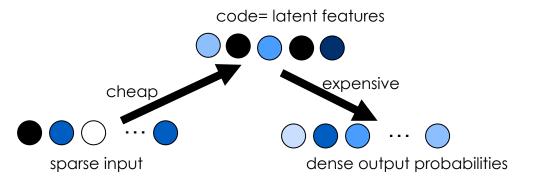
for tanh units (and 4x bigger for sigmoid units)

(Glorot & Bengio AISTATS 2010)



### Handling Large Output Spaces

 Auto-encoders and RBMs reconstruct the input, which is sparse and highdimensional; Language models have a huge output space (1 unit per word).





 (Dauphin et al, ICML 2011) Reconstruct the non-zeros in the input, and reconstruct as many randomly chosen zeros, + importance weights

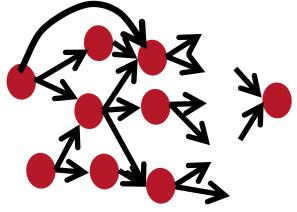
(Collobert & Weston, ICML 2008) sample a ranking loss

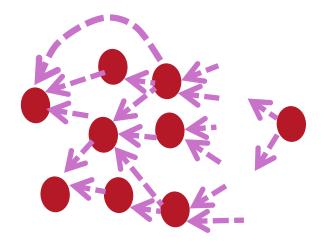
• Decompose output probabilities hierarchically (Morin & Bengio 2005; Blitzer et al 2005; Mnih & Hinton 2007,2009; Mikolov et al 2011)



categories

### Automatic Differentiation





- Makes it easier to quickly and safely try new models.
- Theano Library (python) does it symbolically. Other neural network packages (Torch, Lush) can compute gradients for any given run-time value.

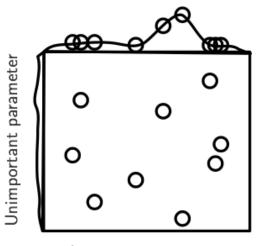
(Bergstra et al SciPy'2010)



### Random Sampling of Hyperparameters (Bergstra & Bengio 2012)

- Common approach: manual + grid search
- Grid search over hyperparameters: simple & wasteful
- Random search: simple & efficient
  - Independently sample each HP, e.g. I.rate~exp(U[log(.1),log(.0001)])
  - Each training trial is iid
  - If a HP is irrelevant grid search is wasteful
  - More convenient: ok to early-stop, continue further, etc.

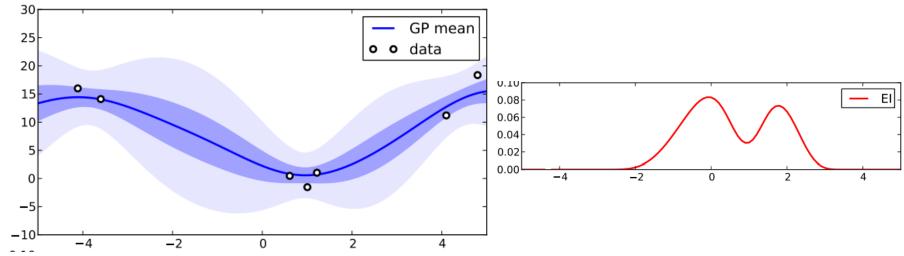
Grid Layout Unimportant parameter Important parameter Random Layout



Important parameter

# Sequential Model-Based Optimization of Hyper-Parameters

- (Hutter et al JAIR 2009; Bergstra et al NIPS 2011; Thornton et al arXiv 2012; Snoek et al NIPS 2012)
- Iterate
- Estimate P(valid. err | hyper-params config x, D)
- choose optimistic x, e.g.  $\max_{x} P(valid. err < current min. err | x)$
- train with config x, observe valid. err. v, D  $\leftarrow$  D U  $\{(x,v)\}$



#### Discussion

#### Concerns

Many algorithms and variants (burgeoning field)

- Hyper-parameters (layer size, regularization, possibly learning rate)
  - Use multi-core machines, clusters and random sampling for cross-validation or sequential modelbased optimization

#### Concerns

- Slower to train than linear models
  - Only by a small constant factor, and much more compact than non-parametric (e.g. n-gram models or kernel machines)
  - Very fast during inference/test time (feed-forward pass is just a few matrix multiplies)
- Need more training data?
  - Can handle and benefit from more training data (esp. unlabeled), suitable for Big Data (Google trains nets with a billion connections, [Le et al, ICML 2012; Dean et al NIPS 2012])
  - Actually needs less labeled data

