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## **Neural network music composition by prediction: Exploring the benefits of psychoacoustic constraints and multiscale processing**

Michael C. Mozer

*Department of Computer Science  
and Institute of Cognitive Science  
University of Colorado  
Boulder, CO 80309-0430*

*e-mail:* mozer@cs.colorado.edu

### **Abstract**

In algorithmic music composition, a simple technique involves selecting notes sequentially according to a transition table that specifies the probability of the next note as a function of the previous context. I describe an extension of this transition table approach using a recurrent autopredictive connectionist network called CONCERT. CONCERT is trained on a set of pieces with the aim of extracting stylistic regularities. CONCERT can then be used to compose new pieces. A central ingredient of CONCERT is the incorporation of psychologically-grounded representations of pitch, duration, and harmonic structure. CONCERT was tested on sets of examples artificially generated according to simple rules and was shown to learn the underlying structure, even where other approaches failed. In larger experiments, CONCERT was trained on sets of J. S. Bach pieces and traditional European folk melodies and was then allowed to compose novel melodies. Although the compositions are occasionally pleasant, and are preferred over compositions generated by a third-order transition table, the compositions suffer from a lack of global coherence. To overcome this limitation, several methods are explored to permit CONCERT to induce structure at both fine and coarse scales. In experiments with a training set of waltzes, these methods yielded limited success, but the overall results cast doubt on the promise of note-by-note prediction for composition.

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In creating music, composers bring to bear a wealth of knowledge of musical conventions. Some of this knowledge is based on the experience of the individual, some is culture specific, and perhaps some is universal. No matter what the source, this knowledge acts to constrain the composition process, specifying, for example, the musical pitches that form a scale, the pitch or chord progressions that are agreeable, and stylistic conventions like the division of a symphony into movements and the AABB form of a gavotte. If we hope to build automatic composition systems that create agreeable tunes, it will be necessary to incorporate knowledge of musical conventions into the systems. The difficulty is in deriving this knowledge in an explicit form: even human composers are unaware of many of the constraints under which they operate (Loy, 1991).

In this article, a connectionist network that composes melodies with harmonic accompaniment is described. The network is called CONCERT, an acronym for connectionist composer of erudite tunes. (The "er" may also be read as erratic or ersatz, depending on what the listener thinks of its creations.) Musical knowledge is incorporated into CONCERT via two routes. First, CONCERT is trained on a set of sample melodies from which it extracts regularities of note and phrase progressions; these are *melodic and stylistic constraints*. Second, representations of pitch, duration, and harmonic structure that are based on psychological studies of human perception have been built into CONCERT. These representations, and an associated theory of generalization proposed by Shepard (1987), provide CONCERT with a basis for judging the similarity among notes, for selecting a response, and for restricting the set of alternatives that can be considered at any time. The representations thus provide CONCERT with *psychoacoustic constraints*.

The experiments reported here are with single-voice melodies, some with harmonic accompaniment in the form of chord progressions. The melodies range from 10 note sequences to complete pieces containing roughly 150 notes. A complete composition system should describe each note by a variety of properties—pitch, duration, phrasing, accent—along with more global properties such as tempo and dynamics. In the experiments reported here, the problem has been stripped down somewhat, with each melody described simply as a sequence of pitch-duration-chord triples. The burden of the present work has been to determine the extent to which CONCERT can discover the structure in a set of training examples.

Before turning to the details of CONCERT, I begin by describing a traditional approach to algorithmic music composition using Markov transition tables, the limitations of this approach, and how these limitations may be overcome in principle using connectionist learning techniques.

### **Transition table approaches to algorithmic music composition**

A simple but interesting technique in algorithmic music composition is to select notes sequentially according to a *transition table* that specifies the probability of the next note as a function of the current note (Dodge & Jerse, 1985; Jones, 1981; Lorrain, 1980). For example, the transition probabilities depicted in Table 1 constrain the next pitch to be one step up or down the C major scale from the current pitch. Generating a sequence according to this probability distribution therefore results in a musical random walk. Transition tables may be hand-constructed according to certain criteria, as in Table 1, or they may be set up to embody a particular musical style. In the latter case, statistics are collected over a set of examples (hereafter, the *training set*) and the transition table entries are defined to be the transition probabilities in these examples.

The transition table is a statistical description of the training set. In most cases, the transition table will lose information about the training set. To illustrate, consider the two sequences A B C and E F G. The transition table constructed from these examples will indicate that A goes to B with probability 1, B to C with probability 1, and so forth. Consequently, given the first note of each sequence, the table can be used to recover the complete sequence. However, with two sequences like B A C and D A E, the transition table can only say that following an A either an E or a C occurs, each with a 50% likelihood. Thus, the table cannot be used to unambiguously reconstruct the examples.

Clearly, in melodies of any complexity, musical structure cannot be fully described by the pairwise statistics. To capture additional structure, the transition table can be generalized from a two-dimensional array to  $n$  dimensions. In the  $n$ -dimensional table, often referred to as a *table of order  $n-1$* , the probability of the next note is indicated as a function of the previous  $n-1$  notes. By increasing the number of previous notes taken into consideration, the table becomes more context sensitive, and therefore serves as a more faithful representation of the training set.<sup>1</sup> Unfortunately, extending the transition table in this manner gives rise to two problems. First, the size of the table explodes exponentially with the amount of context and rapidly becomes unmanageable. With, say, 50 alternative pitches, 10 alternative durations, and a third-order transition table—modest sizes on all counts—7.5 billion entries are required. Second, a table representing the high-order structure masks the tremendous amount of low-order structure present. To elaborate, consider the sequence

A F G B F G C F G D F G# E F G .

One would need to construct a third-order table to faithfully represent this sequence. Such a table would indicate that, for example, the sequence G B F is always followed by G. However, there are first-order regularities in the sequence that a third-order table does not make explicit, namely the fact that an F is almost always followed by a G. The third-order table is thus unable to predict what will follow, say, A A F, although a first-order table would sensibly predict G. There is a tradeoff between the ability to faithfully represent the training set, which usually requires a high-order table, and the ability to generalize in novel contexts, which profits from a low-order table. What one would really like is a scheme by which only the *relevant* high-order structure is represented (Lewis, 1991).

Kohonen (1989; Kohonen, Laine, Tiits, & Torkkola, 1991) has proposed exactly such a scheme. The scheme is a symbolic algorithm that, given a training set of examples, produces a collection of rules—a context-sensitive grammar—sufficient for reproducing most or all of the structure inherent in the set. These rules are of the form *context* → *next\_note*, where *context* is a string of one or more notes, and

**Table 1: Transition probability from current pitch to the next**

<i>next pitch</i>	<i>current pitch</i>						
	C	D	E	F	G	A	B
C	0	.5	0	0	0	0	.5
D	.5	0	.5	0	0	0	0
E	0	.5	0	.5	0	0	0
F	0	0	.5	0	.5	0	0
G	0	0	0	.5	0	.5	0
A	0	0	0	0	.5	0	.5
B	.5	0	0	0	0	.5	0

<sup>1</sup> Following Smolensky (1988), I use the phrase *faithful representation* to mean that the represented items can be accurately reconstructed from the representation. A faithful transition-table representation of a set of examples would be one that, given the first few notes of any example, could unambiguously determine the remainder of the example.

*next\_note* is the next note implied by the context. Because the context length can vary from one rule to the next, the algorithm allows for varying amounts of generality and specificity in the rules. The algorithm attempts to produce deterministic rules—rules that always apply in the given context. Thus, the algorithm will not discover the regularity  $F \rightarrow G$  in the above sequence because it is not absolute. One could conceivably extend the algorithm to generate simple rules like  $F \rightarrow G$  along with exceptions (e.g.,  $D \rightarrow F \rightarrow G\#$ ), but the symbolic nature of the algorithm still leaves it poorly equipped to deal with statistical properties of the data. Such an ability is not critical if the algorithm's goal is to construct a set of rules from which the training set can be exactly reconstructed. However, if one views music composition as an intrinsically random process, it is inappropriate to model every detail of the training set. Instead, the goal ought to be to capture the most important—i.e., statistically regular—structural properties of the training set.

