in Bacteria

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Abstract. The distribution of the lengths of genomic segments invert during the evolutionary divergence of two species cannot be inferred of rectly from the output of genome rearrangement algorithms, due to t rapid loss of signal from all but the shortest inversions. The numb of short inversions produced by these algorithms, however, particular those involving a single gene, is relatively reliable. To gain some insig into the shape of the inversion-length distribution we first apply a genor rearrangement algorithm to each of 32 pairs of bacterial genomes. F each pair we then simulate their divergence using a test distribution generate the inversions and use the simulated genomes as input to t reconstruction algorithm. It is the comparison between the algorith output for the real pair of genomes and the simulated pair which is us to assess the test distribution. We find that simulations based on t exponential distribution cannot provide a good fit, but that simulation based on a gamma distribution can account for both single-gene inve sions and short inversions involving at most 20 genes, and we conclu that the shape of latter distribution corresponds well to the true dist bution at least for small inversion lengths.

1 Introduction

The study of genome rearrangement has made it clear that the length chromosomal segments inverted, transposed or reciprocally translocated determined simply by a random choice of two breakpoints anywher genome. While this is very-well documented in eukaryotes [2, 10, 13, 5], true that prokaryotic genome rearrangement also operates under a v constraints on inversion site and length of inverted segments [12, 17 corporating information on such constraints into procedures for reconsgenome divergence, e.g. in terms of weights in a parsimony analysis, prof in a likelihood analysis or priors in a Bayesian analysis, is a desirable

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evolutionary methodology. With this motivation, in this paper we study tribution of lengths of the segments that are inverted in the evolutionary of bacterial genomes. Inherent in this study are many assumptions, not of which is that the distribution in question exists, i.e., represents a tend atively fixed over time and across the phylogenetic spectrum of bacteri we cannot resolve such a far-reaching question here, our results will p measure of confirmatory justification.

Another assumption is that inversion is the dominant process of ge change in bacteria. Our approach will control for changes in genome size gene gain and gene loss, but not for the effects of simply transposing s from one area of the genome to another. This does not seem to be unwa we find no systematic discussion of a transposition process in the liter bacterial genomes, though transposition of small segments is very coneukaryotic nuclear genomes [5, 10], and duplication-loss, which has t effect as transposition, is often cited as an explanation for gene-order of eukaryotic organelle genomes [3].

In a previous study [11], we analyzed the inversion lengths inferred each of four pairs of bacterial genomes and discovered an unexpectedly h ber of short inversions, single-gene inversions in particular. This contrass the null hypothesis that the two breakpoints of an inversion occur rando independently within the genome of length n, which predicts a uniform tion $U[1, \frac{n}{2}]$ of inversion lengths, where the $\frac{n}{2}$ reflects the fact that for a genome, an inversion of length l is indistinguishable from the complet inversion of length n - l.

The present paper builds on the previous work in two ways. First, w expand our sample of genome pairs, from four to 32, deliberately picked sent the range between closely-related and phylogenetically distant pairs use a more systematic method than in the previous paper for validating of orthology within each pair. Second, rather than just reject the unif hypothesis, we attempt to pin down aspects of the probability distributive version length in bacterial evolution. More precisely, we focus on the shap distribution only where the inversions are short, namely single-gene in and inversions of at most 20 genes. This rather restrained ambition is w by the discovery in [11], summarized in Section 2 below, that in genomic have been even moderately rearranged by the accumulation of inversion monious methods such as that Hannenhalli-Pevzner (HP) algorithm [7], recover the details of very short inversions. Simulations in [11] showed longer inversions "recovered" by such algorithms are overwhelmingly from those used to generate the genomes.

In the next section of this paper we recap only the part of [11] wh with signal decay. In Sections 3 and 4 we describe our methods and data 5 contains our results, which show that a two-parameter distribution such as the gamma distribution, is necessary to reasonably fit the nu short inversions observed in the 32 pairs of genomes, but that a one-p distribution, such as that of the negative exponential distribution, is ina These results are further discussed in Section 6.