#### Concern: non-convex optimization

- Can initialize system with convex learner
  - Convex SVM
  - Fixed feature space
- Then optimize non-convex variant (add and tune learned features), can't be worse than convex learner

Part 4

Challenges & Questions

# Why is Unsupervised Pre-Training Sometimes Working So Well?

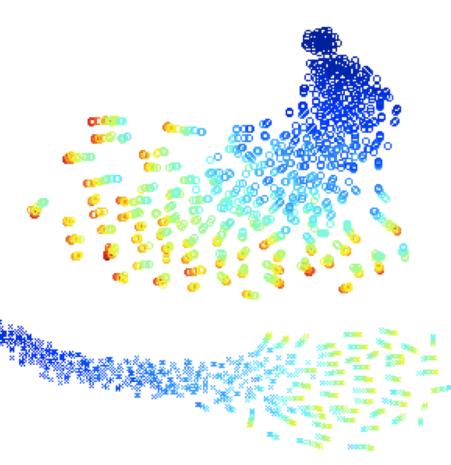
- Regularization hypothesis:
  - Unsupervised component forces model close to P(x)
  - Representations good for P(x) are good for P(y|x)
- Optimization hypothesis:
  - Unsupervised initialization near better local minimum of P(y|x)
  - Can reach lower local minimum otherwise not achievable by random initialization
  - Easier to train each layer using a layer-local criterion



(Erhan et al JMLR 2010)

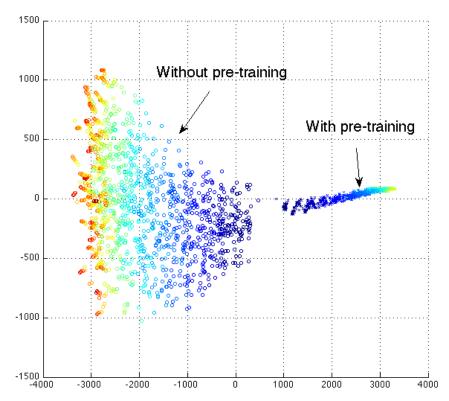
### Learning Trajectories in Function Space

- Each point a model in function space
- Color = epoch
- Top: trajectories w/o pre-training
- Each trajectory converges in different local min.
- No overlap of regions with and w/o pretraining



### Learning Trajectories in Function Space

- Each trajectory converges in different local min.
- With ISOMAP, try to preserve geometry: pretrained nets converge near each other (less variance)
- Good answers =
   worse than a needle
   in a haystack
   (learning dynamics)

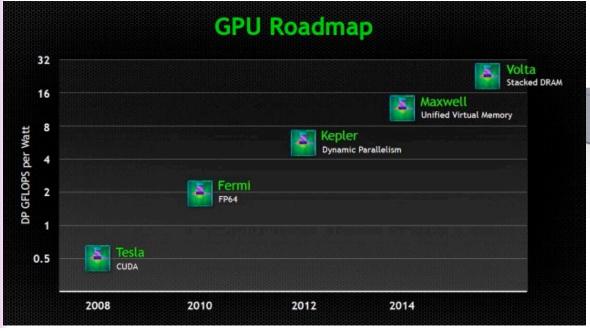


# Deep Learning Challenges (Bengio, arxiv 1305.0445 Deep learning of representations: Looking forward)

- Computational Scaling
- Optimization & Underfitting
- Approximate Inference & Sampling
- Disentangling Factors of Variation
- Reasoning & One-Shot Learning of Facts

#### Challenge: Computational Scaling

- Recent breakthroughs in speech, object recognition and NLP hinged on faster computing, GPUs, and large datasets
- A 100-fold speedup is possible without waiting another 10yrs?
  - Challenge of distributed training
  - Challenge of conditional computation





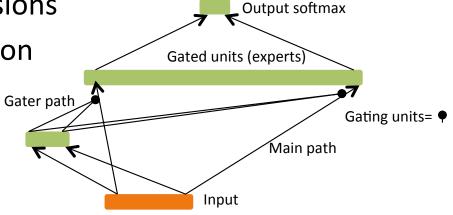
# Conditional Computation: only visit a small fraction of parameters / example

