

Convolutional Networks for Images, Speech, and Time-Series

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1 INTRODUCTION

The ability of multilayer back-propagation networks to learn complex, high-dimensional, non-linear mappings from large collections of examples makes them obvious candidates for image recognition or speech recognition tasks (see PATTERN RECOGNITION AND NEURAL NETWORKS). In the traditional model of pattern recognition, a hand-designed feature extractor gathers relevant information from the input and eliminates irrelevant variabilities. A trainable classifier then categorizes the resulting feature vectors (or strings of symbols) into classes. In this scheme, standard, fully-connected multilayer networks can be used as classifiers. A potentially more interesting scheme is to eliminate the feature extractor, feeding the network with “raw” inputs (e.g. normalized images), and to rely on backpropagation to turn the first few layers into an appropriate feature extractor. While this can be done with an ordinary fully connected feed-forward network with some success for tasks such as character recognition, there are problems.

Firstly, typical images, or spectral representations of spoken words, are large, often with several hundred variables. A fully-connected first layer with, say a few 100 hidden units, would already contain several 10,000 weights. Overfitting problems may occur if training data is scarce. In addition, the memory requirement for that many weights may rule out certain hardware implementations. But, the main deficiency of unstructured nets for image or speech applications is that they have no built-in invariance with respect to translations, or

local distortions of the inputs. Before being sent to the fixed-size input layer of a neural net, character images, spoken word spectra, or other 2D or 1D signals, must be approximately size-normalized and centered in the input field. Unfortunately, no such preprocessing can be perfect: handwriting is often normalized at the word level, which can cause size, slant, and position variations for individual characters; words can be spoken at varying speed, pitch, and intonation. This will cause variations in the position of distinctive features in input objects. In principle, a fully-connected network of sufficient size could learn to produce outputs that are invariant with respect to such variations. However, learning such a task would probably result in multiple units with identical weight patterns positioned at various locations in the input. Learning these weight configurations requires a very large number of training instances to cover the space of possible variations. On the other hand, in convolutional networks, shift invariance is automatically obtained by forcing the replication of weight configurations across space.

Secondly, a deficiency of fully-connected architectures is that the topology of the input is entirely ignored. The input variables can be presented in any (fixed) order without affecting the outcome of the training. On the contrary, images, or spectral representations of speech have a strong 2D local structure, and time-series have a strong 1D structure: variables (or pixels) that are spatially or temporally nearby are highly correlated. Local correlations are the reasons for the well-known advantages of extracting and combining *local* features before recognizing spatial or temporal objects. Convolutional networks force the extraction of local features by restricting the receptive fields of hidden units to be local.

2 CONVOLUTIONAL NETWORKS

Convolutional networks combine three architectural ideas to ensure some degree of shift and distortion invariance: local receptive fields, shared weights (or weight replication), and, sometimes, spatial or temporal subsampling. A typical convolutional network for recognizing characters is shown in figure 1 (from (LeCun et al., 1990)). The input plane receives images of characters that are approximately size-normalized and centered. Each unit of a layer receives inputs from a set of units located in a small neighborhood in the previous layer. The idea of connecting units to local receptive fields on the input goes back to the Perceptron in the early 60s, and was almost simultaneous with Hubel and Wiesel's discovery of locally-sensitive, orientation-selective neurons in the cat's visual system. Local connections have been reused many times in neural models of visual learning (see (Mozer, 1991; Le Cun, 1986) and NEOCOGNITRON in this handbook). With local receptive fields, neurons can extract elementary visual features such as oriented edges, end-points, corners (or similar features in speech spectrograms). These features are then combined by the higher layers. As stated earlier, distortions or shifts of the input can cause the position of salient features to vary. In addition, elementary feature detectors that are useful on one part of the image are likely to be useful across the entire image. This knowledge can be applied by forcing a set of units, whose receptive fields are located at different places on the image, to have identical weight vectors (Rumelhart, Hinton and Williams, 1986). The outputs of such a set of neurons constitute a *feature map*. At each position, different types of units in different