Both the transition table approach and Kohonen's musical grammar suffer from two further drawbacks. First, both algorithms are designed so that a particular note,  $n$ , cannot be used to predict note  $n+i$  unless all intervening notes,  $n+1 \cdots n+i-1$ , are also considered. In general, one would expect that the most useful predictor of a note is the immediately preceding note, but cases exist where notes  $n \cdots n+k$  are more useful predictors of note  $n+i$  than notes  $n+k+1 \cdots n+i-1$  (e.g., a melody in which high pitch and low pitch phrases alternate such as the solo violin partitas of J. S. Bach). The second, and perhaps more serious, drawback is that a symbolic representation of notes does not facilitate generalization from one musical context to perceptually similar contexts. For instance, the congruity of octaves is not encoded, nor is the abstract notion of intervals such as a 'minor third'.

Connectionist learning algorithms offer the potential of overcoming the various limitations of transition table approaches and Kohonen musical grammars. Connectionist algorithms are able to discover relevant structure and statistical regularities in sequences (e.g., Elman, 1990; Mozer, 1989). Indeed, connectionist algorithms can be viewed as an extension of the transition table approach, a point also noted by Dolson (1989). Just as the transition table approach uses a training set to calculate the probability of the next note in a sequence as a function of the previous notes, so does the network I'll describe, CONCERT. The connectionist approach, however, is far more flexible in principle: The form of the transition function can permit the consideration of varying amounts of context, the consideration of noncontiguous context, and the combination of low-order and high-order regularities.

The connectionist approach also promises better generalization through the use of distributed representations (Hinton, McClelland, & Rumelhart, 1986). In a local representation, where each note is represented by a discrete symbol, the sort of statistical contingencies that can be discovered are among notes. However, in a distributed representation, where each note is represented by a set of continuous feature values, the sort of contingencies that can be discovered are among *features*. To the extent that two notes share features, featural regularities discovered for one note may transfer to the other note.

### **Note-by-note composition**

The Markov transition table and the Kohonen algorithm both use a note-by-note technique in which notes are produced sequentially and linearly, from the start of a piece to the end, each note depending on the preceding context. Todd (1989; Bharucha and Todd, 1989) first explored this technique in a connectionist framework. Since then, it has been adopted by many other connectionist researchers (e.g., Stevens and Wiles, 1993). CONCERT also uses the note-by-note technique; it differs from earlier work primarily in that it uses an assortment of state-of-the-art connectionist tricks to achieve a sophisticated implementation of the technique (e.g., back propagation through time, probabilistic interpretation of the network outputs, a maximum likelihood training criterion, representational considerations) and tests the technique on a variety of relatively large-scale problems. By using a powerful architecture and learning algorithm, the

goal of the research is to see how far the note-by-note technique can be pushed. Previous research has been fairly uncritical in accepting and examining a network's performance; the simple fact that a network creates novel output tends to be interpreted as success. In this work, I evaluate CONCERT's performance on simple, well-structured sequences according to an objective criterion, and on complex musical examples according to the ears of experienced human listeners.

Despite the research effort expended on note-by-note composition, it might seem an unlikely technique to succeed. Music has a rich, hierarchical structure, from the level of notes within a theme, to themes within a phrase, to phrases within a movement, to movements within a symphony. One might well be skeptical that a sequential, linear composer could keep track of multiple levels of structure. In principle, however, the connectionist approach can; the present work is a test of whether it can do so in practice.

This type of linear technique has shown surprising and interesting results for natural language processing. Elman (1990, 1993) has trained sequential networks on strings of letters or words and has found that the networks could infer grammatical and semantic structure, even recursive structure. However, this work has focused primarily on the sentence level; one can hardly imagine that it would scale up to handle, say, semantic structure of paragraphs or short stories. Fortunately, music is unlike natural language in several simplifying respects: the set of atomic elements is finite, relatively small and unambiguous, and psychoacoustic and stylistic regularities abound. Consequently, constraints among elements are stronger. Thus, it seems a priori plausible that at least several levels of structure might be inferrable by a linear technique for music.

### The CONCERT architecture

CONCERT is a recurrent network architecture that learns to behave as an autopredictor (Elman, 1990). A melody is presented to it, one note at a time, and its task at each point in time is to predict the next note in the melody. Using a training procedure described below, CONCERT's connection strengths are adjusted so that it can perform this task correctly for a set of training examples. Each example consists of a sequence of notes. The current note in the sequence is represented in the input layer of CONCERT, and the prediction of the next note is represented in the output layer. The input and output layers both represent three aspects of a note: its pitch, its duration, and its harmonic chord accompaniment. As Figure 1 indicates, the next note is encoded in two different ways: The next-note-distributed (or *NND*) layer contains CONCERT's internal representation of the note—divided into three pools of units, forming distributed representations of pitch, duration, and harmony—while the next-note-local (or *NNL*) layer contains one unit for each alternative pitch, duration, and chord. The representation of a note in the *NND* layer, as well as in the input layer, is based on a psychophysical studies, described further below. For now, it should suffice to say that this representation is distributed, i.e., a note is indicated by a *pattern* of activity across the units. Because such patterns of activity can be quite difficult to interpret, the *NNL* layer provides an alternative, explicit representation of the possibilities.

The context layer can represent relevant aspects of the input history, that is, the temporal context in which a prediction is made. When a new note is presented in the input layer, the activity pattern currently in the context layer is integrated with the new note to form a new context representation. In general terms,

$$\mathbf{c}(n) = f(\mathbf{c}(n-1), \mathbf{x}(n)),$$

where  $\mathbf{x}(n)$  is a vector representing the  $n$ th note in the input sequence,  $\mathbf{c}(n)$  is the context activity pattern following processing of input note  $n$ —which I refer to as *step*  $n$ —and  $f$  is a member of the class of functions that can be implemented by the connectionist hardware. At the start of each sequence the context layer is cleared, i.e.,  $\mathbf{c}(0) = \mathbf{0}$ .



Once CONCERT has been trained, it can be run in *composition mode* to create new pieces. This involves first seeding CONCERT with a short sequence of notes, perhaps the initial notes of one of the training examples. From this point on, the output of CONCERT can be fed back to the input, allowing CONCERT to continue generating notes without further external input. Generally, the output of CONCERT does not specify a single note with absolute certainty; instead, the output is a probability distribution over the set of candidates. It is thus necessary to select a particular note in accordance with this distribution. This is the role of the selection process depicted in Figure 1.

### Unit activation rules

The activation rule for the context units is

$$c_i(n) = s \left[ \sum_j w_{ij} x_j(n) + \sum_j v_{ij} c_j(n-1) \right], \quad (1)$$

where  $c_i(n)$  is the activity of context unit  $i$  at step  $n$ ,  $x_j(n)$  is the activity of input unit  $j$  at step  $n$ ,  $w_{ij}$  is the connection strength from unit  $j$  of the input to unit  $i$  of the context layer, and  $v_{ij}$  is the connection strength from unit  $j$  to unit  $i$  within the context layer, and  $s$  is the standard logistic activation function rescaled to the range  $(-1,1)$ . Units in the NND layer follow a similar rule:

$$nnd_i(n) = s \left[ \sum_j u_{ij} c_j(n) \right],$$

where  $nnd_i(n)$  is the activity of NND unit  $i$  at step  $n$  and  $u_{ij}$  is the strength of connection from context unit  $j$  to NND unit  $i$ .