- Deep nets vs decision trees
- Hard mixtures of experts
- Conditional computation for deep nets: sparse distributed gaters selecting combinatorial subsets of a deep net
- Challenges:

Back-prop through hard decisions

Gated architectures exploration

 Symmetry breaking to reduce ill-conditioning



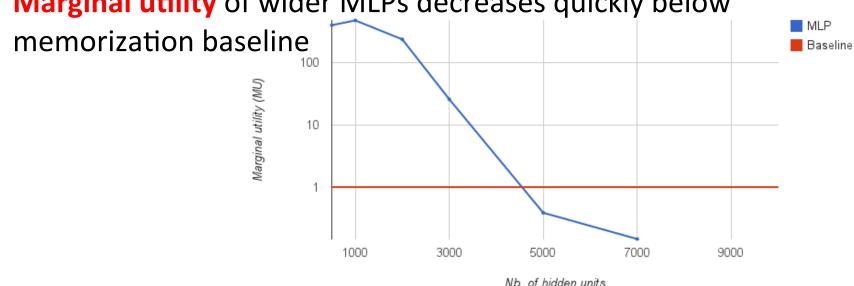
#### Distributed Training

- Minibatches (too large = slow down)
- Large minibatches + 2<sup>nd</sup> order methods
- Asynchronous SGD (Bengio et al 2003, Le et al ICML 2012, Dean et al NIPS 2012)
  - Bottleneck: sharing weights/updates among nodes
- New ideas:
  - Low-resolution sharing only where needed
  - Specialized conditional computation (each computer specializes in updates to some cluster of gated experts, and prefers examples which trigger these experts)

#### Optimization & Underfitting

On large datasets, major obstacle is underfitting

Marginal utility of wider MLPs decreases quickly below



- Current limitations: local minima or ill-conditioning?
- Adaptive learning rates and stochastic 2<sup>nd</sup> order methods
- Conditional comp. & sparse gradients  $\rightarrow$  better conditioning: when some gradients are 0, many cross-derivatives are also 0.

#### MCMC Sampling Challenges

- Burn-in
  - Going from an unlikely configuration to likely ones



- Mixing
  - Local: auto-correlation between successive samples



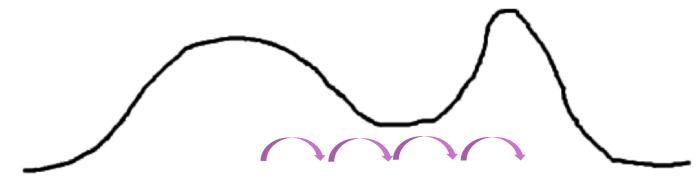
challenge

Global: mixing between major "modes"

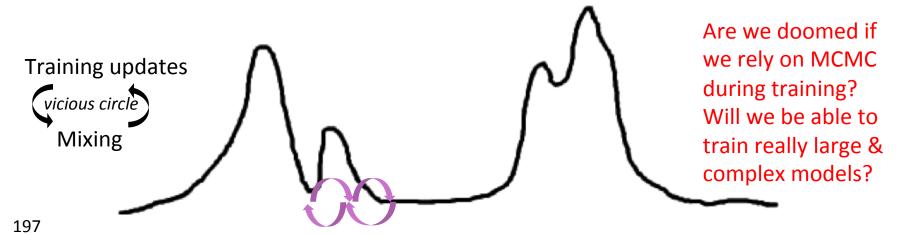


#### For gradient & inference: More difficult to mix with better trained models

Early during training, density smeared out, mode bumps overlap



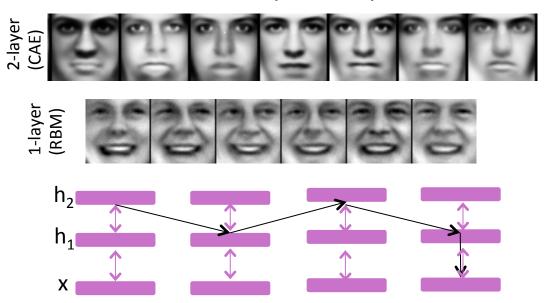
Later on, hard to cross empty voids between modes