feature maps compute different types of features. A sequential implementation of this, for each feature map, would be to scan the input image with a single neuron that has a local receptive field, and to store the states of this neuron at corresponding locations in the feature map. This operation is equivalent to a convolution with a small size kernel, followed by a squashing function. The process can be performed in parallel by implementing the feature map as a plane of neurons that *share* a single weight vector. Units in a feature map are constrained to perform the same operation on different parts of the image. A convolutional layer is usually composed of several feature maps (with different weight vectors), so that multiple features can be extracted at each location. The first hidden layer in figure 1 has 4 feature maps with 5 by 5 receptive fields. Shifting the input of a convolutional layer will shift the output, but will leave it unchanged otherwise. Once a feature has been detected, its exact location becomes less important, as long as its approximate position relative to other features is preserved. Therefore, each convolutional layer is followed by an additional layer which performs a local averaging and a subsampling, reducing the resolution of the feature map, and reducing the sensitivity of the output to shifts and distortions. The second hidden layer in figure 1 performs 2 by 2 averaging and subsampling, followed by a trainable coefficient, a trainable bias, and a sigmoid. The trainable coefficient and bias control the effect of the squashing non-linearity (for example, if the coefficient is small, then the neuron operates in a quasi-linear mode). Successive layers of convolutions and subsampling are typically alternated, resulting in a “bi-pyramid”: at each layer, the number of feature maps is increased as the spatial resolution is decreased. Each unit in the third hidden layer in figure 1 may have input connections from several feature maps in the previous layer. The

convolution/subsampling combination, inspired by Hubel and Wiesel's notions of "simple" and "complex" cells, was implemented in the Neocognitron model (see NEOCOGNITRON), though no globally supervised learning procedure such as back-propagation was available then.

Since all the weights are learned with back-propagation, convolutional networks can be seen as synthesizing their own feature extractor. The weight sharing technique has the interesting side effect of reducing the number of free parameters, thereby reducing the "capacity" of the machine and improving its generalization ability (see (LeCun, 1989) on weight sharing, and LEARNING AND GENERALIZATION for an explanation of notions of capacity and generalization). The network in figure 1 contains about 100,000 connections, but only about 2,600 free parameters because of the weight sharing. Such networks compare favorably with other methods on handwritten character recognition tasks (Bottou et al., 1994) (see also HAND WRITTEN DIGIT RECOGNITION), and they have been deployed in commercial applications.

Fixed-size convolutional networks that share weights along a single temporal dimension are known as Time-Delay Neural Networks (TDNNs). TDNNs have been used in phoneme recognition (without subsampling) (Lang and Hinton, 1988; Waibel et al., 1989), spoken word recognition (with subsampling) (Bottou et al., 1990), and on-line handwriting recognition (Guyon et al., 1991).

3 VARIABLE-SIZE CONVOLUTIONAL NETWORKS, SDNN

While characters or short spoken words can be size-normalized and fed to a fixed-size network, more complex objects such as written or spoken words and sentences have inherently variable size. One way of handling such a composite object is to segment it heuristically into simpler objects that can be recognized individually (e.g., characters, phonemes). However, reliable segmentation heuristics do not exist for speech or cursive handwriting. A brute force solution is to scan (or replicate) a recognizer at all possible locations across the input. While this can be prohibitively expensive in general, convolutional networks can be scanned or replicated very efficiently over large, variable-size input fields. Consider one instance of a convolutional net and its *alter ego* at a nearby location. Because of the convolutional nature of the networks, units in the two nets that look at identical locations on the input have identical outputs, therefore their output does not need to be computed twice. In effect, replicating a convolutional network can be done simply by increasing the size of the field over which the convolutions are performed, and replicating the output layer, effectively making it a convolutional layer. An output whose receptive field is centered on an elementary object will produce the class of this object, while an in-between output may be empty or contain garbage. The outputs can be interpreted as evidence for the categories of object centered at different positions of the input field. A post-processor is therefore required to pull out consistent interpretations of the output. Hidden Markov Models (HMM) or other graph-based

methods are often used for that purpose (see SPEECH RECOGNITION, and PATTERN RECOGNITION AND NEURAL NETWORKS in this volume). The replicated network and the HMM can be trained simultaneously by back-propagating gradients through the HMM. Globally trained, variable-size TDNN/HMM hybrids have been used for speech recognition (see PATTERN RECOGNITION AND NEURAL NETWORKS for a list of references) and on-line handwriting recognition (Schenkel et al., 1993). Two-dimensional replicated convolutional networks, called “Space Displacement Neural Networks” (SDNN) have been used in combination with HMMs or other elastic matching methods for handwritten word recognition (Keeler and Rumelhart, 1991; Matan et al., 1992; Bengio, LeCun and Henderson, 1994). Another interesting application of SDNNs is object spotting (Wolf and Platt, 1994).