The NND and NNL representations can be broken into three component vectors, corresponding to pitch, duration, and chord representations. I describe here the transformation from the NND pitch representation to the NNL pitch representation; the transformation for the duration and chord representations is similar. The pitch transformation is achieved by first computing the distance between the NND pitch representation,  $\mathbf{nndp}(n)$ , and the target (distributed) representation of each pitch  $i$ ,  $\mathbf{p}_i$ :

$$d_i = ||\mathbf{nndp}(n) - \mathbf{p}_i||,$$

where  $||\cdot||$  denotes the  $L_2$  vector norm. This distance is an indication of how well the NND representation matches a particular pitch. The activation of the NNL unit corresponding to pitch  $i$ ,  $nmlp_i$ , increases as the distance decreases:

$$nmlp_i(n) = \frac{e^{-d_i}}{\sum_j e^{-d_j}}.$$

This normalized exponential transform was first proposed by Bridle (1990) and Rumelhart (in press). It produces an activity pattern over the NNL units in which each unit has activity in the range  $(0,1)$  and the activity of all units sums to 1. Consequently, the NNL activity pattern can be interpreted as a probability distribution—in this case, the probability that the next note has a particular pitch. An analogous transformation is performed to determine the activity of NNL units that represent note duration and accompanying chord. The distance measure and the exponential function have their basis in psychological theory (Shepard, 1987), a point I elaborate on shortly.

### Training procedure

CONCERT is trained using a variation of the back propagation algorithm (Rumelhart, Hinton, & Williams, 1986) which adjusts the connection strengths within CONCERT so that the network can perform the next-note prediction task for a set of training examples. The algorithm requires first defining a measure of the network's performance—of how good a job the network does at predicting each note in each of the training examples. Commonly, a squared difference measure of error is used:

$$E_{lms} = \sum_{q,n,j} (nmlp_j(n,q) - \delta(j, P(n,q)))^2 + \sum_{q,n,j} (nnld_j(n,q) - \delta(j, D(n,q)))^2 + \sum_{q,n,j} (nmlc_j(n,q) - \delta(j, C(n,q)))^2,$$

where  $q$  is an index over pieces in the training set,  $n$  an index over notes within a piece, and  $j$  an index over pitch, duration, or chord units in the NNL layer;  $P(n,q)$ ,  $D(n,q)$ ,  $C(n,q)$  are the indices of the target pitch, duration, and chord for note  $n$  of piece  $q$ ;  $\delta(a,b) = 1$  if  $a = b$  or 0 otherwise. This measure is minimized when the outputs of the units corresponding to the correct predictions are 1 and the outputs of all other units are 0.

Another performance measure is sensible in the context of output units that have a probabilistic interpretation (Bridle, 1990; Rumelhart, in press). Because each NNL unit's output represents the probabilistic expectation of a pitch, performance depends on predicting the appropriate notes with high probability. This suggests the likelihood performance measure

$$L = \prod_{q,n} nmlp_{P(n,q)}(n,q) nnld_{D(n,q)}(n,q) nmlc_{C(n,q)}(n,q),$$

which is the joint probability of making the correct prediction for all notes of all pieces.<sup>2</sup> A log likelihood criterion,

$$E = -\log L = -\sum_{q,n} \log nmlp_{P(n,q)}(n,q) + \log nnld_{D(n,q)}(n,q) + \log nmlc_{C(n,q)}(n,q),$$

is used instead because it is easier to work with, and has the same extrema as  $L$ .

Back propagation specifies how the weights in the network should be changed to reduce  $E$ . This involves computing the gradient of  $E$  with respect to the weights in the network:  $\partial E/\partial \mathbf{W}$ ,  $\partial E/\partial \mathbf{V}$ , and  $\partial E/\partial \mathbf{U}$ . The first step in this process is computing the gradient with respect to the activity of units in the NND layer, and then propagating this gradient back to the weights in layers below. For the NND pitch units,

$$\frac{\partial E}{\partial nndp(n,q)} = \left[ \frac{nndp(n,q) - \rho_{P(n,q)}}{d_{P(n,q)}} - \sum_i nmlp_i(n,q) \frac{nndp(n,q) - \rho_i}{d_i} \right].$$

Back propagation still cannot be used to train CONCERT directly, because CONCERT contains recurrent connections and the algorithm applies only to feedforward networks. Several variations of the algorithm

<sup>2</sup> Of course, this interpretation assumes independence of the predictions, which is certainly not true in CONCERT. However, Bridle (1990) provides another justification, somewhat less intuitive, for this performance measure in terms of an information theoretic criterion.

have been proposed for dealing with recurrent networks (Williams & Zipser, in press). I've used the "back propagation through time" (BPTT) procedure of Rumelhart et al. (1986), which transforms a recurrent network into an equivalent feedforward network.<sup>3</sup> This training procedure computes the true gradient of the objective function with respect to the various network weights. This means that if an input note at step  $l$  has any predictive utility at some later time  $n$ , then in principle the algorithm should adjust the connections so that note  $l$  is maintained in the network's memory. Contingencies over time should be discovered when they exist. There is a weaker version of BPTT that passes error back only a fixed number of steps (e.g., the training procedure used by Elman, 1990), which in principle makes contingencies across longer time spans more difficult to maintain and discover. CONCERT has been furnished with the most powerful connectionist recurrent-network learning procedure in order to endow it with the best possible chance of success.

### Representing musical elements

Having described CONCERT's architecture, dynamics, and training procedure, I turn to the issue of representing a musical piece. A piece is defined as a sequence of elements, each of which is characterized by a melody pitch, a melody duration, and a harmonic chord accompaniment. The pitch and duration specify the notes of the melody, each of which is accompanied by a chord (or silence). This encoding synchronizes the melody and the harmony. Although chord changes generally occur at a slower rate than changes in the melody line, this is encoded simply by repeating chords for each note of the melody until the chord changes. The three elements—pitch, duration, and chord representation—are discussed in turn.

#### *Pitch representation*

To accommodate a variety of music, CONCERT needs the ability to represent a range of about four octaves. Using standard musical notation, these pitches are labeled as follows: C1, D1, ..., B1, C2, D2, ... B2, C3, ... C5, where C1 is the lowest pitch and C5 the highest. Sharps and flats are denoted with # and b, respectively, e.g., C#3 and Gb2. Within an octave, there are twelve chromatic steps; the range C1–C5 thus includes 49 pitches.

Perhaps the simplest representation of pitch is to have one unit for each possibility. The pitch C1 would be represented by the activity vector  $[1\ 0\ 0\ \dots]^T$ , C#1 by the vector  $[0\ 1\ 0\ \dots]^T$ , and so forth. An alternative would be to represent pitch by a single unit whose activity was proportional to the frequency of the pitch. One might argue that the choice of a pitch representation is not critical because back propagation can, in principle, discover an alternative representation well suited to the task (Hinton, 1987). In practice, however, researchers have found that the choice of external representation is a critical determinant of the network's ultimate performance (e.g., Denker et al., 1987; Mozer, 1987). Quite simply, the more task-appropriate information that is built into the network, the easier the job the learning algorithm has.

Laden and Keefe (1989) advocate the approach of including as much information as possible from psychoacoustics into the design of networks for music perception and cognition. They have developed a model of chord classification that categorizes triads as major, minor, or diminished chords. Classification performance is superior with the use of a representation that explicitly encodes harmonics of the fundamental pitches.

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<sup>3</sup> An unforgivable pun: Rob Goldstone suggested calling CONCERT's training procedure *Bach propagation*.



neighboring pitches are a tonal half-step apart. In the circle of fifths, the perfect fifth of a pitch is the next pitch immediately counterclockwise.<sup>5</sup> The proximity of two pitches in the five-dimensional PHCCCF space can be determined simply by computing the Euclidean distance between their representations.

Shepard presents detailed arguments for the psychological validity of the PHCCCF representation. I briefly point out some of its benefits. Consider first the PH and CC components. In this three-dimensional subspace, pitches form a helix in which the winding of the helix is due to the chroma circle and the height is due to the pitch height. As pitches proceed up the chromatic scale, they wind up the helix. Pitches exactly one octave apart are directly above one another on the helix; that is, they have the same locus on the chroma circle but different values of pitch height. For this reason, octaves have similar representations. Depending on how the PH component is scaled relative to the CC (i.e., how elongated the helix is), pitches like C1 and C2 may even be closer in the representational space than pitches like C1 and B1, even though C1 is closer to B1 in frequency.