#### Poor Mixing: Depth to the Rescue

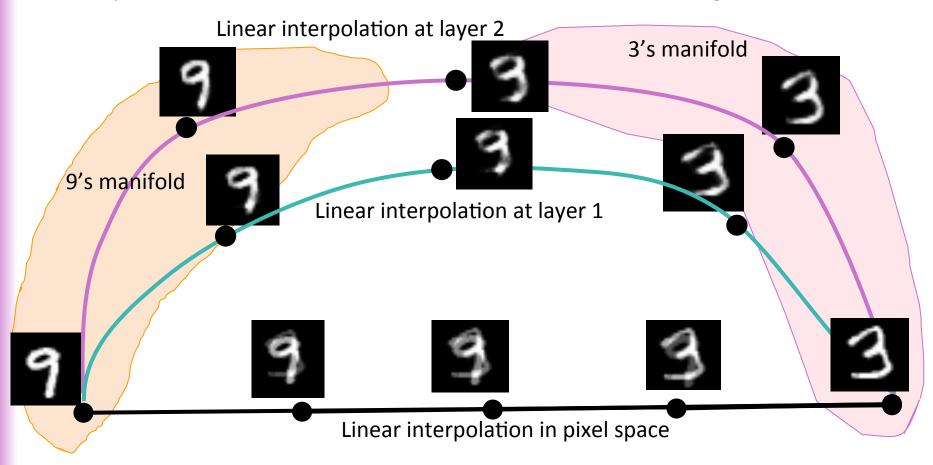
(Bengio et al ICML 2013)

- Sampling from DBNs and stacked Contractive Auto-Encoders:
  - 1. MCMC sampling from top layer model
  - Propagate top-level representations to input-level repr.
- Deeper nets visit more modes (classes) faster



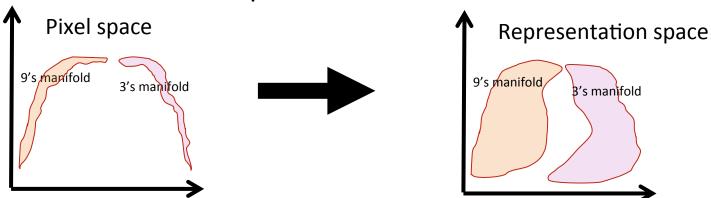
#### Space-Filling in Representation-Space

 High-probability samples fill more the convex set between them when viewed in the learned representation-space, making the empirical distribution more uniform and unfolding manifolds



#### Poor Mixing: Depth to the Rescue

- Deeper representations → abstractions → disentangling
- E.g. reverse video bit, class bits in learned representations: easy to Gibbs sample between modes at abstract level
- Hypotheses tested and not rejected:
  - more abstract/disentangled representations unfold manifolds and fill more the space



can be exploited for better mixing between modes

#### Inference Challenges

- Many latent variables involved in understanding complex inputs (e.g. in NLP: sense ambiguity, parsing, semantic role)
- Almost any inference mechanism can be combined with deep learning
- See [Bottou, LeCun, Bengio 97], [Graves 2012]









 Complex inference can be hard (exponentially) and needs to be approximate → learn to perform inference

### Inference & Sampling

- Currently for unsupervised learning & structured output models
- P(h|x) intractable because of many important modes
- MAP, Variational, MCMC approximations limited to 1 or few modes

Approximate inference can hurt learning

(Kulesza & Pereira NIPS'2007)

 Mode mixing harder as training progresses (Bengio et al ICML 2013)

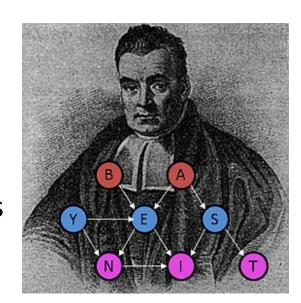
Training updates

vicious circle

Mixing

#### Latent Variables Love-Hate Relationship

- GOOD! Appealing: model explanatory factors h
- BAD! Exact inference? Nope. Just Pain.
   too many possible configurations of h
- WORSE! Each learning step usually requires inference and/or sampling from P(h, x)



# Anonymous Latent Variables

- No pre-assigned semantics
- Learning discovers underlying factors,
   e.g., PCA discovers leading directions of variations
- Increases expressiveness of  $P(x) = \sum_{h} P(x,h)$
- Universal approximators, e.g. for RBMs

(Le Roux & Bengio, Neural Comp. 2008)