Fig. 1. Frequency of inversion sizes (or lengths) inferred by the algorithm for genomes obtained by performing i inversions of length l = 50. The figure on for i = 80 and the bottom one is for i = 200

2 Decay of Evolutionary Signal with Inversion Leng

Consider two genomes containing the same set of genes but in different where this difference is generated by evolutionary operations of a given by as inversions. We first ask to what extent the evolutionary histories recorby the HP type of algorithm [7] actually reflect the true events. It is we that past a threshold of θn , where n is the number of genes and θ range of $\frac{1}{3}$ to $\frac{2}{3}$, the *number* of operations begins to be underestimated operation-based inferences (e.g., [8, 9]). Before that threshold, the total may be accurately estimated but whether any signal is conserved as to to individual operations themselves, and which ones, is a different question

In [11], we carried out the following test: For a genome of size n = generated *i* inversions of length l = 5, 10, 15, 20, 50, 100, 200 at random, reconstructed the optimal inversion history, for a range of values of *i*. T for small enough values of *i*, the algorithm reconstructs the true inversion Depending on *l*, however, above a certain value of *i*, the reconstructed in manifest a range of lengths, as illustrated in Figure 1 (reproduced from



Fig. 2. The solid line plots s, and the dotted line plots r (see text abo

For each l, we calculated

 $r_l = \min\{i | \text{reconstruction has at least 5\% error}\}$ and

 $s_l = \max\{i | \text{reconstruction has at most } 95\% \text{ error}\},\$

where any inversion having length different from l is considered to be Figure 2 (reproduced from [11]) plots r and s as a function of l and sh quickly the detailed evolutionary signal decays for large inversions. Neve we note that for very small inversions, there is a clear signal preserved le longer ones have been completely obscured.

3 Method

In our quest for the distribution of inversion lengths in bacteria, there steps applied to each pair of genomes in our sample:

- We use a carefully validated method for establishing orthologies bet two genomes, based on both sequence and genomic context [4].
- We calculate the inversion distance between the two genomes, as number of detailed evolutionary scenarios exemplifying this distance
- We simulate a matching pair of genomes whose divergence is based ever distribution we are testing.

These steps are detailed in the following paragraphs.

3.1 Orthology

In the new method developed in [4], potential orthologs are evaluated a to a number of criteria:

- status of BLAST match; whether it is the best match in both direct
- quality of BLAST match; in terms of statistical significance
- scope of BLAST match with respect to the total length of the gene
- presence or absence of contextual markers conserved in both genon
- whether there are near optimal competing genes in either genome

This enabled us to construct a matched set of orthologous geness genomes with a maximum of confidence. Of course, some of the mat less clear than others, and the matches in closely related genomes te less ambiguous than in distant pairs. Nevertheless these matches rep systematic, multi-criterion, best estimate.

Once the matches are established, we constructed reduced genomes length by deleting those genes not identified as being in an orthologou This paper reports on the analysis of these reduced genomes only, though also analyzed the full genomes using an inversion/insertion/deletion p [6]. Results from the latter were generally less clear, though they did no with the results reported here.

Note that our use of reduced genomes means that our characteriz inversions as "single-gene" or "1-20 genes" in the comparison of the genomes may sometimes refer to somewhat larger inversions when the genes from the unreduced genomes are restored.

3.2 Algorithm

The results of genome rearrangement algorithms are highly non-unique different evolutionary scenarios have the same, minimal, number of ste

In a previous publication [1] we developed a general method that choice among equally optimal solutions (i.e., the same minimal number ations) generated by a HP type of algorithm, based on any one of many secondary criteria. This takes advantage of the many equally valid cho may be available at each step of the algorithm.

Given our interest in short inversions, we adopt inversion length as ondary criterion. Thus a solution can be obtained by selecting, at rando the shortest allowable inversions at each step of the HP procedure. Run algorithm several times gives rise to several possible solutions. We can the late how many times inversions of a particular length recur in the set of solution in [11], we showed that this length-based strategy enhanced the differ tween pairs of real genomes and simulated pairs where the inversion lengt sampled from the $U[1, \frac{n}{2}]$ distribution. The number of reconstructed sin and other short inversions, already higher in the real genome compari in the simulations, based on HP with no secondary strategy, increased number constructed single-gene and other short inversions for the genomes created uniformly generated inversions. In other words, the increased number inversions inferred by length-based strategy was not simply an artifact strategy since it had little if any effect on the simulated genomes. R attributed it to better detection of bonafide short inversions whose s know to be conserved despite extensive genome rearrangement.

3.3 Simulations

To estimate the shape of the probability distribution of inversion leng explored

- a single parameter distribution, namely a negative exponential dist

$$p(l) = \lambda e^{-\lambda l}.$$

- a two-parameter distribution, namely a gamma distribution

$$p(l) = \frac{l^{\alpha - 1}e^{-l/\beta}}{\beta^{\alpha}\Gamma(\alpha)}.$$

For each each distribution p with cumulative P, we derived simulated genomes to compare with each of the 32 real ones as follows. For a give bacterial genomes, let n be the length of the reduced genome, and let number of inversions necessary to derive one from the other, as measure HP algorithm. We sampled somewhat more than i inversions (to confor the bias introduced by parsimonious reconstruction in a later step) probability distribution and used these to evolve a new circular genome from $1, 2, \dots, n$. One of the breakpoints for each inversion was located ron the genome, and the second was located according to the sample ilength. If an inversion was longer than n/2, we discarded it and did nit, since and inversion of length l is the same as an inversion of length a circular genome. So the effective length distribution was actually

$$p^*(l) = \frac{p(l)}{P(\frac{n}{2})}$$
$$0 < l \le \frac{n}{2}$$

for

and zero elsewhere.

