# RngStreams: An object-oriented random-number package in C with many long streams and substreams

This file describes a C interface to the RngStreams package. The backbone generator is the combined multiple recursive generator (CMRG) Mrg32k3a proposed in [1], implemented in 64-bit floating-point arithmetic. This backbone generator has period length  $\rho \approx 2^{191}$ . The values of V, W, and Z are  $2^{51}$ ,  $2^{76}$ , and  $2^{127}$ , respectively. The seed of the RNG, and the state of a stream at any given step, are 6-dimensional vectors of 32-bit integers. The default initial seed of the package is (12345, 12345, 12345, 12345, 12345).

```
typedef struct RngStream_InfoState * RngStream;
struct RngStream_InfoState {
   double Cg[6], Bg[6], Ig[6];
   int Anti;
   int IncPrec;
   char *name;
};
```

The state of a stream from the present module. The arrays Ig, Bg, and Cg contain the initial state, the starting point of the current substream, and the current state, respectively. This stream generates antithetic variates if  $Anti \neq 0$ . The precision of the output numbers is increased if  $IncPrec \neq 0$ .

#### int RngStream\_SetPackageSeed (unsigned long seed[6]);

Sets the initial seed of the package RngStreams to the six integers in the vector seed. This will be the seed (initial state) of the first stream. If this procedure is not called, the default initial seed is (12345, 12345, 12345, 12345, 12345, 12345, 12345). If it is called, the first 3 values of the seed must all be less than  $m_1 = 4294967087$ , and not all 0; and the last 3 values must all be less than  $m_2 = 4294944443$ , and not all 0. Returns -1 for invalid seeds, and 0 otherwise.

#### RngStream RngStream\_CreateStream (const char name[]);

Creates and returns a new stream with identifier name, whose state variable is of type RngStream\_InfoState. This procedure reserves space to keep the information relative to the RngStream, initializes its seed  $I_g$ , sets  $B_g$  and  $C_g$  equal to  $I_g$ , sets its antithetic and precision switches to 0. The seed  $I_g$  is equal to the initial seed of the package given by RngStream\_SetPackageSeed if this is the first stream created, otherwise it is Z steps ahead of that of the most recently created stream.

```
void RngStream_DeleteStream (RngStream g);
```

Deletes the stream g created previously by RngStream\_CreateStream, and recovers its memory.

```
void RngStream_ResetStartStream (RngStream g);
```

Reinitializes the stream g to its initial state:  $C_g$  and  $B_g$  are set to  $I_g$ .

```
void RngStream_ResetStartSubstream (RngStream g);
```

Reinitializes the stream g to the beginning of its current substream:  $C_g$  is set to  $B_g$ .

#### void RngStream\_ResetNextSubstream (RngStream g);

Reinitializes the stream g to the beginning of its next substream:  $N_g$  is computed, and  $C_g$  and  $B_g$  are set to  $N_g$ .

#### void RngStream\_SetAntithetic (RngStream g, int a);

If  $a \neq 0$ , the stream g will start generating antithetic variates, i.e., 1-U instead of U, until this method is called again with a = 0.

#### void RngStream\_IncreasedPrecis (RngStream g, int incp);

After calling this procedure with  $\mathtt{incp} \neq 0$ , each call (direct or indirect) to RngStream\_RandU01 for stream g will advance the state of the stream by 2 steps instead of 1, and will return a number with (roughly) 53 bits of precision instead of 32 bits. More specifically, in the non-antithetic case, the instruction "x = RngStream\_RandU01(g)" when the precision is increased is equivalent to "x = (RngStream\_RandU01(g) + RngStream\_RandU01(g) \* fact) % 1.0" where the constant fact is equal to  $2^{-24}$ . This also applies when calling RngStream\_RandU01 indirectly (e.g., by calling RngStream\_RandInt, etc.). By default, or if this procedure is called again with  $\mathtt{incp} = 0$ , each call to RngStream\_RandU01 for stream g advances the state by 1 step and returns a number with 32 bits of precision.

#### int RngStream\_SetSeed (RngStream g, unsigned long seed[6]);

Sets the initial seed  $I_g$  of stream g to the vector seed. This vector must satisfy the same conditions as in RngStream\_SetPackageSeed. The stream is then reset to this initial seed. The states and seeds of the other streams are not modified. As a result, after calling this procedure, the initial seeds of the streams are no longer spaced Z values apart. We discourage the use of this procedure. Returns -1 for invalid seeds, and 0 otherwise.

#### void RngStream\_AdvanceState (RngStream g, long e, long c);

Advances the state of stream g by k values, without modifying the states of other streams (as in RngStream\_SetSeed), nor the values of  $B_g$  and  $I_g$  associated with this stream. If e > 0, then  $k = 2^e + c$ ; if e < 0, then  $k = -2^{-e} + c$ ; and if e = 0, then k = c. Note: c is allowed to take negative values. We discourage the use of this procedure.

#### void RngStream\_GetState (RngStream g, unsigned long seed[6]);

Returns in seed[] the current state  $C_g$  of stream g. This is convenient if we want to save the state for subsequent use.

#### void RngStream\_WriteState (RngStream g);

Prints (to standard output) the current state of stream g.

#### void RngStream\_WriteStateFull (RngStream g);

Prints (to standard output) the name of stream g and the values of all its internal variables.

#### double RngStream\_RandU01 (RngStream g);

Returns a (pseudo)random number from the uniform distribution over the interval (0,1), using stream  $\mathbf{g}$ , after advancing the state by one step. The returned number has 32 bits of precision

in the sense that it is always a multiple of  $1/(2^{32}-208)$ , unless RngStream\_IncreasedPrecis has been called for this stream.

### int RngStream\_RandInt (RngStream g, int i, int j);

Returns a (pseudo)random number from the discrete uniform distribution over the integers  $\{i,i+1,\ldots,j\}$ , using stream g. Makes one call to RngStream\_RandUO1.

## References

[1] P. L'Ecuyer. Good parameters and implementations for combined multiple recursive random number generators. *Operations Research*, 47(1):159–164, 1999.