#### Approximate Inference

- MAP
  - $h^* \cong \operatorname{argmax}_h P(h|x) \rightarrow \operatorname{assume} 1 \operatorname{dominant} \operatorname{mode}$
- Variational
  - Look for tractable Q(h) minimizing KL(Q(.)||P(.|x))
  - Q is either factorial or tree-structured
  - strong assumption
- MCMC
  - Setup Markov chain asymptotically sampling from P(h|x)
  - Approx. marginalization through MC avg over few samples
  - assume a few dominant modes
- Approximate inference can seriously hurt learning (Kulesza & Pereira NIPS'2007)

### Learned Approximate Inference

- 1. Construct a computational graph corresponding to inference
  - Loopy belief prop. (Ross et al CVPR 2011, Stoyanov et al 2011)
  - Variational mean-field (Goodfellow et al, ICLR 2013)
  - MAP (Kavukcuoglu et al 2008, Gregor & LeCun ICML 2010)
- 2. Optimize parameters wrt criterion of interest, possibly decoupling from the generative model's parameters

Learning can compensate for the inadequacy of approximate inference, taking advantage of specifics of the data distribution

### However: Potentially HUGE Number of Modes in Posterior P(h|x)

- Foreign speech utterance example, y=answer to question:
  - 10 word segments
  - 100 plausible candidates per word
  - 10<sup>6</sup> possible segmentations
  - Most configurations (999999/1000000) implausible
  - → 10<sup>20</sup> high-probability modes
- All known approximate inference scheme may break down if the posterior has a huge number of modes (fails MAP & MCMC) and not respecting a variational approximation (fails variational)

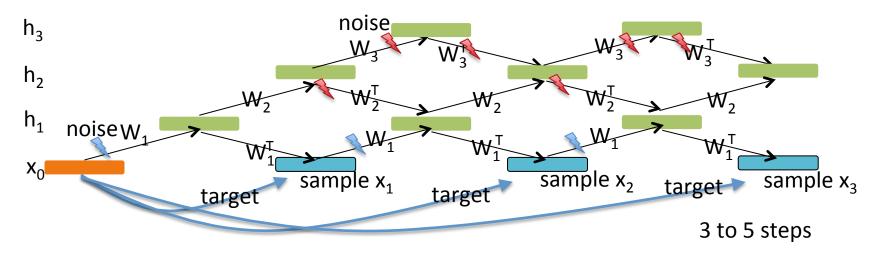


- Deep neural nets learn good P(y|x) classifiers even if there are potentially many true latent variables involved
- Exploits structure in P(y|x) that persist even after summing h

 But how do we generalize this idea to full joint-distribution learning and answering any question about these variables, not just one?

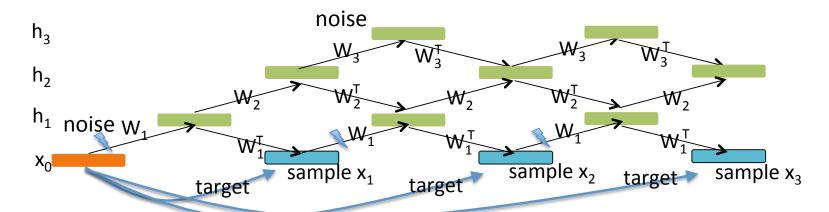
#### Learning Computational Graphs

- Deep Stochastic Generative Networks (GSNs) trainable by backprop (Bengio & Laufer, arxiv 1306.1091)
- Avoid any explicit latent variables whose marginalization is intractable, instead train a stochastic computational graph that generates the right {conditional} distribution.