The circle of fifths endows the representation with other desirable properties. First, the circle localizes the tones in a musical key. Any seven adjacent tones correspond to a particular key. For instance, the tones of the C major and A minor diatonic scales—C, D, E, F, G, A, and B—are grouped together on the circle of fifths. The most common pentatonic keys are similarly localized. Second, and perhaps more critical, the circle of fifths can explain the subjective equality of the intervals of the diatonic scale. To elaborate, Shepard points out that people tend to hear the successive steps of the major scale as equivalent, although with respect to log frequency, some of the intervals are only half as large as others. For example, in C major, the E-F and B-C steps are half tones apart (minor seconds) while all others are a whole tone apart (major seconds). The combination of the pitch height and circle of fifths permits a representation in which the distance between all major and minor seconds is the same. This is achieved by using a scale ratio of approximately 3:1 for the chroma circle relative to the circle of fifths.

One desirable property of the overall PHCCCF representation is that distances between pitches are invariant under transposition. Consider any two pitches, say, D2 and G#4. Transposing the pitches preserves the distance between them in the PHCCCF representation. Thus, the distance from D2 to G#4 is the same as from E2 to A#4, from D1 to G#3, and so forth. See Bharucha (1991) for a further discussion of the psychological issues involved in the representation of musical pitch.

The relative importance of the PH, CC, and CF components can be varied by adjusting the diameters of the chroma circle and circle of fifths. For example, if the two circles have the same diameter, then, in terms of the CC and CF components, the distance between C and G is the same as the distance between C and B. This is because B is one notch from the C on the chroma circle and five notches on the circle of fifths, while the G is five notches away on the chroma circle and one on the circle of fifths. However, if the diameter of the chroma circle is increased, then C is closer to B than to G (based on the distance in the four-dimensional CC and CF subspace); if the diameter is decreased, C is closer to G than to B. If the diameters of both circles are decreased relative to the pitch height scale, then pitch frequency becomes the most important determinant of similarity. Shepard argues that the weighting of the various components depends on the particular musical task and the listener's expertise. Based on Shepard's evidence, a reasonable representation for expert musicians is to weigh the CF and CC components equally, and to set the diameter of the CC and CF components equal to the distance of one octave in PH. This is the scale shown in Figure 2.

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<sup>5</sup> The perfect fifth is a musically significant interval. The frequency ratio of a note to its perfect fifth is 2:3, just as the frequency ratio of a note to its octave is 1:2.

The final issue to discuss is how the PHCCCF representation translates into an activity vector over a set of connectionist units. A straightforward scheme is to use five units, one for pitch height and two pairs to encode the  $(x,y)$  coordinates of the pitch on the two circles.<sup>6</sup>

One problem with this scheme is that, if the units have the usual sigmoidal activation function, equal spacing of tones in pitch height or on the circles in unit *activity* space is not preserved in unit *net input* space. This means that context units attempting to activate NND units do not reap the full benefit of the representation (e.g., transposition invariance). A second problem with the simple five-unit scheme is that each unit encodes a coordinate value directly; there are 7 discrete values for the x- and y-coordinates of the circles, 49 for the pitch height. Consequently, minor perturbations of the activity vector could lead to misinterpretations.

Due to these problems, an alternative representation of the CC and CF components has been adopted. The representation involves 6 binary-valued units to represent a tone on each circle; the representation for chroma circle tones is shown in Table 2. This representation preserves the essential distance relationships among tones on the chroma circle: the distance between two tones is monotonically related to the angle between the tones. Because each unit has to encode only two distinct values, the representation is less sensitive to noise than is one in which each unit encodes a coordinate of the circle.

Unfortunately, there is no similar scheme that can be used to encode pitch height in a boolean space of reasonably low dimensionality that preserves intrinsic distance relationships. Consequently, I have used a single linear unit for pitch height. Although this means that the pitch height unit can take on 49 distinct values, it is not critical that the unit represent a value with great accuracy. The pitch height unit essentially conveys information about the octave; information about the pitch within an octave can be gleaned from the values on the other dimensions. Consequently, a precise response of the pitch height unit is not crucial. Its activity is scaled to range from  $-9.798$  for C1 to  $+9.798$  for C5. This scaling achieves the desired property previously described that the distance in the CC or CF component between pitches on opposite sides of the circle equals the distance between pitches one octave apart in the PH component.<sup>7</sup>

**Table 2: Representation of tones on chroma circle**

<i>tone</i>	<i>representation</i>					
C	-1	-1	-1	-1	-1	-1
C#	-1	-1	-1	-1	-1	+1
D	-1	-1	-1	-1	+1	+1
D#	-1	-1	-1	+1	+1	+1
E	-1	-1	+1	+1	+1	+1
F	-1	+1	+1	+1	+1	+1
F#	+1	+1	+1	+1	+1	+1
G	+1	+1	+1	+1	+1	-1
G#	+1	+1	+1	+1	-1	-1
A	+1	+1	+1	-1	-1	-1
A#	+1	+1	-1	-1	-1	-1
B	+1	-1	-1	-1	-1	-1

<sup>6</sup> The reader may wonder why points on a circle need to be represented in a two-dimensional space. After all, the points lie on a 1D continuum, albeit embedded in a 2D space. Without such an embedding, however, distance relationships between points cannot be preserved. If the circle is cut and flattened into a 1D continuum, formerly adjacent points on opposite sides of the cut will end up far apart.

<sup>7</sup> Although a PH scale factor of 9.798 was used for the target NND representation,  $p_i$ , a PH scale factor of 1.0 was used for the input representation. This was based on empirical studies of what scale factors yielded the best performance. The primary rea-

The PHCCCF representation consists of 13 units altogether. Sample activity patterns for some pitches are shown in Table 3. Rests (silence) are assigned a unique code, listed in the last row of the Table, that is maximally different from all pitches. The end of a piece is coded by a series of rests.

As with any distributed representation, there are limitations as to how many and which pitches can be represented simultaneously. The issue arises because the NND layer needs to be able to encode a set of alternatives, not just a single pitch. If, say, A1, D2, and E2 are equally likely as the next note, the NND layer must indicate all three possibilities. To do so, it must produce an activity vector that is nearer to  $\mathbf{p}_{A1}$ ,  $\mathbf{p}_{D2}$ , and  $\mathbf{p}_{E2}$  than to other possibilities. The point in PHCCCF space that is simultaneously closest to the three pitches is simply the average vector,  $(\mathbf{p}_{A1} + \mathbf{p}_{D2} + \mathbf{p}_{E2})/3$ . Table 4 shows the pitches nearest to the average vector. As hoped for, A1, D2, and E2 are the nearest three. This is not always the case, though. Table 5 shows the pitches nearest to the average vector which represents the set {A1, D2, D#2}. This illustrates the fact that certain clusters of pitches are more compact in the PHCCCF space than others. The PHCCCF representation not only introduces a similarity structure over the pitches, but also a limit on the combinations of pitches that can be considered simultaneously. Arbitrary limitations are a bad thing in general, but here, the limitations are theoretically motivated.

**Table 3: PHCCCF representation for selected pitches**

<i>pitch</i>	<i>PH</i>	<i>CC</i>						<i>CF</i>					
C1	-9.798	+1	+1	+1	-1	-1	-1	-1	-1	-1	+1	+1	+1
F#1	-7.349	-1	-1	-1	+1	+1	+1	+1	+1	+1	-1	-1	-1
G2	-2.041	-1	-1	-1	-1	+1	+1	-1	-1	-1	-1	+1	+1
C3	0	+1	+1	+1	-1	-1	-1	-1	-1	-1	+1	+1	+1
D#3	1.225	+1	+1	+1	+1	+1	+1	+1	+1	+1	+1	+1	+1
E3	1.633	-1	+1	+1	+1	+1	+1	+1	-1	-1	-1	-1	-1
A4	8.573	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1
C5	9.798	+1	+1	+1	-1	-1	-1	-1	-1	-1	+1	+1	+1
rest	0	+1	-1	+1	-1	+1	-1	+1	-1	+1	-1	+1	-1

**Table 4: Distance from representation of {A1,D2,E2} to nearest 10 pitches**

<i>rank</i>	<i>pitch</i>	<i>distance</i>	<i>rank</i>	<i>pitch</i>	<i>distance</i>
1	D2	2.528	6	C#2	4.422
2	E2	2.779	7	A2	4.422
3	A1	3.399	8	E1	4.441
4	B1	3.859	9	G1	4.497
5	C2	4.130	10	G2	4.497

**Table 5: Distance from representation of {A1,D2,D#2} to nearest 10 pitches**

<i>rank</i>	<i>pitch</i>	<i>distance</i>	<i>rank</i>	<i>pitch</i>	<i>distance</i>
1	D2	2.373	6	D#2	3.774
2	C2	3.277	7	A1	3.946
3	E2	3.538	8	F2	4.057
4	C#2	3.654	9	A#1	4.146
5	B1	3.714	10	G1	4.323

---

son that a PH scale factor other than 1.0 on the inputs causes difficulties is that the resulting error surface is poorly conditioned when different units have different activity ranges (Widrow & Stearns, 1985).