An important advantage of convolutional neural networks is the ease with which they can be implemented in hardware. Specialized analog/digital chips have been designed and used in character recognition, and in image preprocessing applications (Boser et al., 1991). Speeds of more than 1000 characters per second were obtained with a network with around 100,000 connections (shown in figure 1).

The idea of subsampling can be turned around to construct networks similar to TDNNs, but that can generate sequences from labels. These networks are called reverse-TDNNs because they can be viewed as upside-down TDNNs: temporal resolution increases from the input to the output, through alternated oversampling and convolution layers (Simard and LeCun, 1992).

4 DISCUSSION

Convolutional neural networks are a good example of an idea inspired by biology that resulted in competitive engineering solutions that compare favorably with other methods (Bottou et al., 1994). While applying convolutional nets to image recognition removes the need for a separate hand-crafted feature extractor, normalizing the images for size and orientation (if only approximately) is still required. Shared weights and subsampling bring invariance with respect to small geometric transformations or distortions, but fully invariant recognition is still beyond reach. Radically new architectural ideas, possibly suggested by biology, will be required for a fully neural image or speech recognition system.

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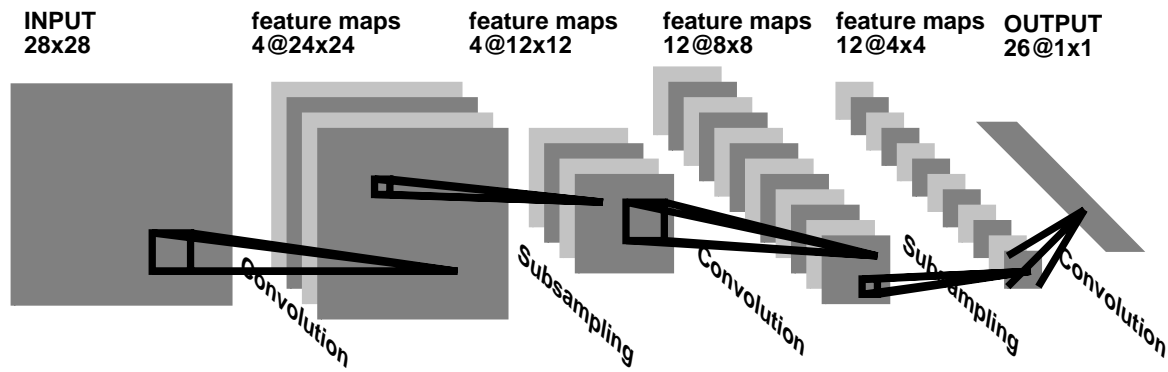


Figure 1: Convolutional Neural Network for image processing, e.g., handwriting recognition

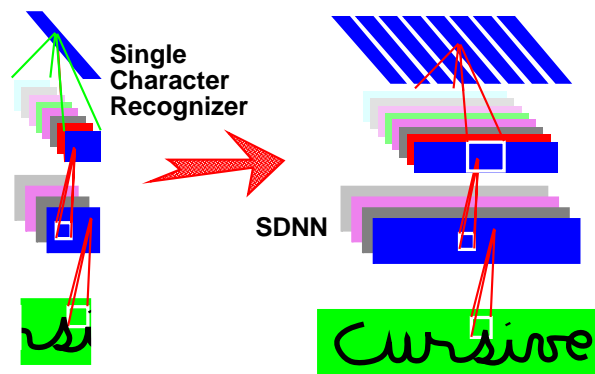


Figure 2: Variable-size replicated convolutional network, SDNN