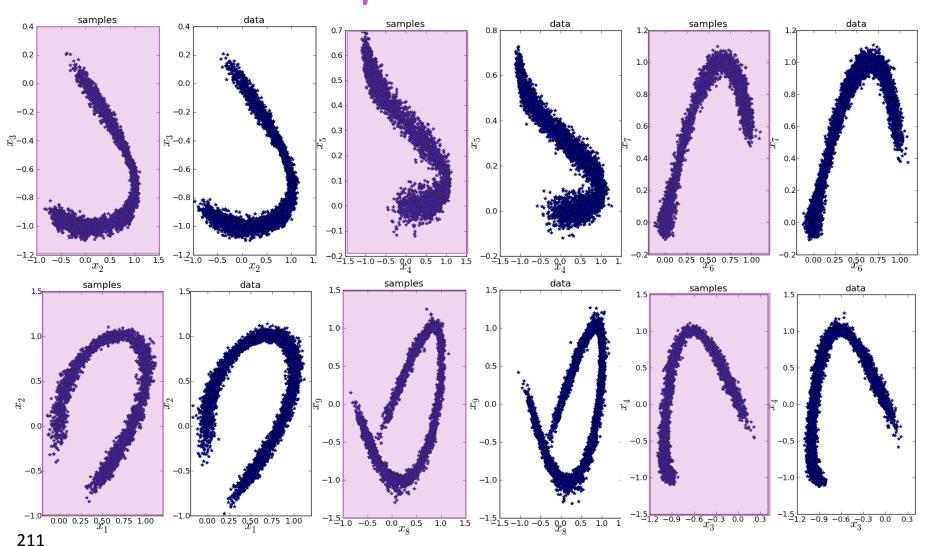


#### Theoretical Results

- The Markov chain associated with a denoising auto-encoder is a consistent estimator of the data generating distribution (if the chain converges)
- Same thing for Generative Stochastic Networks (so long as the reconstruction probability has enough expressive power to learn the required conditional distribution).



## GSN Experiments: validating the theorem in a continuous non-parametric setting



GSN Experiments: Consecutive Samples Filling-in the LHS 0000000000000 うりりりううううううう 0000000000000000000000000

# The Challenge of Disentangling Underlying Factors

- Good disentangling →
  - figure out the underlying structure of the data
  - avoid curse of dimensionality
  - mix better between modes



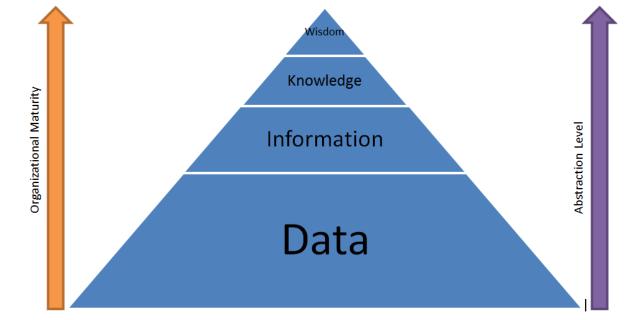


# Learning Multiple Levels of Abstraction

 The big payoff of deep learning is to allow learning higher levels of abstraction

 Higher-level abstractions disentangle the factors of variation, which allows much easier generalization and

transfer



If Time Permits...

Issue: underfitting due to combinatorially many poor effective local minima

where the optimizer gets stuck

#### Culture vs Effective Local Minima

Bengio 2013 (also arXiv 2012)

## Hypothesis 1

 When the brain of a single biological agent learns, it performs an approximate optimization with respect to some endogenous objective.

## Hypothesis 2

• When the brain of a single biological agent learns, it relies on approximate local descent in order to gradually improve itself.

Theoretical and experimental results on deep learning suggest:

## Hypothesis 3

 Higher-level abstractions in brains are represented by deeper computations (going through more areas or more computational steps in sequence over the same areas).

## Hypothesis 4

 Learning of a single human learner is limited by effective local minima.

## Hypothesis 5

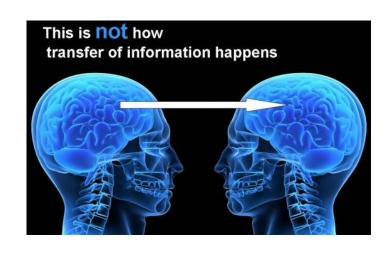
 A single human learner is unlikely to discover high-level abstractions by chance because these are represented by a deep sub-network in the brain.

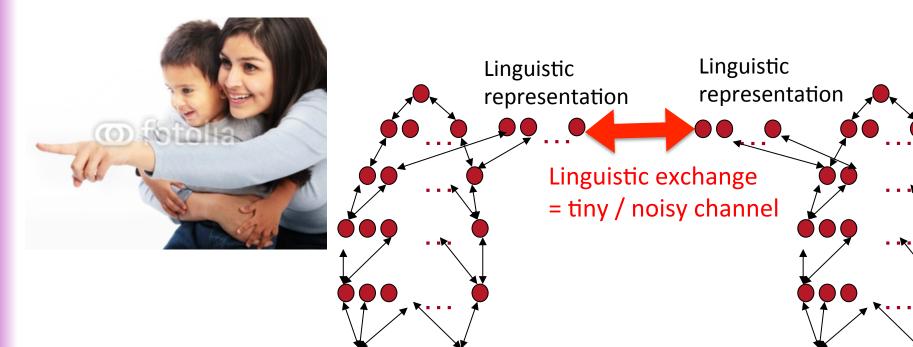
## Hypothesis 6

Curriculum learning 2009)

 A human brain can learn high-level abstractions if guided by the signals produced by other humans, which act as hints or indirect supervision for these high-level abstractions.