### *Chord representation*

The chord representation is based on Laden and Keefe's (1989) proposal for a psychoacoustically grounded distributed representation. I begin by summarizing the Laden and Keefe proposal and then explain how it was modified for CONCERT.

The chords used here are in root position and are composed of three or four component pitches; some examples are shown in Table 6. Consider each pitch separately. In wind instruments, bowed string instruments, and singing voices, a particular pitch will produce a harmonic spectrum consisting of the fundamental pitch (e.g., for C3, 440 hz), and harmonics that are integer multiples of the fundamental (880 hz, 1320 hz, 1760 hz, and 2200 hz). Laden and Keefe projected the continuous pitch frequency to the nearest pitch class of the chromatic scale, e.g., 440 to C3, 880 to C4, 1320 to G3, 1760 to C5, and 2200 to E5, where the projections to G3 and E5 are approximate. Using an encoding in which there is an element for each pure pitch class, a pitch was represented by activating the fundamental and the first four harmonics. The representation of a chord consisted of the superimposition of the representations of the component pitches. To allow for the range C3-C7, 49 elements are required. In Laden and Keefe's work, a neural network with this input representation better learns to classify chords as major, minor, or diminished than a network with an acoustically neutral input representation.

Several modifications of this representation were made for CONCERT. The octave information was dropped, reducing the dimensionality of the representation from 49 to 12. The strength of representation of harmonics was exponentially weighted by their harmonic number; the fundamental was encoded with an activity of 1.0, the first harmonic with an activity of .5, the second harmonic with an activity of .25, and so forth. Activities were rescaled from a 0-to-1 range to a -1-to-1 range. Finally, an additional element was added to the representation based on a psychoacoustic study of perceived chord similarity. Krumhansl, Bharucha, and Kessler (1982) found that people tended to judge the tonic, subdominant, and dominant chords (i.e., C, F, and G in the key of C) as being quite similar. This similarity was not present in the Laden and Keefe representation. Hence, an additional element was added to force these chords closer together. The element had value +1.5 for these three chords (as well as C7, F7, and G7), -1.5 for all other chords. Hierarchical clustering shows some of the similarity structure of the 13-dimensional representation (Figure 5).

### **Basic simulation results**

Many decisions had to be made in constructing CONCERT. In pilot simulation experiments, I explored various aspects of CONCERT, including: variants in the representations, such as using two units to represent the circles in the PHCCCF representation instead of six; alternative error measures, such as the mean-squared error; and the necessity of the>NNL layer. Empirical comparisons supported the architecture and representations described earlier.

**Table 6: Elements of chords**

<i>chord</i>	<i>component pitches</i>			
C major	C3	E3	G3	
C minor	C3	E $\flat$ 3	G3	
C augmented	C3	E3	G $\sharp$ 3	
C diminished	C3	E $\flat$ 3	G $\flat$ 3	
C7	C3	E3	G3	B $\flat$ 3

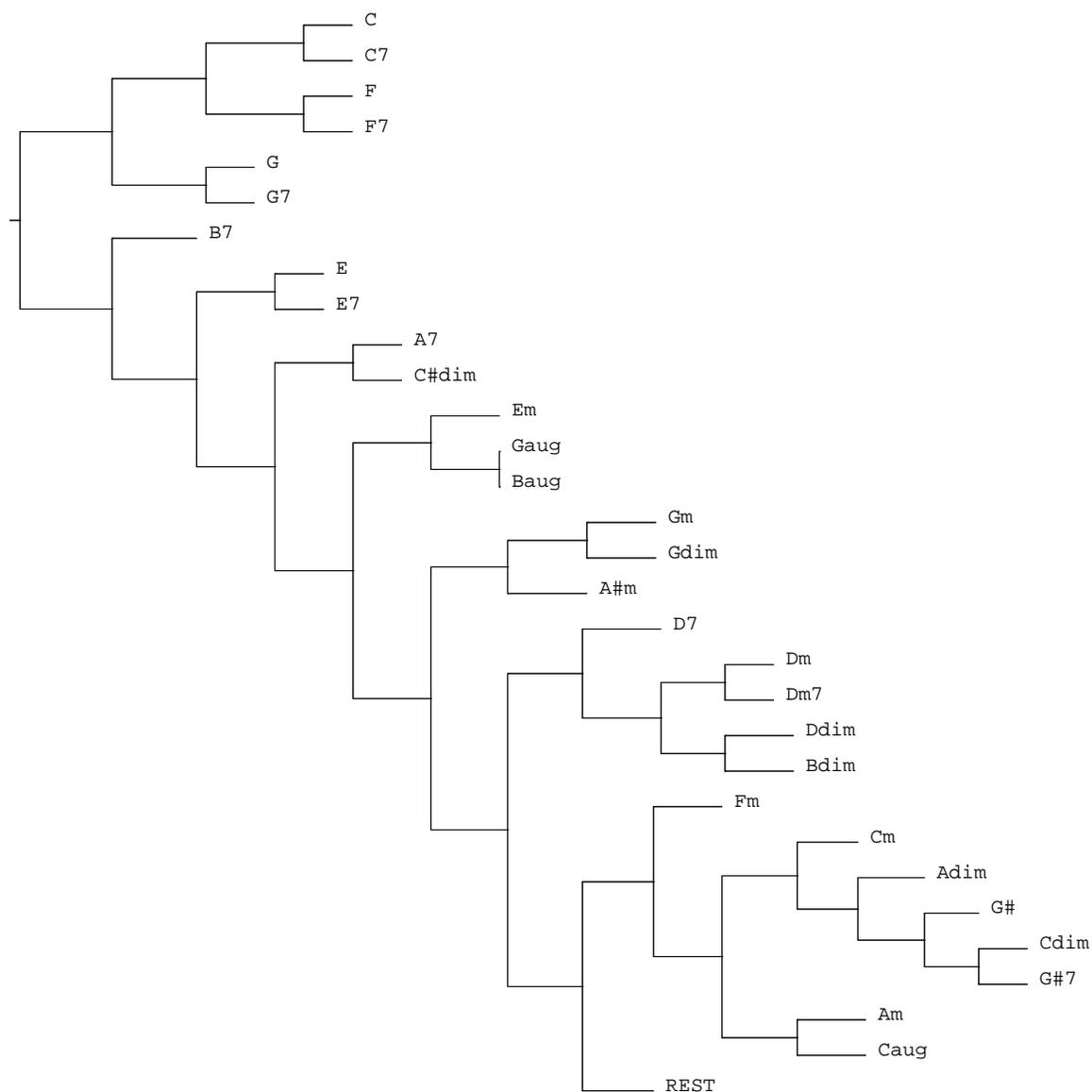


Figure 5. Hierarchical clustering of the representations of various chords used in simulation studies.

One potential pitfall in the research area of connectionist music composition is the uncritical acceptance of a network's performance. It is absolutely essential that a network be evaluated according to some objective criterion. One cannot judge the enterprise to be a success simply because the network is creating novel output. Even random note sequences played through a synthesizer sound interesting to many listeners. Thus, I begin an examination of CONCERT's performance by testing CONCERT on simple artificial pitch sequences, with the aim of verifying that it can discover the structure known to be present. In these sequences, there was no variation in duration and harmony; consequently, the duration and chord components of the input and output were ignored.