4 The Pairs of Bacterial Genomes

We informally sampled 32 pairs of genomes from those treated in [4], some that are as phylogenetically distant as possible, and some that are n closely related. These are listed in Table 1, which also lists i, the n number of inversions necessary to convert one (reduced) genome to the size of the reduced genome n, i.e., the number of orthologous gene the two genomes as determined by the method in [4], the normalized distance i/n, and the number of single-gene and 1-20 gene inversions. identified in the two genomes, i is the inversion distance. Pairs ordered from highest values of the normalized inversion distance i/n. Last two columns number of inversions, out of a total of i, that involve just one gene and twenty genes, respectively

genome A	genome B	i	n	i/i
Neisseria meningitidis MC58	Neisseria meningitidis Z2491	53	1606	0.0
Salmonella typhi	Shigella flexneri 2a	196	2801	0.0'
Escherichia coli CFT073	Salmonella typhimurium LT2	244	3145	0.0
Mycobacterium leprae	Mycobacterium tuberculosis CDC1551	109	1367	0.0
Staphylococcus aureus Mu50	Staphylococcus epidermidis ATCC 12228	148	1805	0.0
Streptococcus agalactiae 2603	Streptococcus pyogenes	201	1156	0.1
Streptococcus mutans	Streptococcus pyogenes	211	1046	0.2
Agrobacterium tumefaciens C58 Uwash Circ	Sinorhizobium meliloti	347	1705	0.2
Escherichia coli CFT073	Yersinia pestis CO92	642	2363	0.2
Pseudomonas aeruginosa	Pseudomonas putida KT2440	996	3189	0.3
Corynebacterium glutamicum	Mycobacterium tuberculosis CDC1551	380	1087	0.3
Bacillus halodurans	Bacillus subtilis	748	1912	0.3
Salmonella typhi	Vibrio cholerae ChI	584	1479	0.3
Listeria innocua	Staphylococcus aureus Mu50	471	1085	0.4
Escherichia coli K12	Vibrio cholerae ChI	717	1648	0.4
Bacillus halodurans	Listeria innocua	518	1186	0.4
Bacillus halodurans	Oceanobacillus iheyensis	818	1856	0.4
Listeria monocytogenes	Staphylococcus epidermidis	486	1080	0.4
Clostridium acetobutylicum	Clostridium perfringens	564	1211	0.4
Salmonella typhimurium LT2	Shewanella oneidensis	741	1474	0.5
Clostridium perfringens	Thermoanaerobacter tengcongensis	427	841	0.5
Oceanobacillus iheyensis	Thermoanaerobacter tengcongensis	452	853	0.5
Pseudomonas putida KT2440	Vibrio cholerae ChI	639	1160	0.5
Staphylococcus epidermidis ATCC 12228	Thermoanaerobacter tengcongensis	359	623	0.5
Listeria innocua	Thermoanaerobacter tengcongensis	450	770	0.5
Clostridium perfringens	Staphylococcus epidermidis ATCC 12228	391	640	0.6
Bacillus halodurans	Clostridium perfringens	619	944	0.6
Mycobacterium tuberculosis CDC1551	Mycoplasma penetrans	90	137	0.6
Bacillus subtilis	Streptococcus agalactiae 2603	533	806	0.6
Bacillus halodurans	Streptococcus pneumoniae R6	509	737	0.6
Staphylococcus aureus Mu50	Streptococcus pyogenes MGAS8232	649	939	0.6
Streptococcus mutans	Thermoanaerobacter tengcongensis	432	598	0.7

We note that parts of the evolutionary history separating many of pairs are shared; perhaps the most obvious example is the E.coli - Version Salmonella - Vibrio comparisons, since these reflect a largely similar l divergence, E.coli and Salmonella having a relatively recent common of This kind of dependence, which in general increase measures of dispersion to bias, is not as great among our other pairs of genomes, and is in virtually impossible to avoid in a phylogenetic context.