# How is one brain transferring abstractions to another brain?





Shared input X

# How do we escape Local minima?

- linguistic inputs = extra examples, summarize knowledge
- criterion landscape easier to optimize (e.g. curriculum learning)
- turn difficult unsupervised learning into easy supervised learning of intermediate abstractions

#### How could language/education/ culture possibly help find the better local minima associated with more useful abstractions?

## Hypothesis 7

More than random search: potential exponential speed-up by divide-and-conquer combinatorial advantage: can combine solutions to independently solved sub-problems

 Language and meme recombination provide an efficient evolutionary operator, allowing rapid search in the space of memes, that helps humans build up better high-level internal representations of their world.

#### From where do new ideas emerge?

• Seconds: inference (novel explanations for current x)

Minutes, hours: learning (local descent, like current DL)

 Years, centuries: cultural evolution (global optimization, recombination of ideas from other humans)

#### Related Tutorials

- Deep Learning tutorials (python): <a href="http://deeplearning.net/tutorials">http://deeplearning.net/tutorials</a>
- Stanford deep learning tutorials with simple programming assignments and reading list <a href="http://deeplearning.stanford.edu/wiki/">http://deeplearning.stanford.edu/wiki/</a>
- ACL 2012 Deep Learning for NLP tutorial <a href="http://www.socher.org/index.php/DeepLearningTutorial/">http://www.socher.org/index.php/DeepLearningTutorial/</a>
- ICML 2012 Representation Learning tutorial <a href="http://www.iro.umontreal.ca/~bengioy/talks/deep-learning-tutorial-2012.html">http://www.iro.umontreal.ca/~bengioy/talks/deep-learning-tutorial-2012.html</a>
- IPAM 2012 Summer school on Deep Learning
   <a href="http://www.iro.umontreal.ca/~bengioy/talks/deep-learning-tutorial-aaai2013.html">http://www.iro.umontreal.ca/~bengioy/talks/deep-learning-tutorial-aaai2013.html</a>
- More reading: Paper references in separate pdf, on my web page

## Software

- Theano (Python CPU/GPU) mathematical and deep learning library <a href="http://deeplearning.net/software/theano">http://deeplearning.net/software/theano</a>
  - Can do automatic, symbolic differentiation
- Senna: POS, Chunking, NER, SRL
  - by Collobert et al. <a href="http://ronan.collobert.com/senna/">http://ronan.collobert.com/senna/</a>
  - State-of-the-art performance on many tasks
  - 3500 lines of C, extremely fast and using very little memory
- Torch ML Library (C++ + Lua) <a href="http://www.torch.ch/">http://www.torch.ch/</a>
- Recurrent Neural Network Language Model <a href="http://www.fit.vutbr.cz/~imikolov/rnnlm/">http://www.fit.vutbr.cz/~imikolov/rnnlm/</a>
- Recursive Neural Net and RAE models for paraphrase detection, sentiment analysis, relation classification <u>www.socher.org</u>

#### Software: what's next

- Off-the-shelf SVM packages are useful to researchers from a wide variety of fields (no need to understand RKHS).
- To make deep learning more accessible: release offthe-shelf learning packages that handle hyperparameter optimization, exploiting multi-core or cluster at disposal of user.
  - Spearmint (Snoek)
  - HyperOpt (Bergstra)

#### Conclusions

- Deep Learning & Representation Learning have matured
  - Int. Conf. on Learning Representation 2013 a huge success!
- Industrial strength applications in place (Google, Microsoft)
- Room for more research:
  - Scaling computation even more
  - Better optimization
  - Getting rid of intractable inference (in the works!)
  - Coaxing the models into more disentangled abstractions
  - Learning to reason from incrementally added facts

## LISA team: Merci. Questions?