*Extending a C major diatonic scale*

To start with a simple experiment, CONCERT was trained on a single sequence consisting of three octaves of a C major diatonic scale: C1 D1 E1 F1 ... B3. The target at each step was the next pitch in the scale: D1 E1 F1 G1 ... C4. CONCERT is said to have learned the sequence when, at each step, the activity of the NNL unit representing the target at that step is more active than any other NNL unit. In 10 replications of the simulation with different random initial weights, 15 context units, a learning rate of .005, and no momentum, CONCERT learned the sequence in about 30 passes. Following training, CONCERT was tested on four octaves of the scale. CONCERT correctly extended its predictions to the fourth octave, except that in 4 of the 10 replications, the final note, C5, was transposed down an octave. Table 7 shows the CONCERT's output for two octaves of the scale. Octave 3 was part of the training sequence, but octave 4 was not. Activities of the three most active NNL pitch units are shown. Because the activities can be interpreted as probabilities, one can see that the target is selected with high confidence.

CONCERT was able to learn the training set with as few as 2 context units, although surprisingly, generalization performance tended to improve as the number of context units was increased. CONCERT was also able to generalize from a 2 octave training sequence, but it often transposed pitches down an octave.

*Learning the structure of diatonic scales*

In this simulation, CONCERT was trained on a set of diatonic scales in various keys over a one octave range, e.g., D1 E1 F#1 G1 A1 B1 C#2 D2. Thirty-seven such scales can be made using pitches in the C1-C5 range. The training set consisted of 28 scales—roughly 75% of the corpus—selected at random, and the test set consisted of the remaining 9. In 10 replications of the simulation using 20 context units, CONCERT mastered the training set in approximately 55 passes. Generalization performance was tested by presenting the scales in the test set one pitch at a time and examining CONCERT's prediction. This is not the same as running CONCERT in composition mode because CONCERT's output was not fed back to the input; instead, the input was a predetermined sequence. Of the 63 pitches to be predicted in the test set, CONCERT achieved remarkable performance: 98.4% correct. The few errors were caused by transposing pitches one full octave or one tonal half step.

To compare CONCERT with a transition table approach, a second-order transition table was built from the training set data and its performance measured on the test set. The transition table prediction (i.e., the pitch with highest probability) was correct only 26.6% of the time. The transition table is somewhat of a

**Table 7: Performance on octaves 3 and 4 of C major diatonic scale**

<i>input pitch</i>	<i>output unit activities</i>					
C3	D3	0.961	C3	0.017	E3	0.014
D3	E3	0.972	D3	0.012	F3	0.007
E3	F3	0.982	D#3	0.008	G3	0.006
F3	G3	0.963	F3	0.015	A3	0.010
G3	A3	0.961	G3	0.024	B3	0.012
A3	B3	0.972	A3	0.025	C4	0.002
B3	C4	0.979	A#3	0.010	C#4	0.005
C4	D4	0.939	C4	0.040	E4	0.009
D4	E4	0.968	D4	0.018	F4	0.006
E4	F4	0.971	D#4	0.016	E4	0.005
F4	G4	0.931	F4	0.037	F#4	0.015
G4	A4	0.938	G4	0.044	B4	0.007
A4	B4	0.915	A4	0.080	A#4	0.003
B4	C5	0.946	A#4	0.040	B4	0.011

straw man for this task: A transition table that is based on absolute pitches is simply unable to generalize correctly. Even if the transition table encoded relative pitches, a third-order table would be required to master the environment. Kohonen's musical grammar faces the same difficulties as a transition table.

A version of CONCERT was tested using a local pitch representation in the input and NND layers instead of the PHCCCF representation. The local representation had 49 pitch units, one per tone. Although the NND and NNL layers may seem somewhat redundant with a local pitch representation, the architecture was not changed to avoid confounding the comparison between representations with other possible factors. Testing the network in the manner described above, generalization performance with the local representation and 20 context units was only 54.4%. Experiments with smaller and larger numbers of context units resulted in no better performance.

### *Learning random walk sequences*

In this simulation, ten-element sequences were generated according to a simple rule: The first pitch was selected at random, and then successive pitches were either one step up or down the C major scale from the previous pitch, the direction chosen at random. The pitch transitions can easily be described by a transition table, as illustrated in Table 1. CONCERT, with 15 context units, was trained for 50 passes through a set of 100 such sequences. If CONCERT has correctly inferred the underlying rule, its predictions should reflect the plausible alternatives at each point in a sequence. To test this, a set of 100 novel random walk sequences was presented. After each note  $n$  of a sequence, CONCERT's performance was evaluated by matching the top two predictions—the two pitches with highest activity—against the actual note  $n+1$  of the sequence. If note  $n+1$  was not one of the top two predictions, the prediction was considered to be erroneous. In ten replications of the simulation, the mean performance was 99.95% correct. Thus, CONCERT was clearly able to infer the structure present in the patterns. CONCERT performed equally well, if not better, on random walks in which chromatic steps (up or down a tonal half step) were taken. CONCERT with a local representation of pitch achieved 100% generalization performance.

### *Learning interspersed random walk sequences*

The sequences in this simulation were generated by interspersing the elements of two simple random walk sequences. Each interspersed sequence had the following form:  $a_1, b_1, a_2, b_2, \dots, a_5, b_5$ , where  $a_1$  and  $b_1$  are randomly selected pitches,  $a_{i+1}$  is one step up or down from  $a_i$  on the C major scale, and likewise for  $b_{i+1}$  and  $b_i$ . Each sequence consisted of ten pitches. CONCERT, with 25 context units, was trained on 50 passes through a set of 200 examples and was then tested on an additional 100. In contrast to the simple random walk sequences, it is impossible to predict the second pitch in the interspersed sequences ( $b_1$ ) from the first ( $a_1$ ). Thus, this prediction was ignored for the purpose of evaluating CONCERT's performance. CONCERT achieved a performance of 94.8% correct. Excluding errors that resulted from octave transpositions, performance improves to 95.5% correct. CONCERT with a local pitch representation achieves a slightly better performance of 96.4%.

To capture the structure in this environment, a transition table approach would need to consider at least the previous two pitches. However, such a transition table is not likely to generalize well because, if it is to be assured of predicting a note at step  $n$  correctly, it must observe the note at step  $n-2$  in the context of every possible note at step  $n-1$ . I constructed a second-order transition table from CONCERT's training set. Using a testing criterion analogous to that used to evaluate CONCERT, the transition table achieved a performance level on the test set of only 67.1% correct. Kohonen's musical grammar would face the same difficulty as the transition table in this environment.

### *Learning AABA phrase patterns*

The melodies in this simulation were formed by generating two phrases, call them A and B, and concatenating the phrases in an AABA pattern. The A and B phrases consisted of five-note ascending chromatic scales, the first pitch selected at random. The complete melody then consisted of 21 elements—four phrases of five notes followed by a rest marker—an example of which is:

```
F#2 G2 G#2 A2 A#2 F#2 G2 G#2 A2 A#2 C4 C#4 D4 D#4 E4 F#2 G2  
G#2 A2 A#2 REST.
```

These melodies are simple examples of sequences that have both fine and coarse structure. The fine structure is derived from the relations among pitches within a phrase, the coarse structure is derived from the relations among phrases. This pattern set was designed to examine how well CONCERT could cope with multiple levels of structure and long-term dependencies, of the sort that is found (albeit to a much greater extent) in real music.

CONCERT was tested with 35 context units. The training set consisted of 200 examples and the test set another 100 examples. Ten replications of the simulation were run for 300 passes through the training set.

Because of the way that the sequences were organized, certain pitches could be predicted based on local context whereas other pitches required a more global memory of the sequence. In particular, the second to fifth pitches within a phrase could be predicted based on knowledge of the immediately preceding pitch. To predict the first pitch in the repeated A phrases and to predict the rest at the end of a sequence, more global information is necessary. Thus, the analysis was split to distinguish between pitches that required only local structure and pitches that required more global structure. Generalization performance was 97.3% correct for the local components, but only 58.4% for the global components.