5 Results

Applying our algorithm to the 32 pairs of bacterial genomes, repeating e parison ten times with different random choices of shortest allowable is at each step, we counted the average number of single-gene inversions average number of inversions of length 20 or less. These were normali and plotted against the normalized inversion distance i/n in Figure 3.

plotted on Figure 3 the result of our simulations based on the negative α tial and gamma distributions. For the negative exponential, it can be s a value of λ that allows the curve obtained from $p(l) \leq 1$ to fit the n on single-gene inversions does not allow the curve obtained from $p(l) \leq$ the real data on inversions of length 20 and less, and vice-versa. For the distribution, on the other hand, values of α and β can be found that fit b of data, although for 1-20 gene inversions, the fit breaks down when $i \geq$

We found such values of the parameters of the gamma distribution imizing the sum of squared differences, between each real pair of geno the corresponding simulated pair, of the normalized number of singleversions in a minimal inversion scenario in plus the analogous difference normalized number of 1-20 gene inversions. The latter differences were by a factor of 0.1, since the number of short inversions was approxim times as large as the number of single-gene inversions. We iterated by fix parameter in turn and searching for the minimizing value of the other pa

6 Discussion

To what extent do our results bear on the question of whether there versal distribution of inversion lengths across the bacterial domain? A this distribution is the result of numerous mechanistic mutational pro the chromosomal level as well as selective processes operating on cell f function, both of which can be expected to vary among genomes.

The generality of the distribution can be assessed in part by the o of the sample points from the overall trend in Figure 3. While it is true a degree of statistical fluctuations, our results are thoroughly compat the hypothesis that all the pairs are following a common tendency. more distantly related genome pairs have fewer 1-20 gene inversions corresponding simulated pairs indicates some tendency for the signal short inversions to be lost for reasons other than genome rearrangement should affect the simulated and real pairs in the same way. The observed in the number of short inversions for normalized distances greater that 0.45 is partly due to an greater incidence of undetectable orthology in distant pairs, and partly to our way of treating unequal gene complete accumulated gene gain and loss for these pairs. Neither of these proble the simulated genome pairs. Whichever the explanation, the fact remains all the distant pairs manifest the same shortfall, and there is no idio behaviour from genome pair to genome pair evident at the aggregate le that overall inversion *frequency* is not addressed in our analysis, since using no external time measure to calibrate the genomic distances, but not pertinent to our results.

Recently, attention has been drawn to the prevalence and significance inversions, albeit more in eukaryotes [2, 10, 16, 13, 5] than in prokaryotes Here we have advanced our approach to the study of short inversions, ta vantage of the greatly elevated persistence in their evolutionary signal, c



Fig. 3. Fit of exponential and gamma models (open dots and trend lines) to single gene inversions and 1-20 gene inversions (filled dots). Exponential p $\lambda = 0.002$ or 0.05, gamma parameters $\alpha = 0.60, \beta = 1200$

to that of longer inversions. We found that the distribution of *inferred* is lengths could be accounted for by a gamma distribution for the gener versions, with a high proportion of single-gene and other short inverse a rapid but non-exponential initial decline. The initial 30 values of the distribution with parameters $\alpha = 0.60$, $\beta = 1200$ are depicted in Figure that we do not consider any but this first few values of l. The upper ta gamma distribution is not relevant to this study; indeed our generation dure truncates most all of the domain of the distribution greater than $\frac{l}{2}$ case, we are using the gamma as a descriptive device and are not sugges theoretically privileged in being mathematically derived from some mu or selective model for the inversion process. Note that in [11] we ruluniform distribution as descriptively inadequate, and in the present p also ruled out the exponential distribution.



Fig. 4. Gamma distribution with parameters $\alpha = 0.60, \beta = 1200$

How can the preference for short inversions be explained? We sug it is a combination of factors:

- Single-gene inversions may represent a particular evolutionary mo with selective functional consequences. They may allow a gene to obt scriptional independence from its erstwhile operon, or to otherwis its expression pattern, or to take advantage of new or altered func or to participate in a different pathway through a more appropriate positioning (cf genomic hitchhiking [14]).
- Single-gene inversions may simply be the clearest manifestation of versal tendency towards short inversions as the least disruptive of proximity configuration, and attendant functionality, of a genome. In argued that a predisposition for such inversions in small genomes in plain the prevalence of internally-shuffled "gene clusters" found acro sequenced genomes in microorganisms, in contrast to the "conser ments", including fixed gene order, pattern characteristic of the hikaryotes.
- Mechanistic process that favour mutational processes operating or distances.

Any knowledge about the distribution of inversion lengths would b able to the inference of genome rearrangements. It is very difficult t suitable data, however, so that the approach offered here is an examp indirect methods that must be developed in order to eventually home i true distribution.

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