### *Discussion*

Through the use of simple, structured training sequences, it is possible to evaluate the performance of CONCERT. The initial results from CONCERT are encouraging. CONCERT is able to learn structure in short sequences with strong regularities, such as a C major scale and a random walk in pitch. Two examples of structure were presented that CONCERT can learn but that cannot be captured by a simple transition table or by Kohonen's musical grammar. One example involved diatonic scales in various keys, the other involved interspersed random walks.

CONCERT clearly benefits from its psychologically-grounded representation of pitch. In the task of extending the C major scale, CONCERT with a local pitch representation would simply fail. In the task of learning the structure of diatonic scales, CONCERT's generalization performance drops by nearly 50% when a local representation is substituted for the PHCCCF representation. The PHCCCF representation is not always a clear win: generalization performance on random walk sequences improves slightly with a local representation. However, this result is not inconsistent with the claim that the PHCCCF representation assists CONCERT in learning structure present in human-composed melodies. The reason is that random walk sequences are hardly based on the sort of musical conventions that gave rise to the PHCCCF representation, and hence, the representation is unlikely to be beneficial. In contrast, musical scales are at the heart of many musical conventions; it makes sense that scale-learning profits from the PHCCCF representation. Human-composed melodies should fare similarly. Beyond its ability to capture aspects of human pitch perception, the PHCCCF representation has the advantage over a local representation of

reducing the number of free parameters in the network. This can be an important factor in determining network generalization performance.

The result from the AABA-phrase experiment is disturbing, but not entirely surprising. Consider the difficulty of correctly predicting the first note of the third repetition of the A phrase. The listener must remember not only the first note of the A phrase, but also that the previous phrase has just ended (that five consecutive notes ascending the chromatic scale were immediately preceding) and that the current phrase is not the second or fourth one of the piece (i.e., that the next note starts the A phrase). Minimally, this requires a memory that extends back 11 notes. Moreover, most of the intervening information is irrelevant.

### **Capturing higher-order musical organization**

In principle, CONCERT trained with back propagation should be capable of discovering arbitrary contingencies in temporal sequences, such as the global structure in the AABA phrases. In practice, however, many researchers have found that back propagation is not sufficiently powerful, especially for contingencies that span long temporal intervals and that involve high order statistics. For example, if a network is trained on sequences in which one event predicts another, the relationship is not hard to learn if the two events are separated by only a few unrelated intervening events, but as the number of intervening events grows, a point is quickly reached where the relationship cannot be learned (Mozer, 1989, 1992, 1993; Schmidhuber, 1992). Bengio, Frasconi, and Simard (1993) present theoretical arguments for inherent limitations of learning in recurrent networks.

This poses a serious limitation on the use of back propagation to induce musical structure in a note-by-note prediction paradigm because important structure can be found at long time scales as well as short. A musical piece is more than a linear string of notes. Minimally, a piece should be characterized as a set of musical phrases, each of which is composed of a sequence of notes. Within a phrase, local structure can probably be captured by a transition table, e.g., the fact that the next note is likely to be close in pitch to the current, or that if the past few notes have been in ascending order, the next note is likely to follow this pattern. Across phrases, however, a more global view of the organization is necessary.

The difficult problem of learning coarse as well as fine structure has been addressed recently by connectionist researchers (Mozer, 1992; Mozer & Das, 1993; Myers, 1990; Ring, 1992; Schmidhuber, 1992; Schmidhuber, Mozer, & Prelinger, 1993). The basic idea in many of these approaches involves building a *reduced description* (Hinton, 1988) of the sequence that makes global aspects more explicit or more readily detectable. In the case of the AABA structure, this might involve taking the sequence of notes composing A and redescribing them simply as "A". Based on this reduced description, recognizing the phrase structure AABA would involve little more than recognizing the sequence AABA. By constructing the reduced description, the problem of detecting global structure has been turned into the simpler problem of detecting local structure.

The challenge of this approach is to devise an appropriate reduced description. I describe here the simple scheme in Mozer (1992) as a modest step toward a solution. This scheme constructs a reduced description that is a bird's eye view of the musical piece, sacrificing a representation of individual notes for the overall contour of the piece. Imagine playing back a song on a tape recorder at double the regular speed. The notes are to some extent blended together and indistinguishable. However, events at a coarser time scale become more explicit, such as a general ascending trend in pitch or a repeated progression of notes. Figure 6 illustrates the idea. The curve in the top graph, depicting a sequence of individual pitches, has been smoothed and compressed to produce the bottom graph. Mathematically, "smoothed and compressed" means that the waveform has been low-pass filtered and sampled at a lower rate. The result



Several comments regarding this approach.

- Figure 6 is inaccurate in that it represents a filtering of the raw input sequence. The idea proposed here actually involves a filtering of the transformed input (i.e., the representation in the context layer). Regardless, the basic intuition applies in either case.
- Time constants have been incorporated into the activation rules of other connectionist architectures. Most pertinent is Bharucha and Todd's (1989) use of fixed time constants to implement an exponentially decaying memory of input context. McClelland's (1979) cascade model makes use of time constants in a feedforward network. The continuous-time networks of Pearlmutter (1989) and Pineda (1987) are based on a differential equation update rule, of which Equation 2 is a discrete time version. Mozer (1989) proposed an architecture for sequence recognition that included linear-integrator units. However, none of this work has exploited time constants to control the temporal responsivity of individual units.
- Although Figure 6 depicts only two time scales, context units can operate at many different time scales, with smaller values of  $\tau_i$  specializing the units to be sensitive to local properties of the sequence and larger values specializing the units to be sensitive to more global properties. One obvious possibility is to use back propagation to determine the appropriate values of  $\tau_i$ ; however, my suspicion is that there are many local optima blocking the path to the best  $\tau_i$ .
- This approach specializes each context unit for a particular time scale. Nonetheless, it allows for interactions between representations at different time scales, as each context unit receives input from all others. Thus, CONCERT can in principle learn to encode relationships between structure at different scales.
- Equation 2 suggests one particular type of reduced description, consisting of a smoothed and compressed representation of the context unit response over time. This is a simple-minded reduced description; ideally, one would like the reduced description to characterize meaningful "chunks" or events in the input sequence. I expand upon this idea upon later in the article.

### *AABA phrase patterns revisited*

In the experiment with AABA phrase patterns described earlier, the CONCERT architecture contained 35 context units, all with  $\tau = 0$ . In this experiment, called the *reduced description* or *RD* version, 30 context units had  $\tau = 0$  and 5 had  $\tau = 0.8$ . The experiment was otherwise identical. Table 8 compares the generalization performance of the original and RD networks, for predictions involving local and global structure. Performance involving global structure was significantly better for the RD version ( $F(1,9)=179.8$ ,  $p<.001$ ), but there was only a marginally reliable difference for performance involving local structure ( $F(1,9)=3.82$ ,  $p=.08$ ). The global structure can be further broken down to prediction of the end of the sequence and prediction of the first pitch of the repeated A phrases. In both cases, the performance improvement for the RD version was significant: 88.0% versus 52.9% for the end of sequence ( $F(1,9)=220$ ,  $p<.001$ ); 69.4% versus 61.2% for the first pitch ( $F(1,9)=77.6$ ,  $p<.001$ ).

**Table 8: Performance on AABA phrases**

<i>structure</i>	original net	RD net
local	97.3%	96.7%
global	58.4%	75.6%

Experiments with different values of  $\tau$  in the range .7–.95 yielded qualitatively similar results, as did experiments in which the A and B phrases were formed by random walks in the key of C. Overall, modest improvements in performance are observed, yet the global structure is never learned as well as the local, and it is clear that CONCERT’s capabilities are no match to those of people in this simple domain.

### Larger simulation experiments

In the next three sections, I describe simulations using real music as training data, and including the reduced description technique described in the previous section.

#### *Composing melodies in the style of Bach*

The melody line of ten simple pieces by J. S. Bach were used to train CONCERT (Table 9). The set of pieces is not particularly coherent; it includes a variety of musical styles. The primary thing that the pieces have in common is their composer. The original pieces had several voices, but the melody generally appeared in the treble voice. Importantly, to naive listeners the extracted melodies sounded pleasant and coherent without the accompaniment.

In the training data, each piece was terminated with a sequence of three rests. This allowed CONCERT to learn not only the notes within a piece but also when the end of the piece was reached. Further, each major piece was transposed to the key of C major and each minor piece to the key of A minor. This was done to facilitate learning because the pitch representation does not take into account the notion of musical key; hopefully, a more sophisticated pitch representation would avoid the necessity of this step.

Two fixed input units were included in this simulation. One indicated whether the piece was in a major versus minor key, another whether the piece was in 3/4 meter versus 2/4 or 4/4. These inputs did not change value for a given piece. To keep CONCERT on beat, an additional input unit was active for notes that were on the downbeat of each measure. If a note was tied from one measure to the next, it was treated as two events; this assured each downbeat would correspond to a distinct input event.<sup>8</sup>

Learning the examples involves predicting a total of 1,260 notes altogether. CONCERT was trained with 40 hidden units, 35 with  $\tau = 0$  and 5 with  $\tau = .8$ , for 3000 passes through the training set. The learning rate was gradually lowered from .0004 to .0002. By the completion of training, CONCERT could correctly predict about 95% of the pitches and 95% of the durations correctly. Attempts were made to train

**Table 9: Bach training examples**

<i>piece</i>	<i>number of notes</i>
Minuet in G major (no. 1)	126
Minuet in G major (no. 2)	166
Minuet in D minor	70
Minuet in A minor	84
Minuet in C minor	80
March in G major	153
March in D major	122
March in Eb major	190
Musette in D major	128
Little prelude in C major	121

<sup>8</sup> To maintain information about note ties, an additional component of the duration representation signaled whether a note was tied from the previous.





To encourage the consideration of structure on a longer time scale, a final experiment introduced harmonic accompaniment to the melody line. The training examples were a set of 25 waltzes by various composers, collected in a "Fakebook" with a rhythmically-simplified melody line and accompanying chord progressions. The change in chords occurred at a slower rate than the change in notes of the melody: In the training set, the average duration of a melody note was 1.4 beats, while the average duration between chord changes was 5.9 beats. Consequently, one might hope that in order to learn the structure of the chord progression, it would be necessary to span longer periods of time, and hence, it would be necessary for CONCERT to extract higher-level structure from the pieces.

Each note in the input was accompanied by the current chord. Chord duration was not explicitly represented; the duration of a chord was simply the sum of the durations of the consecutive notes that were associated with the chord.

Figure 9 shows two compositions produced by CONCERT based on the waltz data set. There was little evidence in the compositions that significant global structure was learned.

### *Discussion*

While CONCERT performs well on simple, structured, artificial sequences, the prognosis looks bleaker for natural music. One critic described CONCERT's creations as "compositions only their mother could love." To summarize more delicately, few listeners would be fooled into believing that the pieces had been composed by a human. While the local contours made sense, the pieces were not musically coherent, lacking thematic structure and having minimal phrase structure and rhythmic organization.

It appears that the CONCERT architecture and training procedure do not scale well as the length of the pieces grow and as the amount of higher-order structure increases. This comes as no surprise to some: learning the structure of music through a note-by-note analysis is formally the same task as learning to read and understand English from a letter-by-letter analysis of text. Nonetheless, many researchers are pursuing a linear note-by-note approach to music analysis and composition. This is not entirely naive, as connectionist algorithms are in principle capable of discovering the multiple levels of structure in music. However, the experiments reported here show no cause for optimism in practice, despite the use of state-of-the-art connectionist architectures and training algorithms, and attempts to encourage CONCERT to learn global structure.

The present results clearly signal difficulty in using sequential networks to match transition probability distributions of arbitrary order. Even more sophisticated approaches are clearly needed. I mention several directions that one might consider in the domain of music analysis and composition.

- *Multiple recurrent hidden layers.* The current CONCERT architecture is limited in that the update rule for the context layer is a squashed linear mapping. That is, the new context is a linear function of the old context and current input, passed through a squashing function. To give CONCERT more flexibility in the update rule, one might consider multiple hidden layers in the recurrent loop (for related work, see Cottrell & Tsung, 1993; Tsung & Cottrell, 1993).
- *Alternative approaches to remembering the past.* There are many connectionist approaches to constructing a memory of past events for the purpose of predicting the future (Mozer, 1993; Principe, Hsu, & Kuo, 1994). CONCERT with the RD units would be considered a TIS-exponential architecture according to Mozer's taxonomy. Another promising approach might be to include a small buffer in the input and/or context layers to hold a history of recent activities, allowing local temporal structure to be learned without wasting the resources of the recurrent connections.



performed, it seems promising and worth pursuing.

- *Chunking architectures.* In the cascaded sequential networks described above, the network designers specify in advance the hierarchical decomposition of a linear sequence. Todd (1991) assumes that an explicit decomposition is included as part of the training process. Burr and Miyata (1993) assume that successively higher levels operate on fixed, slower time scales: the lowest level net is updated once a beat, the next net once every three beats, the next net every twelve beats, and so forth. Rather than providing the system with a hierarchical decomposition, one would really like for the system to discover the decomposition itself. Ideally, each level of the hierarchy should encode meaningful "chunks" or events in the sequence—the nature of a chunk being determined by the statistics of the environment—and the next higher level should operate on these chunks. Schmidhuber, Mozer, and Prelinger (1993) describe an architecture of this sort in which the higher level analyzes only components of the input that cannot be interpreted by the lower level, yielding an automatic decomposition of sequences. This architecture has not been tested on musical sequences. Mozer and Das (1993) present an explicit chunking mechanism that has the capability of creating new symbols to represent an abstraction of a sequence of input elements. The mechanism operates on the generated symbols just as it does on the input elements, allowing it to recursively chunk the chunks. The creation of new symbols achieves a reduced description that is more flexible than the time constant method proposed in this article. The time constant method attempts to derive global statistics, whereas the chunking mechanism derives only local statistics, but does so over abstractions of the input. We are presently exploring how the chunking mechanism performs on musical sequences.
- *Explicit representation of structure.* In the final simulation study, CONCERT was trained to predict harmonic accompaniment, which naturally operates at a coarser time scale than the melody itself. The hope was that by including this coarser structure as an explicit component of the task, CONCERT would be forced to learn it. One can push this idea further and include structure at even coarser time scales, e.g., the sort of description that musicologists might use to characterize or analyze a piece, such as phrase boundaries, themes, inversions, key modulations. Given training data annotated with these descriptions, CONCERT would have the opportunity to learn global structure explicitly.
- *Staged training.* Music appears to have a tremendous amount of local structure that can mask the presence of global structure. The evidence for this comes from the fact that CONCERT performed very well on training sets even without paying attention to global structure. One might get around this problem by staging training in CONCERT, first training RD units with large time constants, and then gradually introducing units with smaller (and zero) time constants in the course of training. This would force CONCERT to examine the more global structure from the start.
- *Representations of musical elements in context.* In the current work, the encoding of pitch, duration, and harmony is independent of the temporal context in which the elements are embedded. This is clearly wrong from a psychological perspective: in music, as in every domain of cognition, context and expectations affect the interpretation of perceptual elements. A truer cognitive architecture would allow interactions between the processes that determine the encoding and the processes—modeled in CONCERT—that generate expectancies (see Bharucha, 1987, 1991, for a relaxation model that has this general flavor). Another way of embodying this interaction is to consider the representation of musical elements in a musical context. The representations of pitch and chords in CONCERT are based on psychoacoustic studies that consider only pairwise similarities. Psychological studies of pitch and harmony in a musical context (e.g., Krumhansl, 1990; Krumhansl & Kessler, 1982; Longuet-Higgins, 1976, 1979) could potentially be of value in incorporating the preceding input history into the network's representations. Similarly,

structured representations of rhythm (e.g., Lerdahl & Jackendoff, 1983; McAuley, 1993) might help to impose higher-level organization on the input sequences.

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